HYBRID ELECTRIC VEHICLE SIMULINK TOOLBOX

USER'S GUIDE TECHNICAL NOTES PATHS VALIDATION

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By

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13. ABSTRACT (Maximum 200 words)

A general purpose toolbox was developed for modeling and simulation of electric and hybrid electric vehicles (HEV). This simulation and modeling toolbox, referred to as PATHS (Performance Assessment Toolbox for Hybrid Systems) was developed using Matlab® and Simulink®. PATHS is a forward-looking model organized into a suite of libraries, each containing modular computer models of typical HEV components. The objective of the developed toolbox is to provide the user the ability to model, simulate and analyze the performance of a custom-built or pre-existing HEV. PATHS is a physics-based modeling and simulation toolbox. The equations used to model the different components were derived from classical text books, using sound engineering methods. PATHS was also validated against a 22-foot series hybrid shuttle bus operated on a chassis dynamometer.

This report is divided into the following sections: User's Guide, Technical Notes, and PATHS Validation.

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EXECUTIVE SUMMARY

The HEV toolbox was initially conceived as a "standard" set of modules for use in evaluating the performance of concept HEV architecture. This effort resulted in the development of a general-purpose HEV modeling and simulation toolbox, named PATHS (Performance Assessment Toolbox for Hybrid Systems). PATHS is based on principles of physics models, developed in Matlab® and Simulink®, is modularized into several libraries and uses the forward-looking approach. It can be used to obtain detailed performance characteristics of the modeled HEV or its sub-components, as well as perform parametric trade-off studies. Particularly useful is the ability to size components and evaluate their effects on vehicle performance in computer simulation prior to prototyping or fabricating hardware. The following are possible applications of the toolbox: evaluation of new drivetrain options / architectures; test and debug hybrid vehicle control strategies; sub-componentssizing and specifications; evaluation of hardware modifications on HEV performance; impact of software modifications on HEV performance and other sub-components; build a computer model of a HEV before hardware prototyping.

The following is the current list of libraries within PATHS: engine library, electric machine library, energy storage library, vehicle library, controllers library, couplings library, and a miscellaneous library. The multiple components within a library have the same input-output structure so that they can be interchanged in an HEV model. The user can also add to the library as long as the input-output structure of the particular library is maintained. PATHS is fully customizable as long as the user adheres to the input-output structure of each library and is aware of the existing naming convention of the variables.

Validation of PATHS was performed by first developing a computer model of a 22-foot series hybrid shuttle bus, followed by comparing its output to data collected from the same bus on a chassis dynamometer. The hybrid shuttle bus was placed on a heavy-duty chassis dynamometer and driven by a human operator, while data was collected from the drive motors, Auxiliary Power Unit (APU), batteries, and vehicle speed sensors. This data was compared with model predictions, executing the same driving profile as that of the hybrid bus. Both steady state and transient comparisons were made between the bus and the model. Fuel consumption predicted by the APU model was within 1% over 6 EPA cycles of measured data. The battery state of charge predicted by the lead-acid battery model was within 5% over 6 EPA cycles of measured data. The motor model predictions (transient / steady state) are within 10% of measured data for low speeds and lower throttle positions. Larger deviations between the measured and model predicted data at larger speeds and higher throttle positions. The dynamic vehicle model validated to within 2% of measured data.

This report is divided into the following sections: User's Guide, Technical Notes, and PATHS Validation.

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HYBRID ELECTRIC VEHICLE SIMULINK TOOLBOX

(Commercial Vehicle Version)

USER'S GUIDE

Version 1.1

1.0 OVERVIEW OF DARPA HEV SIMULATION TOOLBOX

1.1 Background

The DARPA HEV Simulation Toolbox was initially conceived as a "standard" set of modules for use in evaluating the performance of concept Hybrid Electric Vehicle (HEV) architectures in simulated driving conditions. Two versions of the toolbox are in existence: one for commercial applications, and one for military applications. Both toolboxes contain the same modules. However, the simulation toolbox for military applications contains an additional library of military specific modules. The HEV simulation toolbox was collectively developed by the following organizations:

| Southwest Research Institute (SwRI) | Dr. A. Nedungadi | (210) 522-3965 |
|---|---------------------|----------------|
| Univ. of TX Inst. for Adv. Technology (IAT) | Dr. Scott Fish | (512) 471-9060 |
| Georgia Institute of Technology (GT) | Dr. Thomas Habetler | (404) 894-8929 |
| Univ. of Hawaii (UH) | Dr. Vassilis Syrmos | (808) 956-3432 |
| Univ. of TX Center of Electro-Mechanics (CEM) | Mr. John Kajs | (512) 471-4496 |

1.2 Introduction

This user's guide provides a concise description of the commercial version of the DARPA HEV simulation toolbox. Use of this toolbox is restricted to licensees of the software. An application for a license to the commercial version of the simulation toolbox is available by contacting SwRI (Dr. A. Nedungadi (210) 522-3965). All applications for a license agreement to use the military version of the simulation toolbox must be addressed to IAT (Dr. Scott Fish (512) 471-9060).

The simulation toolbox is organized into a suite of libraries, each containing modular computer models of typical HEV components. All the models were developed using MATLAB[©] and its graphical click-and-pick modeling tool, Simulink[©]. The objective of the developed toolbox is to

provide the user the essential building blocks to simulate and analyze the performance of a custom built or pre-existing electric hybrid vehicle.

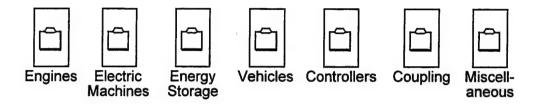


Figure 1. Hybrid Electric Vehicle Simulink Toolbox (Commercial)

The following list describes all the libraries and models available within the toolbox:

| ENGINE LIBRARY |
|---|
| Table lookup diesel engine without emissions |
| Table lookup gas turbine engine without emissions |
| Spark ignition dynamic engine with emissions |
| ELECTRIC MACHINE LIBRARY |
| AC induction steady-state motor |
| AC induction dynamic motor |
| Permanent magnet steady-state generator |
| Permanent magnet dynamic generator |
| Table lookup steady-state generator |
| ENERGY STORAGE LIBRARY |
| Lead acid battery |
| flywheel battery |
| Capacitor |

| VEHICLE LIBRARY |
|--|
| Tracked vehicle |
| Wheeled vehicle (version 1 and 2) |
| Wheel (version 1 and 2) |
| ☐ Driver |
| |
| CONTROLLERS LIBRARY |
| Energy management (2) |
| Energy storage system controller |
| APU controller |
| System controller |
| |
| COUPLINGS LIBRARY |
| Gear box |
| Engine-generator coupling |
| Motor-wheel coupling (version 1 and 2) |
| |
| MISCELLANEOUS LIBRARY |
| DC-DC converter |
| AC-AC converter |
| AC-DC converter |
| DC-AC converter |
| Capacitor |
| Roller bearing |
| Magnetic bearing |
| Windage model |
| Driving profile |
| |

A rigid naming convention was used for all the variables used within the developed models. The first three alphabetic characters represent the abbreviation of the model name. The fourth

single alphabetic character represents the possible device type, if one exists. The fifth single numeric character between 0 and 9 represents the number of instances of this item. The sixth character is a required underscore, followed by the variable name. Table 1 summarizes all the model names, the respective three character abbreviations that describe the particular model name, and all possible device types for each model.

| Table 1. Summary Of Model Names, Abbreviations And Device Types | | | | |
|---|--------------|--|--|--|
| MODEL | ABBREVIATION | POSSIBLE DEVICE TYPES | | |
| Engine | eng | s (spark ignition) d (diesel) t (turbine) s (stirling) | | |
| Motor | mot | I (induction - steady-state) k (induction - dynamic) | | |
| Generator | gen | p (permanent magnet - steady-state) q (permanent magnet - dynamic) | | |
| Energy Storage System | ess | b (lead acid battery) f (flywheel) c (capacitor) | | |
| Axle | axl | none | | |
| Coupling | cpl | none | | |
| Wheel | whl | none | | |
| Vehicle | veh | none | | |
| Transmission | trm | m (manual) a (automatic) | | |
| Controller | ctl | none | | |

For example, the variable motI1_VAr represents the first instance of the variable name VAr of the induction motor model. The variable genp2_J represents the second instance of the variable name J of the permanent magnet generator model. MATLAB[©] is case sensitive, therefore motI1 VAr is not the same as moti1_VAr.

The following format is used to describe each model. A table summarizes the required inputs and outputs of the model, followed by a list of constants that are used within the model. Any auxiliary calculations that are not part of the output are listed in the section of auxiliary calculations. This is followed by the first three lines of the mask (consult your Simulink manual) of the model. This is provided to enable the user to recreate the mask if it is accidentally deleted.

A list of assumptions is listed for each model, enabling the user to determine if the complexity of the model would suffice for the given application. Finally, typical values of the constants used within each of the models are presented to give the user an indication of the appropriate order of magnitude of the constants used during simulation of the different models.

This user's guide is accompanied by a technical notes document that contains all the differential equations/equations used within each of the models. These equations are provided to enable the user to assess the applicability of the particular model to the application in question. If certain modifications or extensions are required, the user will have to retrieve the particular model from the Simulink® environment and make the required changes.

It is assumed that the user is an experienced Simulink user since many of the developed models use similar advanced features. It is also assumed that the user has working knowledge of system modeling and interfacing modules with multiple inputs and outputs. The user interacts with the developed toolbox by simply dragging the required item from the appropriate toolbox library and connecting it with other modules while adhering to the input and output connections described in this manual.

The developed models have all been tested through numerous computer simulations. The equations used to model the different components were derived from classical text books, using sound engineering methods. Validation of the most essential components has been completed (see accompanying validation report). It is possible to tweak the parameters used within each model to make its performance compare to the physical system. This calibration task is left to the user if he/she needs to calibrate a particular model to a known physical system. The numerous simulations performed during the verification phase indicate that the simulation of a complex system, such as an electric hybrid vehicle, can be significantly affected by either parameter mismatch within a model or intercomponent mismatch. Typically, this is diagnosed by the simulation taking very small time steps or simulation instabilities.

2.0 ENGINE LIBRARY

The engine library contains three types of engines: (1) table lookup steady-state diesel engine without emissions, (2) table lookup steady-state gas turbine engine without emissions, and (3) a dynamic model of a spark ignition engine with emission calculations. In an HEV application, the engine model is typically connected to a generator using a mechanical coupling from the coupling library (see Section 6). The first two engine models incorporate a lag response time with steady-state performance tables. Their use maintains the shape of the torque vs. speed and throttle setting function while scaling for the desired shaft speed and torque at design conditions. The third engine model is a more detailed dynamic model of a spark-ignition engine.

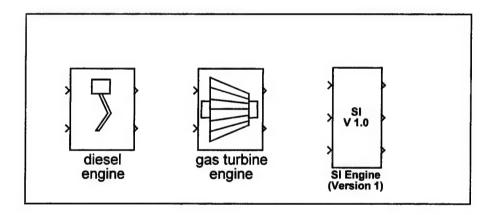
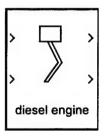


Figure 2. Engine Model Library

2.1 Diesel Engine



| INPUTS | OUTPUTS |
|---|---|
| Non-Dimensional Throttle Control (0-1) | Vector of Engine Torque (N-m) and Inertia Constant (kg*m^2) |
| Engine Shaft Speed (RPM) | Fuel Mass (kg) |

Purpose: The purpose of the diesel engine model is to accurately represent the engine torque and fuel consumption characteristics to its input throttle setting and shaft speed. The model

is quasi-steady with a user-defined first order lag in response to the throttle. Other than the engine lag, the performance is determined by table lookup with steady-state performance data. The fuel consumption data is in lb/(hp hr) and is assumed not to vary with engine power rating. The torque table is scaled with the engine power and speed to remain consistent.

Parameters: Note: These values are loaded from disk through the mask or inputted by the user.

engd1_pwr engine design power (hp)
engd1_spd engine design speed (rpm)
engd1_J inertia constant (kg*m^2)
fuel_mass_i initial fuel mass (kg)

sample_N max number of samples

sample_T simulation time between samples

Auxiliary Calculations: None

Diesel Engine Mask

(1) ENGD

(2) Diesel Engine Block Definitions\n(Click on "Help" to list Inport and Outport Parameters.)|[pwr(hp),spd(rpm),J(kgm2)]|Initial Fuel Mass (kg)|[sample N,sample T]

(3) load('engd');pwr=@1(1)*746;spd=@1(2)*pi/30;J=@1(3);fuel_i=@2; sample N=@3(1);sample T=@3(2);

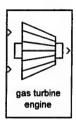
(4) Drawing Command.

(5) Diesel Engine Block Port Parameters.\n\nInport 1: Nondimensional command signal (throttle setting) from diesel engine controller block.\nInport 2: Speed from the generator coupler block.\n\nOutport 1: Vector of [ENGT_T, ENGT_J] output to the generator coupler block.

Model Equations: The diesel model here is composed of three parts. The first part applies a $1/\tau s$ transfer function to the throttle, modeling the response time lag in the actual machine to inputs from the throttle. The second two parts determine the output torque and specific fuel consumption from steady-state lookup tables that are scaled from a known diesel engine

performance set. It is assumed that the steady-state performance tables are adequate when combined with the engine lag to describe the actual performance of a dynamic model. No calculations are included for emissions in this model.

2.2 Gas Turbine Engine



| INPUTS | OUTPUTS |
|--------------------------|-------------------------------|
| Non-Dimensional | Vector of Engine Torque (N-m) |
| Throttle Control (0-1) | and Inertia Constant (kg*m^2) |
| Engine Shaft Speed (RPM) | Fuel Mass (kg) |

Purpose: The purpose of the gas turbine model is to accurately represent the engine torque and fuel consumption characteristics to its input throttle setting and shaft speed. The model is quasi-steady with a user-defined first order lag in response to the throttle. Other than the engine lag, the performance is determined by table lookup with steady-state performance data. The fuel consumption data is in lb/(hp hr) and is assumed not to vary with engine power rating. The torque table is scaled with the engine power and speed to remain consistent. The output fuel mass represents remaining mass of fuel in tanks connected to this engine. This data can be used to account for weight loss in time by vehicle dynamics models.

Parameters: Note: These values are loaded from disk through the mask or inputted by the user.

engt1_pwr engine design power (hp)
engt1_spd engine design speed (rpm)
engt1_J inertia constant (kg*m^2)
fuel mass i initial fuel mass (kg)

sample_N max number of samples

sample T simulation time between samples

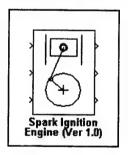
Auxiliary Calculations: None

Gas Turbine Engine Mask

- (1) ENGT
- (2) Gas Turbine Engine Block Definitions\n(Click on "Help" to list Inport and Outport Parameters.)|[pwr(hp),spd(rpm),J(kgm2)]|Initial Fuel Mass(kg)|[sample N,sample T]
- (3) load('engtdata');pwr=@1(1)*746;spd=@1(2)*pi/30;J=@1(3);fuel_i=@2; sample N=@3(1); sample T=@3(2);
- (4) Drawing Commands
- (5) Gas Turbine Engine Block Port Parameters.\n\nInport 1: Throttle Command (0->1).\nInport 2: Shaft Speed (RPM).\n\nOutport 1: Vector of [Shaft Torque (N*m), Inertia Constant $(kg*m^2)$].

Model Equations: The gas turbine model here is composed of three parts. The first part applies a 1/ts transfer function to the throttle, modeling the response time lag in the actual machine to inputs from the throttle. The second two parts determine the output torque and specific fuel consumption from steady-state lookup tables that are scaled from a known diesel engine performance set. It is assumed that the steady-state performance tables are adequate, when combined with the engine lag, to describe the actual performance of a dynamic model. No calculations are included for emissions in this model.

2.3 Spark Ignition Engine



| INPUTS | OUTPUTS |
|----------------------------|--------------------------|
| Throttle Fraction [0-1] | Output Torque [Nm] |
| Desired Engine Speed [rpm] | Engine Inertia [kgm²] |
| Engine ON/OFF Switch [0/1] | Total Fuel Consumed [kg] |

% General constants:

eng universal gas const:

Universal gas constant [J/kmol/K]

eng std pres:

Standard pressure [Pa]

eng std temp:

eng mol wt_air:

Standard temperature [K]

eng gas const air:

Molecular weight of the air [kg/kmol] Specific gas constant for air [J/kg/K]

eng std air density:

Density of standard air [kg/m³]

eng mol wt exhaust:

Molecular weight of exhaust gases [kg/kmol]

eng gas const exhaust:

Specific gas constant for exhaust gases [J/kg/K]

% Primary engine scaling parameters

eng displacement:

Engine displacement [m³]

eng rated speed:

Maximum engine rated speed [rad/s]

% Secondary engine scaling parameters

eng compression ratio:

Engine compression ratio []

eng rated bmep:

Brake mean effective pressure at rated conditions [Pa]

eng rated torque:

Rated engine torque [N-m]

eng rated power: eng rated vol eff: Rated engine power [watts] Volumetric efficiency at rated conditions [fraction]

eng rated air vol flow:

Air volume flow rate at rated conditions [m³/s]

eng rated air mass flow:

Air mass flow rate at rated conditions [kg/s]

% SI Engine 2 (Main model)

eng ambient pressure:

Ambient pressure [Pa]

eng ambient temperature:

Ambient temperature [K]

eng ambient air density: eng inertia:

Density of ambient air [kg/m³] Engine rotary inertia [kg-m²]

eng off torque factor:

Factor for engine torque when engine is off [N-m / rad/s]

% Air fuel system (1)

eng manifold volume ratio: Ratio of intake manifold to engine displacement []

eng manifold volume:

Volume of intake manifold [m³]

% Air system (1.1)

eng throttle bypass ratio:

Ratio of bypass flow area around throttle to total throttle area

[fraction]

eng rated intake vacuum:

Intake manifold vacuum at rated conditions [Pa]

eng rated pres ratio infl:

Pressure ratio influence factor (in flow equation) at rated

conditions [fraction]

eng max air flow:

Maximum air flow through throttle (choked) [kg/s]

eng speed density weight:

Fractional weight for speed density air flow compared to mass

flow sensor [fraction]

% Fuel system (1.2)

eng af ratio speed:

Vector of engine speed for air fuel ratio [rad/s]

eng af ratio Pi:

Vector of intake manifold pressure for air fuel ratio table [Pa];

eng af ratio table:

Air fuel ratio table [number]

% Mixing and dynamics (1.3)

eng liquid fuel fraction:

Fraction of fuel that stays in liquid form [fraction]

eng fuel evaporation time const:

Time constant for evaporation of liquid fuel in intake

manifold wall [sec]

% Reciprocator air flow (2.1)

eng vol eff speed:

Vector of engine speed for volumetric efficiency table [rad/s]

eng vol eff Pi:

Vector of intake manifold pressure for volumetric efficiency

table [Pa]

eng vol eff table:

Volumetric efficiency table [number]

% Torque production (2.2)

eng nominal isfc:

(Nominal) indicated specific fuel consumption [kg/J]

eng fmep factor 0:

Correlation factor 0 for friction mean effective pressure []

eng fmep factor 1:

Correlation factor 1 for friction mean effective pressure []

eng fmep factor 2:

Correlation factor 2 for friction mean effective pressure []

% Engine exhaust (2.3)

eng stoich af ratio:

Stoichiometric air fuel ratio []

eng exh temp af coef:

Correlation factor for effect of air fuel ratio on exhaust temp.[] Vector of engine speed for exhaust temperature table [rad/s]

eng exh temp speed: eng exh temp Pi:

Vector of intake manifold pressure for exhaust temp. table [Pa]

eng exh temp table:

Exhaust temperature table [K]

eng emissions speed:

Vector of engine speed for engine emission tables [rad/s]

eng emissions Pi:

Vector of intake manifold pressure for engine out emission

tables [Pa]

eng emissions HC table:

Engine out hydrocarbon emissions table [kg/kg fuel]

eng emissions CO table: eng emissions NOx table:

Engine out carbon monoxide emissions table [kg/kg/fuel] Engine out oxides of nitrogen emissions table [kg/kg fuel]

eng emissions PM table:

Engine out particulate matter emissions table [kg/kg fuel]

% Muffler and aftertreatment (3)

eng rated exhaust pressure:

Exhaust pressure at rated conditions [Pa]

eng exh pres scaling:

Scaling factor for matching exhaust pressure []

eng rated exhaust temperature: eng rated exhaust density:

Exhaust temperature at rated conditions [K] Density of exhaust at rated conditions [kg/m³]

eng muffler pressure factor:

Correlation factor for engine muffler pressure [] Catalyst conversion efficiency for oxides of nitrogen []

eng catalyst eff NOx: eng catalyst eff HC:

Catalyst conversion efficiency for hydrocarbons []

eng catalyst eff CO: eng catalyst eff PM:

Catalyst conversion efficiency for carbon monoxide [] Catalyst conversion efficiency for particulate matter [] The following variables (last value) are saved in work space for post run analysis:

eng_s_speed: Engine speed [rad/sec]
eng_s_throttle: Throttle [fraction]
eng_torque: Engine torque [Nm]

eng_total_emissions:

eng_s_volumetric_efficiency:

eng_s_pumping_torque:

Vector of total engine emissions [g]

Volumetric efficiency [number]

Pumping loop torque [Nm]

eng_s_gross_torque: Gross torque [Nm]

eng_s_combustion_torque: Combustion torque [Nm]

eng_therm_eff_gross: Gross thermal efficiency [fraction]

eng_s_friction_torque: Friction torque [Nm]
eng_s_exhaust_temp: Exhaust temperature [K]
eng_s_exhaust_gage_pressure: Exhaust gage pressure [Pa]
eng_s_exhaust_pressure: Exhaust absolute pressure [Pa]

eng_engine_emissions: Vector of engine out emissions, HC,CO,NOx,PM [g/hr] eng_vehicle_emissions: Vector of vehicle out emissions, HC,CO,NOx,PM [g/hr]

Mask: None

Table 2 presents typical values used for the constants in the engine model

| Table 2. Typical Constant Values in Engine Model | | |
|--|--------------------|--|
| Constant | Value | |
| eng_universal_gas_const: | 8314.3 [J/kmol/K] | |
| eng_std_pres: | 101.3 [Pa] | |
| eng_std_temp: | 298.17 [K] | |
| eng_mol_wt_air: | 28.96 [kg/kmol] | |
| eng_gas_const_air: | 287.096 [J/kg/K] | |
| eng_std_air_density: | 1.1834 [kg/m³] | |
| eng_mol_wt_exhaust: | 28.96 [kg/kmol] | |
| eng_gas_const_exhaust: | 287.096 [J/kg/K] | |
| eng_displacement: | 0.0018 [m³] | |
| eng_rated_speed: | 628.3185 [rad/s] | |
| eng_compression_ratio: | 8 | |
| eng_rated_bmep: | 1E6 [Pa] | |
| eng_rated_torque: | 1.131E4 [Nm] | |
| eng_rated_power: | 7.106E6 [watts] | |
| eng_rated_vol_eff: | 80 [%] | |
| eng_rated_air_vol_flow: | 0.072 [m³/s] | |
| eng_rated_air_mass_flow: | 0.0852 [kg/s] | |
| eng_ambient_pressure : | 101300 [Pa] | |
| eng_ambient_temperature: | 298.17 [K] | |
| eng_ambient_air_density: | 1.1834 [kg/m³] | |
| eng_inertia: | 0.1454 [kg-m^2] | |
| eng_off_torque_factor: | -0.1 [N-m / rad/s] | |
| eng_manifold_volume_ratio: | 0.0018 | |
| eng_manifold_volume: | 0.0018 [m³] | |

% Air system (1.1)

```
eng_throttle bypass ratio:
                            0.005
eng rated intake vacuum:
                            3000 [Pa]
eng rated pres ratio infl:
                            0.234
eng max air flow:
                            0.3642 [kg/s]
eng speed density weight:
                            1
eng af ratio speed:
                            [0.1667, 1]
eng af ratio Pi:
                            [0, 88000, 102000];
eng af ratio table:
                            [14.6, 14.6, 13]
                            [14.6, 14.6, 12.5]
eng liquid fuel fraction:
                            0.5
eng fuel evaporation time const:
                                   0.25 [sec]
eng vol eff speed:
                            [0.1667 0.3333 0.5000 0.6667 0.8333 1.0000]
eng vol eff Pi:
                            [20000
                                     100000] [Pa]
eng vol eff table:
                            [0.5000
                                    0.7000
                            0.5000
                                   0.7500
                            0.5000
                                   0.8000
                            0.5000
                                   0.8900
                            0.5000
                                   0.8700
                           0.5000 0.77001
eng nominal isfc:
                           6.67E-8 [kg/J]
eng fmep factor 0:
                           0.75
eng fmep factor 1:
                           0.15
eng fmep factor 2:
                           0.05
eng stoich af ratio:
                           14.6
eng exh temp af coef:
                           0
eng exh temp speed:
                           [0.1667
                                     1.0000 ] [rad/s]
eng exh temp Pi:
                           [20000
                                     1000001 [Pa]
eng exh temp table:
                           [673
                                     823]
                           [773
                                    1173] [deg K]
eng emissions speed:
                           [673
                                   823
                                           773
                                                   1173] [rad/s]
eng emissions Pi:
                           [40000
                                      50000
                                               60000
                                                         70000
                                                                   80000 ] [Pa]
eng_emissions HC table:
                           [0.0162
                                    0.0146
                                             0.0135 0.0124 0.0113]
                           [0.0151]
                                    0.0139
                                             0.0134 0.0121 0.01111
                           [0.0140
                                   0.0136
                                             0.0130 0.0120 0.0110]
                           [0.0130
                                    0.0133
                                             0.0128
                                                     0.0118
                                                              0.01071
                           [0.0124 0.0131
                                             0.0125
                                                     0.0112
                                                              0.0100
                           [kg/kg fuel]
eng emissions CO table:
                           [0.0802]
                                    0.0831
                                             0.0851
                                                     0.0837
                                                              0.0855]
                           [0.0840
                                    0.0860
                                             0.0890
                                                     0.0887
                                                              0.08981
                           [0.0861
                                    0.0894
                                             0.0935
                                                     0.0941
                                                              0.09331
                           [0.0892
                                    0.0921
                                             0.0969
                                                     0.0987
                                                              0.09871
                           [0.0909 0.0959
                                             0.0995
                                                     0.1013
                                                              0.1016
                                  [kg/kg fuel]
```

| eng_emissions_NOx_table: | 0.0] 0.0] 0.0] 0.0] |)279)384)482)569)632 /kg fi | 0.0 0.0 0.0 | 0465 0553 0635 0698 0755 | 0.0633 0.0673 | 0.0560 0.0583 0.0598 0.0608 0.0631 | 0.0517] 0.0539] 0.0558] 0.0571] 0.0593] |
|--------------------------|------------------------------|--|-------------------|--------------------------------------|----------------------------|--|---|
| eng_emissions_PM_table: | [0 [0 [0 [0 | 0 0 0 0 0 (kg fi | 0 0 0 0 | 0 0 0 0 | 0] 0] 0] 0] 0] | | |

| eng rated exhaust pressure: | 40000 [Pa] |
|---------------------------------------|----------------------------------|
| eng_exh_pres_scaling: | 0.5 |
| eng_rated_exhaust_temperature: | 1173 [K] |
| <pre>eng_rated_exhaust_density:</pre> | $0.4196 \text{ [kg/m}^3\text{]}$ |
| eng_muffler_pressure_factor: | 4.85E5 |
| eng_catalyst_eff_NOx: | 0.5 |
| eng_catalyst_eff_HC: | 0.5 |
| eng_catalyst_eff_CO: | 0.5 |
| eng_catalyst_eff_PM: | 0.5 |

Assumptions:

The following assumptions have been used for the quasi steady-state model:

May be used with any type of engine:

Spark ignited (SI) liquid fuel (gasoline)

Spark ignited (SI) gaseous fuel (natural gas)

Compression ignited (CI), typically called diesel engines

Gas turbine

Any other

- Uses steady-state maps for torque curves, fuel consumption and emissions.
- Any torque in the range of minimum to maximum is assumed to be available instantly.
- No transients of ANY KIND are included.
- Fastest model execution. Adequate in many vehicle models, including series hybrid applications where the engine is operating at steady or nearly steady conditions.

The following assumptions have been used in the Spark Ignited (SI) engine transient model:

- Liquid fueled (e.g. gasoline). Should not be used for gas fueled (e.g. natural gas) engines.
- Naturally aspirated (no turbocharging or supercharging). Most SI engines are naturally aspirated.
- Mean value torque model. Estimates average torque over engine cycle.
- Does not compute torque variation within a cycle.
- Assumes continuous flows. Does not consider manifold pressure waves or tuning. Tuning may be included through effect on volumetric efficiency.
- Three internal mode states associated with intake manifold emptying/filling manifold wall wetting by fuel catalyst bed temperature.
- Model does not consider any time delays associated with:

fueling decisions

fuel transport lag

torque production

- Engine is assumed to be fully warmed up at all times. Cold-start emissions are not calculated.
- Model does not simulate cranking or associated emissions.

3.0 ELECTRIC MACHINE LIBRARY

The electric machine library contains models of an AC induction motor as well as a permanent magnet generator. The AC induction motor model is connected to the wheel of an HEV either directly or via a motor wheel coupling. The generator is connected to an engine via an engine-generator coupling.

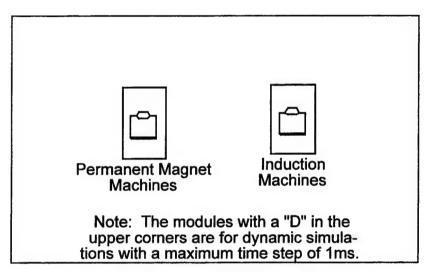


Figure 3. Machine Model Library

3.1 Steady-State Permanent Magnet Generator System Module with Fixed Efficiency Rectifier

| INPUTS | OUTPUTS |
|------------------------|--|
| DC Bus Voltage [V] | Rectifier Current [A] |
| DC Command Current [A] | [Output Torque [N·m], Machine Inertia [kg·m²]] |
| Engine Speed [rpm] | |

Constants as defined by the mask:

VAr: Rated Power of Generator [W]
Vr: Rated Line-Neutral Voltage of Generator [V]
nr: Rated Speed of Generator [rad/s]
poles: Number of Generator Poles []
Ib: Rated Line Current of Generator [A]
Zb: Base Impedance of Generator for Per Unit $[\Omega]$ wb: Base Speed of Generator for Per Unit [rad/s]

Per Unit Stator Resistance [] Rspu: Rmpu: Per Unit Iron Loss Resistance [] Laspu: Per Unit Stator q-axis Inductance [1] Ldspu: Per Unit Stator d-axis Inductance [] Llspu: Per Unit Stator Leakage Inductance [] Lmdpu: Per Unit Stator d-axis Magnetizing Inductance [] Idfpu: Per Unit PM "Field" Current [] recteff: Rectifier Efficiency [1 Inertia out: Machine Inertia [kg·m²] sample N: Number of Samples to Save to the MATLAB® Workspace sample T: Length of Time Between Each Sample

Auxiliary Calculations: None

Mask:

1. SS PM Generator System

SS PM Generator/Rectifier System|Gen
 Rtgs[P(hp),V(V),n(rpm)]:|Rtgs[poles,NLV(V),Core L(hp)]:|[Rs (ohms),Lqs,Lds,Lls
 (H)]:|Rectifier Efficiency:|Machine Inertia(kg*m*m):| [sample_N, sample_T]:

3. mvr=gencinit(@1,@2,@3); VAr = mvr(1,1); Vr = mvr(1,2); nr = @1(1,3); poles = @2(1,1); Rmpu = mvr(1,3); Ib = mvr(1,4); Zb = mvr(1,5); wb = mvr(1,6); Rspu = mvr(1,7); Lqspu=mvr(1,8); Ldspu = mvr(1,9); Llspu = mvr(1,10); Lmdpu = mvr(1,11); Idfpu=mvr(1,12); recteff = @4; Inertia_out = @5; sample_N = @6(1,1); sample T=@6(1,2);

This module simulates a permanent-magnet generator connected to a dc bus through a three-phase rectifier. The module mask contains the example values for a 50 hp, 230 V generator, which is user changeable. The generator is connected to the dc bus through a three-phase, fully controlled PWM voltage source (boost-type) rectifier as shown in Figure 4. Please refer to the following assumptions for other important simulation details.

Assumptions:

 This module will only be used in simulations with a minimum time step of 100 ms or larger.

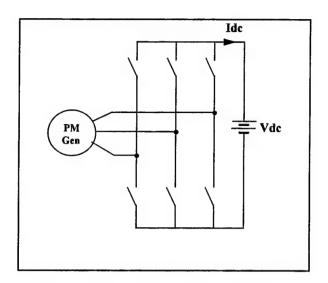


Figure 4. - Generator System Configuration. Ideal Switches Can Be IGBTS, BJTS or GTOS With Anti-Parallel Diodes

- The generator sign convention is that positive current is leaving the terminals of the machine. This current produces positive torque for positive speeds. For the module itself, a positive actual dc rectifier current (output #1) indicates the generating mode.
- Model does not include rectifier harmonic effects.
- The rectifier is assumed to have a fixed, user definable efficiency. The losses in the generator are modeled as stator copper and core loss (R_s and R_m, respectively in Figure 6).
- Within the module, a set of power values is computed at each time step in order to facilitate energy balance equations. The power values are as follows: the dc bus power, the mechanical power of the generator, the electrical power at the terminals of the machine, the rectifier loss power, and the total motor losses (core & copper losses). These values are *not* saved to the workspace automatically.
- The generator is controlled at all times with conventional "brushless dc" (also known as "field-oriented" or "vector") control. That is, the current in the generator is controlled to be in phase with the internal generator voltage (back emf).
- No provision is made for field weakening of the PM machine. If sufficient bus voltage is unavailable to maintain the control (this typically occurs when the speed is above the rated speed with rated bus voltage), then the generator is turned off (output power to the bus is zero) due to an "overspeed condition" for the given bus voltage.

- The generator current is limited to 1.5 times the value, which results in rated torque at rated speed. This also limits the direct axis flux in the machine.
- The user is cautioned that the machine parameters and rated values are not necessarily independent of one another. It is certainly possible to input values in the mask, which results in an uncontrollable machine or in control over a very small operating range.

Figure 5 shows the inputs and outputs of the steady-state generator model. Figure 6 depicts the steady-state synchronous d-q reference frame model used in the simulation. The electrical terminal voltage is calculated directly from this equivalent circuit using the command values of current and speed. The electrical and mechanical equations used in the simulation, and given by the equivalent circuit, are,

$$i_{qs}^{e} = i_{qm}^{e} + \frac{1}{R_{m}} (\omega_{r} L_{ds} i_{dm}^{e} - \omega_{r} L_{md} I_{df})$$

$$i_{ds}^{e} = i_{dm}^{e} - \frac{\omega_{r} L_{qs} i_{qm}^{e}}{R_{m}}$$

$$v_{qs}^{e} = -R_{s} i_{qs}^{e} + \omega_{r} L_{md} I_{df} - \omega_{r} L_{ds} i_{dm}^{e}$$

$$v_{ds}^{e} = -R_{s} i_{ds}^{e} + \omega_{r} L_{qs} i_{qm}^{e}$$

$$\tau = L_{md} I_{df} i_{qm}^{e}$$

where the superscript e denotes the synchronous reference frame, and I_{df} is the fictitious current that corresponds to the strength of the permanent magnet. This current is internally calculated from the no load speed and voltage. The iron loss resistor, R_m , is calculated from the rated core losses value provided by the user.

8

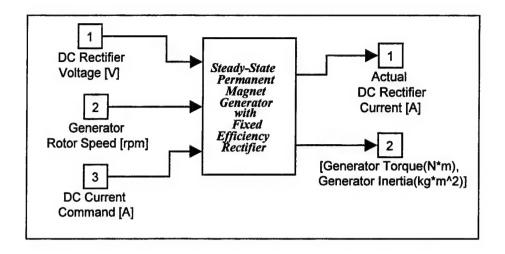


Figure 5 - Inputs and Outputs of PM Generator System

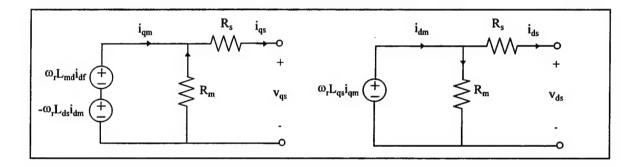


Figure 6 - Steady-State dq-Equivalent Circuits

The generator is controlled using conventional synchronous reference frame field orientation (i.e., "brushless dc" control) such that $i_{dm} = 0$.

When the mask is activated, the window in Figure 7 is displayed. The first input line asks the user to list the rated power, rated line, voltage, and rated speed of the generator. The next input line requests the values for the number of poles, the no-load voltage at rated speed, and the core losses at rated speed. The machine parameters of the per-phase stator resistance, per-phase q- and d-axis stator self inductances, and the per-phase leakage inductance are defined in the third line of the mask. The fixed efficiency of the rectifier is specified in line 4, and the system inertia is defined in the fifth input vector. Finally, the user can specify the

number of samples and the time step between each sample for use in "To Workspace" blocks within the module. The default values listed in Table 3 describe a 50 horsepower permanent-magnet synchronous generator with a fixed efficiency rectifier.

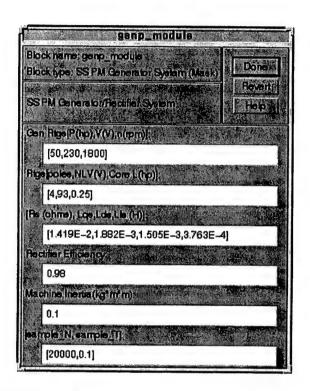


Figure 7 – Window Displayed When Mask Is Activated For The Permanent Magnet
Generator Module With Fixed Rectifier Efficiency

| Table 3. Machine Definitions and Values | | |
|--|------------|--|
| Machine Definitions | Values | |
| Rated Power | 50 hp | |
| Rated Voltage | 230 V | |
| Rated Speed | 1800 rpm | |
| Number of Poles | 4 | |
| No-Load Voltage @ Rated Speed | 93 V | |
| Core Losses @ Rated Voltage & Speed | 0.25 hp | |
| Per-Phase Stator Resistance, R _s | 1.419E-2 Ω | |
| Per-Phase Stator q-axis Inductance, L _a | 1.882E-3 H | |
| Per-Phase Stator d-axis Inductance, L _d | 1.505E-3 H | |
| Per-Phase Stator Leakage Inductance, Lis | 3.763E-4 H | |
| Rectifier Efficiency | 0.98 | |
| Machine Inertia | 0.1 kg⋅m² | |
| Number of Samples Saved to Workspace | 20000 | |
| Time Between each Saved Sample | 0.1 | |

3.2 Steady-State Permanent Magnet Generator System Module with Calculated Rectifier Losses

| INPUTS | OUTPUTS |
|------------------------|-------------------------|
| DC Bus Voltage [V] | Rectifier Current [A] |
| DC Command Current [A] | Output Torque [N·m] |
| Engine Speed [rpm] | Machine Inertia [kg·m²] |

Constants as defined by the mask:

VAr: Rated Power of Generator [W]

Vr: Rated Line-Neutral Voltage of Generator [V]

nr: Rated Speed of Generator [rad/s] poles: Number of Generator Poles []

Ib: Rated Line Current of Generator [A]

Zb: Base Impedance of Generator for Per Unit $[\Omega]$ wb: Base Speed of Generator for Per Unit [rad/s]

Rspu: Per Unit Stator Resistance []
Rmpu: Per Unit Iron Loss Resistance []
Lqspu: Per Unit Stator q-axis Inductance []
Ldspu: Per Unit Stator d-axis Inductance []
Llspu: Per Unit Stator Leakage Inductance []

Lmdpu: Per Unit Stator d-axis Magnetizing Inductance []

Idfpu: Per Unit PM "Field" Current []

fc: PWM Switching Frequency of the Rectifier [Hz]

EQD: Total Switching Energy Loss per Amp of the IGBT-Diode Combination [J/A]

Vnom: Voltage at which EQD is specified [V]

rQ: On State IGBT Resistance $[\Omega]$ rD: On State Diode Resistance $[\Omega]$

VQ: Forward Voltage Drop of the IGBT [V]
VD: Forward Voltage Drop of the Diode [V]

PWM: Determines if Sinusoidal(1) or Space Vector (0) PWM is used.[]

Inertia out: Machine Inertia [kg.m²]

sample_N: Number of Samples to Save to the MATLAB Workspace []

sample_T: Length of Time Between Each Sample []

Auxiliary Calculations: None

Mask:

- 1. SS PM Generator System
- 2. SS PM Generator / Rectifier System|Gen Ratings[P(hp),V(V),n(rpm),J(kgm²)]|
 Rtgs[poles,NLV(V),Core L(hp)]|[Rs(ohms),Lqs(H),Lds(H),Lls(H)]| Rect

- [rQ,rD(ohms),VQ,VD(V)]|[PWM,f(Hz),EQD(J/A),Vnom(V)]| [sample_N, sample_T]:
- 3. mvr=gencinit(@1,@2,@3);VAr=mvr(1,1);Vr=mvr(1,2);nr=@1(1,3);poles=@2(1,1);
 Rmpu=mvr(1,3);Ib=mvr(1,4);Zb=mvr(1,5);wb=mvr(1,6);Rspu=mvr(1,7);
 Lqspu=mvr(1,8);Ldspu=mvr(1,9);Llspu=mvr(1,10);Lmdpu=mvr(1,11);
 Idfpu=mvr(1,12);rQ=@4(1,1);rD=@4(1,2);VQ=@4(1,3);VD=@4(1,4);PWM=@5(1,1);
 fc=@5(1,2);Inertia_out=@1(1,4);EQD=@5(1,3);Vnom=@5(1,4);sample_N=@6(1,1);
 sample_T=@6(1,2);

This module simulates a permanent-magnet generator connected to a dc bus through a three-phase rectifier. The module mask contains example values for a 50 hp, 230V generator, which are user changeable. The generator is connected to the dc bus through a three-phase fully controlled PWM voltage source (boost-type) rectifier as shown in Figure 8. The rectifier uses either the sinusoidal PWM method [1] or the space vector PWM method [2].

Assumptions:

- This module will only be used in simulations with a minimum time step of 100 ms or larger.
- The generator sign convention is such that positive current leaves the terminals of the machine. This current produces positive torque for positive speeds. A positive dc rectifier current (output #1) indicates the generating mode.

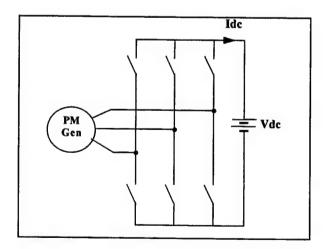


Figure 8 - Generator System Configuration:
Ideal Switches Can Be IGBTs, BJTs or GTOs With Antiparallel Diodes

- Within the module, a set of power values is computed at each time step in order to facilitate energy balance equations. The power values are as follows: the dc bus power, the mechanical power of the generator, the electrical power at the terminals of the machine, the rectifier loss power, and the total motor losses (core & copper losses). These values are not saved to the workspace automatically.
- Loss calculations for the Alt-Rev space vector PWM method [2] are based on the third harmonic PWM method since both control methods result in similar steady-state operation.
- Phase currents and phase voltages of the generator are assumed to be purely sinusoidal for rectifier loss calculations. This assumption is justifiable if the PWM frequency is reasonably high.
- The machine model does not include rectifier harmonic effects.
- The losses in the generator are modeled as stator copper loss (R_s in Figure 10) and core loss (R_m in Figure 10).
- The generator is controlled at all times with conventional "brushless dc" (also known as "field-oriented" or "vector") control. That is, the current in the generator is controlled to be in phase with the internal generator voltage (back emf).
- No provision is made for field weakening of the PM machine. If sufficient bus voltage is unavailable to maintain the control (this typically occurs when the speed is above the rated speed with rated bus voltage), the generator is turned off (output power to the bus is zero) due to an "overspeed condition" for the given bus voltage.
- The generator current is limited to 1.5 times the value, which results in rated torque at rated speed. This also limits the direct axis flux in the machine.
- The user is cautioned that the machine parameters and rated values are not necessarily independent of one another. It is certainly possible to input values in the mask, which result in an uncontrollable machine, or in control over a very small operating range.

Figure 10 shows the inputs and outputs of the steady-state permanent magnet generator model with calculated rectifier losses. Figure 11 depicts the steady-state synchronous d-q reference frame machine model used in the simulation. The electrical terminal voltage is calculated directly from this equivalent circuit using the command values of current and speed. The electrical and mechanical equations used in the simulation, and given by the equivalent circuit, are,

$$\begin{split} i_{qs}^{e} &= i_{qm}^{e} + \frac{1}{R_{m}} \left(\omega_{r} L_{ds} i_{dm}^{e} - \omega_{r} L_{md} I_{df} \right) \\ i_{ds}^{e} &= i_{dm}^{e} - \frac{\omega_{r} L_{qs} i_{qm}^{e}}{R_{m}} \\ v_{qs}^{e} &= -R_{s} i_{qs}^{e} + \omega_{r} L_{md} I_{df} - \omega_{r} L_{ds} i_{dm}^{e} \\ v_{ds}^{e} &= -R_{s} i_{ds}^{e} + \omega_{r} L_{qs} i_{qm}^{e} \\ \tau &= L_{md} I_{df} i_{qm}^{e} \end{split}$$

where the superscript e denotes the synchronous reference frame and I_{df} is the fictitious current which corresponds to the strength of the permanent magnet. This current is internally calculated from the no load speed and voltage. The iron loss resistor, R_m , is calculated from the rated core losses value provided by the user.

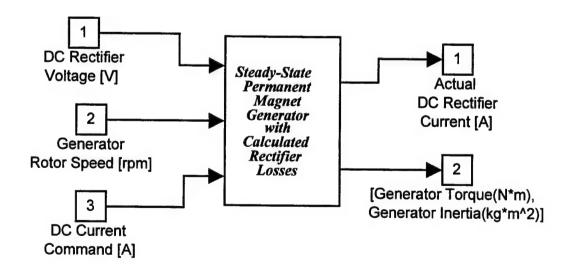


Figure 9. Steady-State Permanent Magnet Generator with Calculated Rectifier Losses

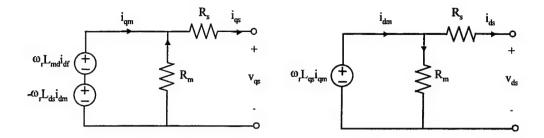


Figure 10 - Inputs and Outputs of PM Generator System with Calculated Rectifier Losses.

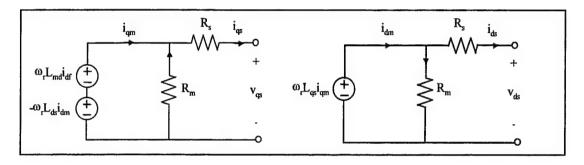


Figure 11 - Steady-State dq-Equivalent Circuits

The generator is controlled using conventional synchronous reference frame field orientation (i.e., "brushless dc" control) such that $i_{dm} = 0$.

The following are the machine variables used for the device loss calculations within the rectifier:

$$I_{p} = \sqrt{2} Ib \sqrt{2 \left(Iqspu^{2} + Idspu^{2} \right)}$$

$$V_{p} = \sqrt{2} Vr \sqrt{2 \left(Vqspu^{2} + Vdspu^{2} \right)}$$

$$\phi = \tan^{-1} \left(\frac{Vdspu}{Vqspu} \right) - \tan^{-1} \left(\frac{Idspu}{Iqspu} \right)$$

$$M = \frac{2V_{p}}{Vdc}$$

where

 V_p Peak machine output phase voltage I_p Peak output current of the machine M Modulation index

φ Phase lag of the machine line current
 Vdc Voltage of the DC bus.
 Iqspu RMS q-axis machine output current
 Idspu RMS d-axis machine output current
 Vqspu RMS q-axis machine output phase voltage
 Vdspu RMS d-axis machine output phase voltage

Table 4 shows the equations governing the rectifier device currents.

| Table 4 | Table 4. Equations Governing Rectifier Device Currents | | | | | | | |
|-------------------------------------|--|---|--|--|--|--|--|--|
| Device Currents | Sinusoidal PWM | Space Vector PWM | | | | | | |
| $\overline{I_Q}$ | $I_{p}\left(\frac{1}{2\pi} + \frac{M\cos\phi}{8}\right)$ | $I_{p}\left(\frac{1}{2\pi} + \frac{\sqrt{3}M\cos\phi}{12}\right)$ | | | | | | |
| $\overline{I_D}$ | $I_{p}\left(\frac{1}{2\pi}-\frac{M\cos\phi}{8}\right)$ | $I_{p}\left(\frac{1}{2\pi}-\frac{\sqrt{3}M\cos\phi}{12}\right)$ | | | | | | |
| $\left I_{Q}\right _{\mathit{RMS}}$ | $I_{p}\sqrt{\frac{1}{8} + \frac{M\cos\phi}{3\pi}}$ | $I_{p}\sqrt{\frac{1}{8}+M\frac{30\cos\phi-\cos3\phi}{45\sqrt{3}\pi}}$ | | | | | | |
| $\left I_{D} ight _{\mathit{RMS}}$ | $I_{p}\sqrt{\frac{1}{8}-\frac{M\cos\phi}{3\pi}}$ | $I_{p}\sqrt{\frac{1}{8}-M\frac{30\cos\phi-\cos3\phi}{45\sqrt{3}\pi}}$ | | | | | | |

where $\overline{I_{\varrho}}$ Average current through the IGBT $\overline{I_{D}}$ Average current through the diode $\left|I_{\varrho}\right|_{\scriptscriptstyle RMS}$ RMS current through the IGBT $\left|I_{\scriptscriptstyle D}\right|_{\scriptscriptstyle RMS}$ RMS current through the diode

The rectifier losses are then calculated using the following equations:

Conduction losses:

$$\begin{split} P_{Q(cond)} &= \overline{I_{Q}} \cdot VQ + \left| I_{Q} \right|_{RMS}^{2} \cdot rQ \\ P_{D(cond)} &= \overline{I_{D}} \cdot VD + \left| I_{D} \right|_{RMS}^{2} \cdot rD \end{split}$$

where

 $P_{Q(cond)}$

Conduction power loss in the IGBT

P D(cond. Conduction power loss in the diode

Switching losses:

$$\begin{split} P_{Q(sw)} &= \frac{f \cdot E_Q \cdot I_p}{\pi} \bigg(\frac{Vdc}{Vnom} \bigg) \\ P_{D(sw)} &= \frac{f \cdot E_D \cdot I_p}{\pi} \bigg(\frac{Vdc}{Vnom} \bigg) \\ P_{TOT(sw)} &= P_{Q(sw)} + P_{D(sw)} = \frac{f \cdot EQD \cdot I_p}{\pi} \bigg(\frac{Vdc}{Vnom} \bigg) \end{split}$$

where

 $P_{Q(sw)}$

Switching power loss in the IGBT

 $P_{D(sw)}$

Switching power loss in the diode

 $P_{TOT(sw)}$

Total switching power loss

Vdc

Voltage of the DC bus.

 E_{o}

Switching energy loss per Amp of the IGBT

 E_D

Switching energy loss per Amp of the diode

EQD

 $E_Q + E_D$

The total rectifier loss power(P_{loss}) is six times the sum of the conduction and switching losses of the IGBT and the diode.

$$P_{loss} = 6\left(P_{Q(sw)} + P_{D(sw)} + P_{Q(cond)} + P_{D(cond)}\right)$$

IGBT Selection Guide:

Table 5 shows the IGBT modules that contain the antiparallel diodes.

| | Table 5. IGBT Modules that Contain the Antiparallel Diodes | | | | | | | | | |
|--------------|--|------------------|---------------------|-------------------|---------------------|---------------------|------------------------------|-----------------------|-----------------------|--|
| IGBT Module# | Frequency | V _{CES} | l _c @ | P _{DMAX} | VQ _{MAX} @ | VD _{MAX} @ | EQD (@V _{nom}) | rQ @ | rD@ | |
| | Range | (V) | T _J =25℃ | (VV) | T _J =25℃ | T _J =25℃ | @T _J =125℃ | T _J =125°C | T _J =125°C | |
| | (kHz) | | (A) | | (V) | (V) | (mJ/A) | (mΩ) | $(m\Omega)$ | |
| IRGDDN300M06 | 3-10 | 600 | 400 | 1563 | 2.0 | 2.0 | 0.2 @ V _{rom} =300V | - | _ | |
| IRGDDN400M06 | 3-10 | 600 | 600 | 1984 | 2.0 | 2.0 | 0.2 @ V _{rom} =300V | _ : | _ | |
| IRGDDN600M06 | 3-10 | 600 | 800 | 2604 | 2.7 | 2.0 | 0.2 @ V _{mm} =300V | _ | _ | |
| IRGDDN200M12 | 3-10 | 1200 | 420 | 1800 | 2.7 | 3.4 | 0.6 @ V _{rom} =600V | 2.00 | 5.50 | |
| IRGDDN300M12 | 3-10 | 1200 | 560 | 2400 | 2.7 | 3.4 | 0.6 @ V _{mm} =600V | 2.50 | 4.00 | |
| IRGDDN400M12 | 3-10 | 1200 | 400 | 2770 | 2.7 | 3.4 | 0.6 @ V _{nom} =600V | _ | - | |
| IRGDDN300K06 | 10-30 | 600 | 340 | 1563 | 2.7 | 2.0 | 0.15@ V _{mm} =300V | _ | _ | |
| IRGDDN400K06 | 10-30 | 600 | 520 | 1984 | 2.7 | 2.0 | 0.15@ V _{mm} =300V | _ | | |
| IRGDDN600K06 | 10-30 | 600 | 680 | 2604 | 2.7 | 2.0 | 0.15@ V _{nom} =300V | - | - | |

| where | $V_{C\!E\!S}$ | Maximum Continuous Collector to Emitter Voltage |
|-------|-------------------|---|
| | I_c | Maximum Continuous Collector Current |
| | P_{DMAX} | Maximum Power dissipation |
| | VQ_{max} | Maximum Collector to Emitter ON Voltage |
| | VD_{MAX} | Maximum Forward Voltage Drop of the Diode |
| | EQD | Total Switching Energy Loss per Amp of the IGBT-Diode Combination |
| | V_{nom} | Collector Voltage at which EQD is specified |
| | rQ | On State IGBT Resistance |
| | rD | On State Diode Resistance |
| | T_{J} | Device Junction Temperature |

The value of on-state resistance of the IGBT and diode is found by calculating the inverse of the slope of the device current versus device voltage curve (during conduction).

When the mask is activated, the window in Figure 11 is displayed. The first input line asks the user to list the rated power, rated line voltage, and rated speed of the generator as well as the system inertia. The next input line requests the values for the number of poles, the no load voltage at rated speed, and the core losses at rated speed. The machine parameters of per-phase stator resistance, per-phase q- and d-axis stator self inductances, and the per-phase leakage inductance are defined in the third line of the mask. The rectifier is described by the next two input vectors of the mask. In the first vector, the on-state resistance of the switching

devices(rQ) and the diodes(rD) and their respective forward voltage drops are defined. The second input vector for the rectifier specifies the PWM method (1 for Sinusoidal/0 for Space Vector), the switching frequency, the total switching energy loss per amp of the switching device/diode combination, and the collector voltage at which this switching loss occurs.

Finally, the user can specify the number of samples and the time step between each sample for use in "To Workspace" blocks within the module. The default values, which describe a 50 horsepower permanent-magnet synchronous generator with a three-phase IGBT boost rectifier, are listed in Table 6 on the following page.

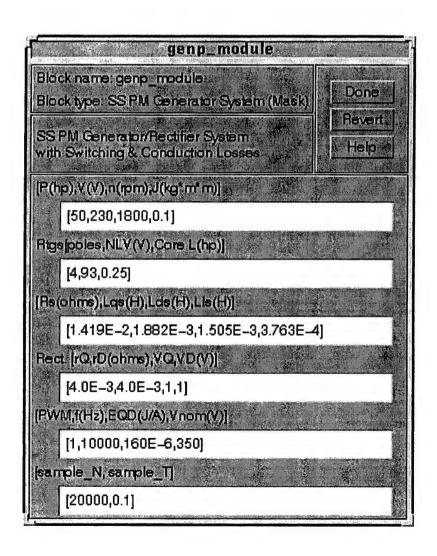


Figure 12. Window Displayed When Mask Is Activated For The Permanent Magnet
Generator Module With Calculated Rectifier Losses

| Table 6. Default Values | | | | |
|--|------------|--|--|--|
| Machine and Rectifier Definitions | Values | | | |
| Rated Power, P | 50 hp | | | |
| Rated Voltage, V | 230 V | | | |
| Rated Speed, n | 1800 rpm | | | |
| Number of Poles, poles | 4 | | | |
| No-Load Voltage @ Rated Speed, NLV | 93 V | | | |
| Core Losses @ Rated Voltage & Speed, Core L | 0.25 hp | | | |
| Per-Phase Stator Resistance, R _s | 1.419E-2 Ω | | | |
| Per-Phase Stator q-axis Inductance, L _{os} | 1.882E-3 H | | | |
| Per-Phase Stator d-axis Inductance, L _{ds} | 1.505E-3 H | | | |
| Per-Phase Stator Leakage Inductance, Lis | 3.763E-4 H | | | |
| Machine Inertia, J | 0.1 kg·m² | | | |
| PWM Switching Frequency of the Rectifier, f _c | 10000 Hz | | | |
| Total Switching Energy Loss per Amp of the IGBT-Diode Combination, EQD | 160 □J/A | | | |
| Voltage at which EQD is specified, Vnom | 350 V | | | |
| On State IGBT Resistance, rQ | 4.0E-3 □ | | | |
| On State Diode Resistance, rD | 4.0E-3 □ | | | |
| Forward Voltage Drop of the IGBT, VQ | 1 V | | | |
| Forward Voltage Drop of the Diode, VD | 1 V | | | |
| Type of PWM used [Sinusoidal(1) or Space Vector(0)] | 1 | | | |
| Number of Samples to Save to the MATLAB Workspace, sample_N | 20000 | | | |
| Length of Time Between Each Sample, sample_T | 0.1 | | | |

References:

- [1] Ken Berringer, Jeff Marvin and Philippe Perruchoud, "Semiconductor Power Losses in AC Inverters," Conference Record-IAS Annual Meeting (IEEE Industry Applications Society), pp. 882-886, 1995.
- [2] Philippe J.P. Perruchoud and Peter J. Pinewski, "Power Losses for Space Vector Modulation Techniques," *IEEE Workshop on Power Electronics in Transportation*, pp. 167-173, Oct. 1996.

3.3 Steady-State Induction Generator System with Fixed Efficiency Rectifier

| INPUTS | OUTPUTS | | | |
|------------------------|--|--|--|--|
| DC Bus Voltage [V] | Rectifier Current [A] | | | |
| DC Command Current [A] | [Output Torque [N·m], Machine Inertia [kg·m²]] | | | |
| Engine Speed [rpm] | | | | |

Constants as defined by the mask:

VAr: Rated Power of Motor [W]

Vr: Rated Line-Neutral Voltage of Motor [V] wb: Base Speed of Motor for Per Unit [rad/s]

wmr: Rated Speed of Motor [rad/s]
poles: Number of Motor Poles []

corel: Core Losses of Motor @ Rated Voltage & Speed [W]
SLL: Stray Load Losses of Motor @ Rated Voltage & Speed [W]

Ib: Base Line Current of Motor [A]

Zb: Base Impedance of Motor for Per Unit $[\Omega]$

Rspu: Per Unit Stator Resistance []
Rrpu: Per Unit Rotor Resistance []
Lspu: Per Unit Stator Inductance []
Lrpu: Per Unit Rotor Inductance []

Lmpu: Per Unit Magnetizing Inductance []

fluxr: Per Unit Rotor Flux @ Rated Conditions []

recteff: Inverter Efficiency []
Inertia_out: Machine Inertia [kg·m²]

sample_N: Number of Samples to Save to the MATLAB® Workspace

sample T: Length of Time Between Each Sample

Auxiliary Calculations: None

Mask:

- 1. SS Induc. Generator Sys.
- SS Induction Generator/Rectifier System|Gen Rtgs[P(hp),V(V),f(Hz)]:|Rtgs[n(rpm),CL(hp), SLL(hp)]:|[Rs,Rr (ohms), Lls,Llr,Lm (H)]:|Rectifier Efficiency:|Machine Inertia(kg*m*m):|[sample_N, sample_T]:
- 3. mvr=genIinit(@1,@2,@3);VAr=mvr(1,1);Vr=mvr(1,2);wb=mvr(1,3);wmr=mvr(1,4); poles=mvr(1,5);corel=mvr(1,6);SLL=mvr(1,15);Ib=mvr(1,7);Zb=mvr(1,8);Rspu=mvr(1,9);Rrpu=mvr(1,10);Lmpu=mvr(1,11);Lspu=mvr(1,12);Lrpu=mvr(1,13);fluxr=mvr(1,14); recteff=@4; Inertia out=@5;sample N=@6(1,1);sample T=@6(1,2);')

This module simulates a three-phase squirrel cage induction generator and a three phase boost-type or voltage-sourced (IGBT) rectifier supply. The module mask contains the example values for a 50 hp, 230 V generator, which are user changeable. The core losses and stray load losses are included in the model and can be set in the module mask as well. Please refer to the assumptions below for other important simulation details.

Assumptions:

- This module will only be used in simulations with a minimum time step of 100 ms or larger.
- The generator is controlled at all times with conventional "field-oriented" or "vector" control. That is, the slip frequency and current in generator are regulated to provide dynamic control of the generator torque.
- The flux in the generator is limited to its rated value (\approx rated V/f).
- The torque is limited to the peak or pullout torque for rated flux. The current is therefore limited to the current at peak torque.
- When the bus voltage is not sufficient to provide rated flux, field weakening is enabled which maintains maximum bus voltage on the generator. In this mode, the flux is inversely proportional to the generator speed, and the peak torque is inversely proportional to the square of the generator speed.
- At low speeds, the rotor copper losses significantly affect the performance of the induction generator. When in the *motoring* mode, the actual DC current can overshoot the requested value substantially. To protect the HEV system and eliminate large overshoot in the *motoring mode*, the q-axis stator current is limited to 1.5 pu in addition to the previously discussed limits.
- The copper losses are modeled by R_s and R_r' in
- Figure 13. The core losses are calculated to be proportional to the generator flux. The stray load losses are proportional to the generator torque.
- The generator sign convention is that positive current is leaving the terminals of the machine. This current produces positive torque for positive speeds. For the module itself, a positive actual dc rectifier current (output #1) indicates the generating mode.
- Within the module, a set of power values is computed at each time step in order to facilitate energy balance equations. The power values are as follows: the dc bus power, the mechanical power of the generator, the electrical power at the terminals of the machine, the rectifier loss power, and the total motor losses (core, stray load, and copper losses). These values are *not* saved to the workspace automatically.

- The model does not include rectifier harmonic effects.
- The rectifier is assumed to have a fixed, user-definable efficiency.

Figure 13 shows the inputs and outputs of the steady-state induction generator model. Figure 14 depicts the per-phase equivalent circuit model of the induction machine, and defines the generator parameters. Figure 15 shows the induction generator model after the transformation to the synchronous d-q reference frame. The electrical terminal voltages and currents are calculated directly from this equivalent circuit and the mechanical equations using the command values of torque and speed. The synchronous reference frame electrical and mechanical equations used in the simulation are,

$$v_{qs}^{e} = -R_{s}i_{qs}^{e} + \omega \lambda_{ds}^{e}$$

$$v_{ds}^{e} = -R_{s}i_{ds}^{e} - \omega \lambda_{qs}^{e}$$

$$0 = R_{r}i_{qr}^{e} + (\omega - \omega_{r})\lambda_{dr}^{e}$$

$$0 = R_{r}i_{dr}^{e} - (\omega - \omega_{r})\lambda_{qr}^{e}$$

$$\lambda_{qs}^{e} = -(L_{m} + L_{ls})i_{qs}^{e} + L_{m}i_{qr}^{e}$$

$$\lambda_{ds}^{e} = -(L_{m} + L_{lr})i_{dr}^{e} + L_{m}i_{dr}^{e}$$

$$\lambda_{qr}^{e} = (L_{m} + L_{lr})i_{qr}^{e} - L_{m}i_{qs}^{e}$$

$$\lambda_{dr}^{e} = (L_{m} + L_{lr})i_{dr}^{e} - L_{m}i_{ds}^{e}$$

$$\tau = L_{m}(i_{ds}^{e}i_{qr}^{e} - i_{as}^{e}i_{dr}^{e})$$

where the *e* superscript denotes the synchronous reference frame.

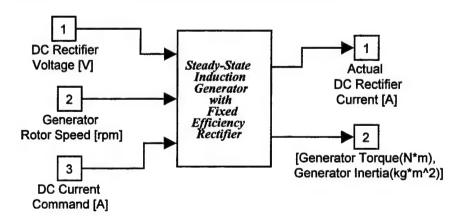


Figure 13. Inputs And Outputs Of The Steady-State Induction Generator Model With A Fixed Efficiency Rectifier

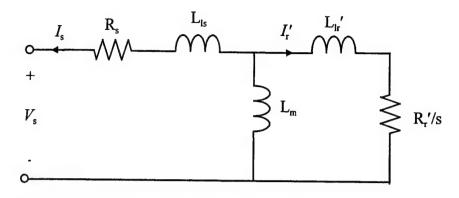


Figure 14. Induction Machine Per Phase Equivalent Circuit

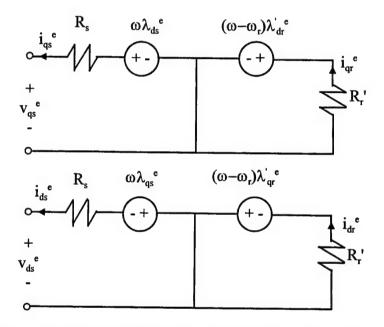


Figure 15. Steady-State dq Equivalent Circuit Of An Induction Generator

The generator is controlled using conventional rotor flux field orientation ("brushless dc" control) such that in the synchronous reference frame, $\lambda_{qr}^{\ e} = 0$.

When the mask is activated, the window in Figure 15 is displayed. The first input line asks the user to list the rated power, rated line voltage and rated frequency of the induction generator. The next input line requests the values for the rated speed, and the rated core and stray load losses that occur under rated operating conditions. The per-phase machine parameters of stator and rotor resistance, stator and rotor leakage inductance, and the

magnetizing inductance are defined in the third line of the mask. The fixed efficiency of the rectifier is specified in line 4, and the system inertia is defined in the fifth input vector. Finally, the user can specify the number of samples and the time step between each sample for use in "To Workspace" blocks within the module. The default values listed in Table 7 below describe a 50 horsepower induction generator with a fixed efficiency rectifier.

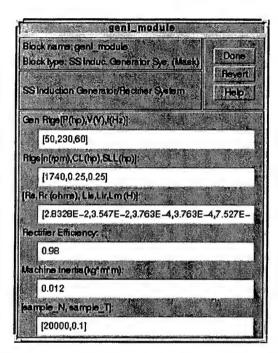


Figure 16. Window Displayed When Mask Is Activated For The Induction Generator

Module With Fixed Rectifier Efficiency

| Table 7. Default Values | | | | | | |
|--|---------------|--|--|--|--|--|
| Machine Definitions | Values | | | | | |
| Rated Power | 50 hp | | | | | |
| Rated Voltage | 230 V | | | | | |
| Rated Frequency | 60 Hz | | | | | |
| Rated Speed | 1740 rpm | | | | | |
| Core Losses @ Rated Voltage & Speed | 0.25 hp | | | | | |
| Stray Load Losses @ Rated Voltage & Speed | 0.25 hp | | | | | |
| Per-Phase Stator Resistance, R _s | 2.8328E-2 Ω | | | | | |
| Per-Phase Rotor Resistance, R _r | 3.547E-2 Ω | | | | | |
| Per-Phase Stator Leakage Inductance, L _{ls} | 3.763E-4 H | | | | | |
| Per-Phase Rotor Leakage Inductance, L _{Ir} | 3.763E-4 H | | | | | |
| Per-Phase Magnetizing Inductance, L _m | 7.527E-3 H | | | | | |
| Rectifier Efficiency | 0.98 | | | | | |
| Motor Inertia | 0.012 [kg·m²] | | | | | |
| Number of Samples Saved to Workspace | 20000 | | | | | |
| Time Between each Saved Sample | 0.1 | | | | | |

3.4 Steady-State Induction Machine - Traction Motor System with Fixed **Efficiency Inverter**

| INPUTS | OUTPUTS |
|---------------------------------|---|
| DC Bus Voltage [V] | Inverter Current [A] |
| Rotor Speed [rpm] | [Output Torque [N·m], Machine Inertia [kg·m²] |
| Per Unit Input Torque Command[] | |

Constants as defined by the mask:

VAr:

Rated Power of Motor [W]

Vr:

Rated Line-Neutral Voltage of Motor [V]

wb:

Base Speed of Motor for Per Unit [rad/s]

wmr:

Rated Speed of Motor [rad/s]

poles:

Number of Motor Poles [1]

corel:

Core Losses of Motor @ Rated Voltage & Speed [W]

SLL:

Stray Load Losses of Motor @ Rated Voltage & Speed [W]

Ib:

Base Line Current of Motor [A]

Zb:

Base Impedance of Motor for Per Unit $[\Omega]$

Rspu:

Per Unit Stator Resistance []

Rrpu:

Per Unit Rotor Resistance []

Lspu: Lrpu:

Per Unit Stator Inductance [] Per Unit Rotor Inductance [1]

Lmpu:

Per Unit Magnetizing Inductance []

fluxr:

Per Unit Rotor Flux @ Rated Conditions []

inveff: Inertia out: Inverter Efficiency [] Machine Inertia [kg·m²]

sample N:

Number of Samples to Save to the MATLAB® Workspace

sample T:

Length of Time Between Each Sample

Auxiliary Calculations: None

Mask:

- 1. SS Induction Motor Sys
- 2. SS Induction Motor/Inverter System|Rated [P(hp),V(V),f(Hz)]:|Rated [n(rpm),CL(hp),SLL(hp)]:|[Rs,Rr (ohms), Lls,Llr,Lm (H)]:|Inverter Efficiency:|Machine Inertia(kg*m*m):|[sample N,sample T]:
- 3. mvr=motIinit(@1,@2,@3); VAr=mvr(1,1); Vr=mvr(1,2); wb=mvr(1,3); wmr=mvr(1,4); poles=mvr(1,5); corel=mvr(1,6); SLL=mvr(1,15); Ib=mvr(1,7); Zb=mvr(1,8); Rspu=mvr(1,9); Rrpu=mvr(1,10); Lspu=mvr(1,12); Lrpu=mvr(1,13); Lmpu=mvr(1,11); fluxr=mvr(1,14); inveff=@4; Inertia_out=@5; sample_N=@6(1,1); sample_T=@6(1,2);

This module simulates a three-phase, squirrel-cage induction motor and a three-phase, boost-type or voltage-sourced (IGBT) inverter supply. The module mask contains the example values for a 50 hp, 230 V motor, which are user changeable. The core losses and stray load losses are included in the model and can be set in the module mask as well. Please refer to the assumptions below for other important simulation details.

Assumptions:

- This module will only be used in simulations with a minimum time step of 100 ms or larger.
- The motor is controlled at all times with conventional "field-oriented" or "vector" control. That is, the slip frequency and current in motor are regulated to provide dynamic control of the motor torque.
- The flux in the motor is limited to its rated value (\approx rated V/f).
- The torque is limited to the peak or pullout torque for rated flux. The current is therefore limited to the current at peak torque.
- When the bus voltage is not sufficient to provide rated flux, field weakening is enabled, which maintains maximum bus voltage on the motor. In this mode, the flux is inversely proportional to the motor speed, and the peak torque is inversely proportional to the square of the motor speed.
- The copper losses are modeled by R_s and R_r' in Figure 17. The core losses are calculated to be proportional to the motor flux. The stray load losses are proportional to the motor torque.
- The sign convention for the motor module is that positive current enters the terminals of the machine. Positive current produces positive torque, i.e., positive dc inverter current (output #1) indicates the module is motoring.
- Within the module, a set of power values is computed at each time step in order to facilitate energy balance equations. The power values are as follows: the dc bus power, the mechanical power of the motor, the electrical power at the terminals of the machine, the inverter loss power, and the total motor losses (core, stray load, and copper losses). These values are *not* saved to the workspace automatically.

- The model does not include inverter harmonic effects.
- The inverter is assumed to have a fixed, user-definable efficiency.

Figure 17 shows the inputs and outputs of the steady-state induction motor model. Figure 18 depicts the per-phase equivalent circuit model of the induction machine and defines the motor parameters. Figure 19 shows the induction motor model after the transformation to the synchronous d-q reference frame. The electrical terminal voltages and currents are calculated directly from this equivalent circuit and the mechanical equations using the command values of torque and speed. The synchronous reference frame electrical and mechanical equations used in the simulation are,

$$\begin{aligned} v_{qs}^{e} &= R_{s}i_{qs}^{e} + \omega \lambda_{ds}^{e} \\ v_{ds}^{e} &= R_{s}i_{ds}^{e} - \omega \lambda_{qs}^{e} \\ 0 &= R_{r}i_{qr}^{e} + (\omega - \omega_{r}) \lambda_{dr}^{e} \\ 0 &= R_{r}i_{dr}^{e} - (\omega - \omega_{r}) \lambda_{qr}^{e} \\ \lambda_{qs}^{e} &= (L_{m} + L_{ls})i_{qs}^{e} + L_{m}i_{qr}^{e} \\ \lambda_{ds}^{e} &= (L_{m} + L_{lr})i_{ds}^{e} + L_{m}i_{dr}^{e} \\ \lambda_{qr}^{e} &= (L_{m} + L_{lr})i_{dr}^{e} + L_{m}i_{qs}^{e} \\ \lambda_{dr}^{e} &= (L_{m} + L_{lr})i_{dr}^{e} + L_{m}i_{ds}^{e} \\ \tau &= L_{m}(i_{qs}^{e}i_{dr}^{e} - i_{ds}^{e}i_{qr}^{e}) \end{aligned}$$

where the e superscript denotes the synchronous reference frame.

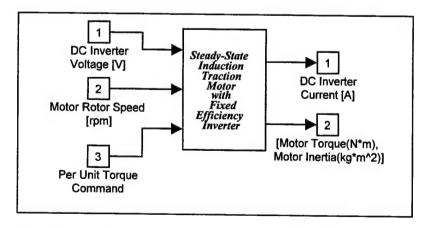


Figure 17. Inputs And Outputs Of Induction Motor System
With Fixed Efficiency Inverter

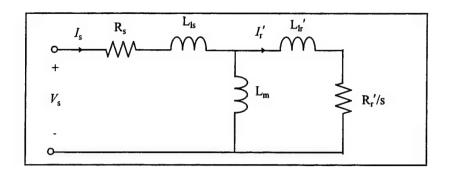


Figure 18. Induction Machine Per Phase Equivalent Circuit

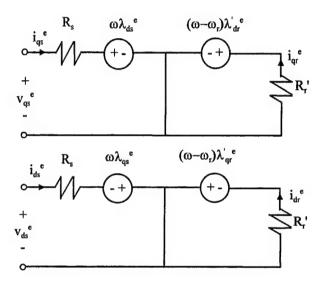


Figure 19. Steady-State dq Equivalent Circuit Of An Induction Motor

The motor is controlled using conventional rotor flux field orientation ("brushless dc" control) such that in the synchronous reference frame, $\lambda_{qr}^{\ e} = 0$.

When the mask is activated, the window in Figure 19 is displayed. The first input line asks the user to list the rated power, rated line voltage and rated frequency of the induction motor. The next input line requests the values for the rated speed, and the rated core and stray load losses that occur under rated operating conditions. The per-phase machine parameters of stator and rotor resistance, stator and rotor leakage inductance, and the magnetizing inductance are defined in the third line of the mask. The fixed efficiency of the inverter is specified in line 4 and the system inertia is defined in the fifth input vector. Finally, the user

can specify the number of samples and the time step between each sample for use in "To Workspace" blocks within the module. The default values, which describe a 50 horsepower induction machine/traction motor with a fixed efficiency inverter, are listed in Table 8 on the following page.

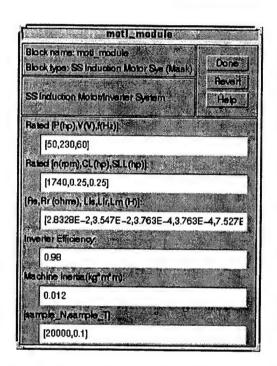


Figure 20. Window Displayed When Mask Is Activated For The Induction Machine –

Traction Motor Module With Fixed Rectifier Efficiency

| Table 8. Default Values | | | | | | |
|--|---------------|--|--|--|--|--|
| Machine Definitions | Values | | | | | |
| Rated Power | 50 hp | | | | | |
| Rated Voltage | 230 V | | | | | |
| Rated Frequency | 60 Hz | | | | | |
| Rated Speed | 1740 rpm | | | | | |
| Core Losses @ Rated Voltage & Speed | 0.25 hp | | | | | |
| Stray Load Losses @ Rated Voltage & Speed | 0.25 hp | | | | | |
| Per-Phase Stator Resistance, R _s | 2.8328Ε-2 Ω | | | | | |
| Per-Phase Rotor Resistance, R _r | 3.547E-2 Ω | | | | | |
| Per-Phase Stator Leakage Inductance, Lis | 3.763E-4 H | | | | | |
| Per-Phase Rotor Leakage Inductance, Lir | 3.763E-4 H | | | | | |
| Per-Phase Magnetizing Inductance, L _m | 7.527E-3 H | | | | | |
| Inverter Efficiency | 0.98 | | | | | |
| Motor Inertia | 0.012 [kg·m²] | | | | | |
| Number of Samples Saved to Workspace | 20000 | | | | | |
| Time Between each Saved Sample | 0.1 | | | | | |

3.5 Steady-State Induction Machine - Traction Motor System with Calculated Inverter Losses

| INPUTS | OUTPUTS |
|---------------------------------|--|
| DC Bus Voltage [V] | Inverter Current [A] |
| Rotor Speed [rpm] | [Output Torque [N·m], Machine Inertia [kg·m²]] |
| Per Unit Input Torque Command[] | |

Constants as defined by the mask:

VAr: Rated Power of Motor [W]

Vr: Rated Line-Neutral Voltage of Motor [V] wb: Base Speed of Motor for Per Unit [rad/s]

wmr: Rated Speed of Motor [rad/s] poles: Number of Motor Poles []

corel: Core Losses of Motor @ Rated Voltage & Speed [W]
SLL: Stray Load Losses of Motor @ Rated Voltage & Speed [W]

Ib: Base Line Current of Motor [A]

Zb: Base Impedance of Motor for Per Unit $[\Omega]$

Rspu: Per Unit Stator Resistance []
Rrpu: Per Unit Rotor Resistance []
Lspu: Per Unit Stator Inductance []
Lrpu: Per Unit Rotor Inductance []

Lmpu: Per Unit Magnetizing Inductance []

fluxr: Per Unit Rotor Flux @ Rated Conditions []

Inertia out: Machine Inertia [kg·m²]

fc: PWM Switching Frequency of the Inverter [Hz]

EQD: Total Switching Energy Loss per Amp of the IGBT-Diode Combination

[J/A]

Vnom: Voltage at which EQD is specified [V]

rQ: On State IGBT Resistance $[\Omega]$ rD: On State Diode Resistance $[\Omega]$

VQ: Forward Voltage Drop of the IGBT [V]
VD: Forward Voltage Drop of the Diode [V]

PWM: Determines if Sinusoidal(1) or Space Vector (0) PWM is used.[]

sample_N: Number of Samples to Save to the MATLAB® Workspace

sample T: Length of Time Between Each Sample

Auxiliary Calculations: None

Mask:

- 1. SS Induction Motor Sys
- SS Induction Motor/Inverter System|Rated [P(hp), V(V), f(Hz), Machine Inertia(kg*m*m)]:|Rated [n(rpm), CL(hp), SLL(hp)]:|[Rs,Rr (ohms), Lls, Llr, Lm (H)]:|Inverter [rQ, rD (ohms), VQ, VD(V)]:|Inverter [PWM, fc(Hz), EQD(J/A), Vnom (V)]:|[sample_N,sample_T]:
- 3. mdefn=motlinit(@1,@2,@3); VAr=mdefn(1,1); Vr=mdefn(1,2); wb=mdefn(1,3); wmr=mdefn(1,4); poles=mdefn(1,5); corel=mdefn(1,6); SLL=mdefn(1,15); Ib=mdefn(1,7); Zb=mdefn(1,8); Rspu=mdefn(1,9); Rrpu=mdefn(1,10); Lspu=mdefn(1,12); Lrpu=mdefn(1,13); Lmpu=mdefn(1,11); fluxr=mdefn(1,14); rQ=@4(1,1); rD=@4(1,2); VQ=@4(1,3); VD=@4(1,4); PWM=@5(1,1); fc=@5(1,2); EQD=@5(1,3); Vnom=@5(1,4); Inertia_out=@1(1,4); sample_N=@6(1,1); sample_T=@6(1,2);

This module simulates a three-phase, squirrel-cage induction motor and a three-phase, boost-type or voltage-sourced (IGBT) inverter supply. The three phase inverter employs either the sinusoidal PWM method [1] or the space vector PWM method [2]. The module mask contains the example values for a 50 hp, 230 V motor, which are user changeable. The core losses and stray load losses are included in the model and can be set in the module mask as well. Please refer to the assumptions below for other important simulation details.

Assumptions:

- This module will only be used in simulations with a minimum time step of 100 ms or larger.
- The motor is controlled at all times with conventional "field-oriented" or "vector" control. That is, the slip frequency and current in motor are regulated to provide dynamic control of the motor torque.
- The flux in the motor is limited to its rated value (\approx rated V/f).
- The torque is limited to the peak or pullout torque for rated flux. Therefore, the current is therefore limited to the current at peak torque.
- When the bus voltage is not sufficient to provide rated flux, field weakening is enabled which maintains maximum bus voltage on the motor. In this mode, the flux is inversely proportional to the motor speed, and the peak torque is inversely proportional to the square of the motor speed.

- The copper losses are modeled by R_s and R_r' in Figure 21. The core losses are calculated to be proportional to the motor flux. The stray load losses are proportional to the motor torque.
- The sign convention for the motor module is that positive current enters the terminals of the machine. Positive current produces positive torque, i.e., positive dc inverter current (output #1) indicates the module is motoring.
- Within the module, a set of power values is computed at each time step to facilitate energy balance equations. The power values are as follows: the dc bus power, the mechanical power of the motor, the electrical power at the terminals of the machine, the inverter loss power, and the total motor losses (core, stray load, and copper losses). These values are *not* saved to the workspace automatically.
- Loss calculations for the Alt-Rev space vector PWM method [2] are based on the third harmonic PWM method since both control methods result in similar steady-state operation.
- Phase currents and phase voltages of the machine are assumed to be purely sinusoidal for inverter loss calculations. This assumption is justifiable if the PWM frequency is reasonably high.
- The model does not include inverter harmonic effects.

Figure 21 shows the inputs and outputs of the steady-state induction motor model. Figure 22 depicts the per-phase equivalent circuit model of the induction machine and defines the motor parameters. Figure 23 shows the induction motor model after the transformation to the synchronous d-q reference frame. The electrical terminal voltages and currents are calculated directly from this equivalent circuit and the mechanical equations using the command values of torque and speed. The synchronous reference frame electrical and mechanical equations used in the simulation are,

$$\begin{aligned} v_{qs}^{e} &= R_{s}i_{qs}^{e} + \omega \lambda_{ds}^{e} \\ v_{ds}^{e} &= R_{s}i_{ds}^{e} - \omega \lambda_{qs}^{e} \\ 0 &= R_{r}i_{qr}^{e} + (\omega - \omega_{r})\lambda_{dr}^{e} \\ 0 &= R_{r}i_{dr}^{e} - (\omega - \omega_{r})\lambda_{qr}^{e} \\ \lambda_{qs}^{e} &= (L_{m} + L_{ls})i_{qs}^{e} + L_{m}i_{qr}^{e} \\ \lambda_{ds}^{e} &= (L_{m} + L_{ls})i_{ds}^{e} + L_{m}i_{qr}^{e} \\ \lambda_{qr}^{e} &= (L_{m} + L_{lr})i_{qr}^{e} + L_{m}i_{qs}^{e} \\ \lambda_{dr}^{e} &= (L_{m} + L_{lr})i_{qr}^{e} + L_{m}i_{ds}^{e} \\ \tau &= L_{m}(i_{as}^{e}i_{dr}^{e} - i_{ds}^{e}i_{qr}^{e}) \end{aligned}$$

where the e superscript denotes the synchronous reference frame.

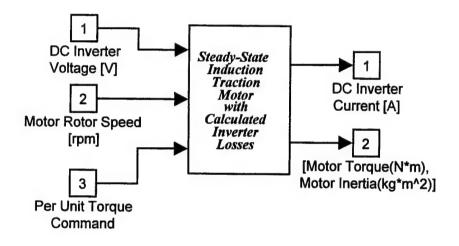


Figure 21. Inputs And Outputs Of Induction Traction Motor System
With Calculated Inverter Losses

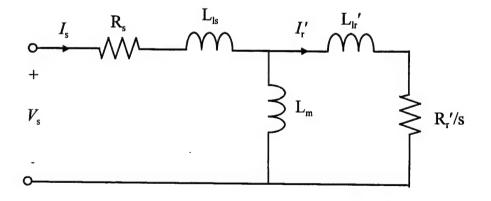


Figure 22. Induction Machine Per Phase Equivalent Circuit

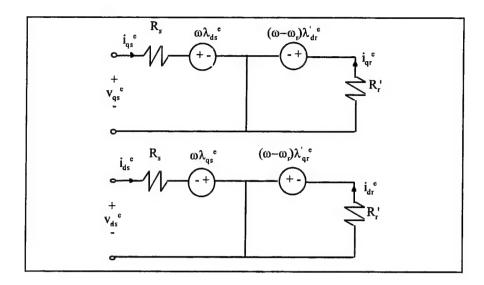


Figure 23. Steady-State dq Equivalent Circuit Of An Induction Motor

The motor is controlled using conventional rotor flux field orientation ("brushless dc" control) such that in the synchronous reference frame, $\lambda_{qr}^{e} = 0$.

The following are the machine variables used for device loss calculations within the inverter:

$$\begin{split} I_{P} &= \sqrt{2} \; Ib \; \sqrt{2 \left(Iqspu^{2} + Idspu^{2} \right)} \\ V_{p} &= \sqrt{2} \; V \; \sqrt{2 \left(Vqspu^{2} + Vdspu^{2} \right)} \\ \phi &= \tan^{-1} \left(\frac{Vdspu}{Vqspu} \right) - \tan^{-1} \left(\frac{Idspu}{Iqspu} \right) \\ M &= \frac{2V_{P}}{Vdc} \end{split}$$

| V_{D} | Peak machine output phase voltage |
|---------|---|
| v- | Peak output current of the machine |
| M | Modulation index |
| ϕ | Phase lag of the machine line current |
| Vdc | Voltage of the DC bus. |
| Iqspu | RMS q-axis machine output current |
| Idspu | RMS d-axis machine output current |
| Vqspu | RMS q-axis machine output phase voltage |
| Vdspu | RMS d-axis machine output phase voltage |
| | φ Vdc Iqspu Idspu Vqspu |

Table 9 shows the equations governing the inverter device currents.

| Table | Table 9. Equation Governing the Inverter Device Currents | | | | | | |
|---|--|---|--|--|--|--|--|
| Device Currents | Sinusoidal PWM | Space Vector PWM | | | | | |
| $\overline{I_{\mathcal{Q}}}$ | $I_{p}\left(\frac{1}{2\pi} + \frac{M\cos\phi}{8}\right)$ | $I_{p}\left(\frac{1}{2\pi} + \frac{\sqrt{3}M\cos\phi}{12}\right)$ | | | | | |
| $\overline{I_D}$ | $I_{p}\left(\frac{1}{2\pi}-\frac{M\cos\phi}{8}\right)$ | $I_{p}\left(\frac{1}{2\pi}-\frac{\sqrt{3}M\cos\phi}{12}\right)$ | | | | | |
| $\left I_{Q} ight _{\mathit{RMS}}$ | $I_{p}\sqrt{\frac{1}{8} + \frac{M\cos\phi}{3\pi}}$ | $I_{p}\sqrt{\frac{1}{8}+M\frac{30\cos\phi-\cos3\phi}{45\sqrt{3}\pi}}$ | | | | | |
| $\left I_{\scriptscriptstyle D} ight _{\scriptscriptstyle RMS}$ | $I_{p}\sqrt{\frac{1}{8}-\frac{M\cos\phi}{3\pi}}$ | $I_{p}\sqrt{\frac{1}{8}-M\frac{30\cos\phi-\cos3\phi}{45\sqrt{3}\pi}}$ | | | | | |

where

 $\begin{array}{ll} \overline{I_{\mathcal{Q}}} & \text{Average current through the IGBT} \\ \overline{I_{\mathcal{D}}} & \text{Average current through the diode} \\ \left|I_{\mathcal{Q}}\right|_{\mathit{RMS}} & \text{RMS current through the IGBT} \\ \left|I_{\mathcal{D}}\right|_{\mathit{RMS}} & \text{RMS current through the diode} \end{array}$

The inverter losses are then calculated using the following equations:

Conduction losses:

$$\begin{split} P_{Q(cond)} &= \overline{I_Q} \cdot VQ + \left| I_Q \right|^2_{RMS} \cdot rQ \\ P_{D(cond)} &= \overline{I_D} \cdot VD + \left| I_D \right|^2_{RMS} \cdot rD \end{split}$$

where

 $P_{Q(cond)}$ Conduction power loss in the IGBT $P_{D(cond)}$ Conduction power loss in the diode

Switching losses:

$$\begin{split} P_{Q(sw)} &= \frac{f \cdot E_Q \cdot I_p}{\pi} \bigg(\frac{Vdc}{Vnom} \bigg) \\ P_{D(sw)} &= \frac{f \cdot E_D \cdot I_p}{\pi} \bigg(\frac{Vdc}{Vnom} \bigg) \\ P_{TOT(sw)} &= P_{Q(sw)} + P_{D(sw)} = \frac{f \cdot EQD \cdot I_p}{\pi} \bigg(\frac{Vdc}{Vnom} \bigg) \end{split}$$

The total inverter loss power (P_{loss}) is six times the sum of the conduction and switching losses of the IGBT and the diode.

$$P_{loss} = 6\left(P_{O(sw)} + P_{D(sw)} + P_{O(cond)} + P_{D(cond)}\right)$$

IGBT Selection Guide:

Table 10 shows the IGBT modules that contain antiparallel diodes.

| | Table 10. IGBT Modules that Contain Antiparallel Diodes | | | | | | | | | |
|--------------|---|------|---------|-------|---------|---------------------|-------------------------------|------------------|----------------------|--|
| IGBT Module# | Frequency | VCES | lc@ | PDMAX | VQMAX@ | VD _{MAX} @ | EQD (@Vnom) | rQ (m Ω) | rD (m Ω) | |
| | Range | (V) | TJ=25°C | (VV) | TJ=25°C | TJ=25°C | @ TJ=125°C | @ ТJ | @TJ=125 ⁰ | |
| | (kHz) | | (A) | | (V) | (V) | (mJ/A) | =125°C | С | |
| IRGDDN300M06 | 3-10 | 600 | 400 | 1563 | 2.0 | 2.0 | 0.2 @ V _{nom} =300V | _ | - | |
| IRGDDN400M06 | 3-10 | 600 | 600 | 1984 | 2.0 | 2.0 | 0.2 @ V _{nom} =300V | - | - | |
| IRGDDN600M06 | 3-10 | 600 | 800 | 2604 | 2.7 | 2.0 | 0.2 @ V _{nom} =300V | - | _ | |
| IRGDDN200M12 | 3-10 | 1200 | 420 | 1800 | 2.7 | 3.4 | 0.6 @ V _{nom} =600V | 2.00 | 5.50 | |
| IRGDDN300M12 | 3-10 | 1200 | 560 | 2400 | 2.7 | 3.4 | 0.6 @ V _{nom} =600V | 2.50 | 4.00 | |
| IRGDDN400M12 | 3-10 | 1200 | 400 | 2770 | 2.7 | 3.4 | 0.6 @ V _{nom} =600V | - | - | |
| IRGDDN300K06 | 10-30 | 600 | 340 | 1563 | 2.7 | 2.0 | 0.15 @ V _{nom} =300V | - | - | |
| IRGDDN400K06 | 10-30 | 600 | 520 | 1984 | 2.7 | 2.0 | 0.15 @ V _{nom} =300V | - | - | |
| IRGDDN600K06 | 10-30 | 600 | 680 | 2604 | 2.7 | 2.0 | 0.15 @ V _{nom} =300V | | - | |

| where | V_{CES} | Maximum Continuous Collector to Emitter Voltage | |
|-------|---|---|--|
| | I _C Maximum Continuous Collector Current | | |
| | P_{DMAX} | Maximum Power dissipation | |
| | VQ_{MAX} | Maximum Collector to Emitter ON Voltage | |
| | VD_{MAX} | Maximum Forward Voltage Drop of the Diode | |
| | EQD | Total Switching Energy Loss per Amp of the IGBT-Diode Combination | |
| | V_{nom} | Collector Voltage at which EQD is specified | |
| | rQ | On State IGBT Resistance | |
| | rD | On State Diode Resistance | |
| | T_{J} | Device Junction Temperature | |

The value of on-state resistance of the IGBT and diode is found by calculating the inverse of the slope of the device current versus device voltage curve(during conduction).

When the mask is activated, the window in Figure 24 is displayed. The first input line asks the user to list the rated power, rated line voltage, and rated frequency of the induction motor as well as the system inertia. The next input requests the values for the rated speed, and the rated core and stray load losses that occur under rated operating conditions. The per-phase machine parameters of stator and rotor resistance, stator and rotor leakage inductance, and the magnetizing inductance are defined in the third line of the mask. The inverter is described by the next two input vectors of the mask. In the first vector, the on-state resistance of the switching devices (rQ) and the diodes (rD) and their respective forward voltage drops are defined. The second input vector for the inverter specifies the PWM method (1 for Sinusoidal/0 for Space Vector), the switching frequency, the total switching energy loss per amp of the switching device/diode combination, and the collector voltage at which this switching loss occurs. Finally, the user can specify the number of samples and the time step between each sample for use in "To Workspace" blocks within the module. The default values listed in Table 11 on the following page describe a 50 horsepower induction machine/traction motor with a three-phase IGBT boost inverter.

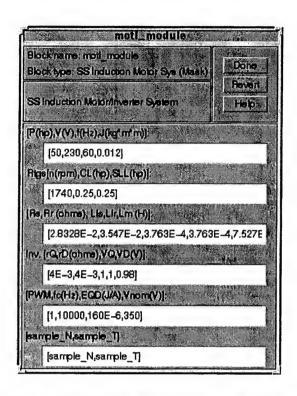


Figure 24. Window Displayed When Mask Is Activated For The Induction Machine –
Traction Motor Module With Calculated Inverter Losses

| Table 11. Default Values | |
|--|---------------|
| Machine and Inverter Definitions | Values |
| Rated Power | 50 hp |
| Rated Power | 50 hp |
| Rated Voltage | 230 V |
| Rated Frequency | 60 Hz |
| Rated Speed | 1740 rpm |
| Stray Load Losses @ Rated Voltage & Speed | 0.25 hp |
| Core Losses @ Rated Voltage & Speed, Core L | 0.25 hp |
| Per-Phase Stator Resistance, R _s | 2.8328E-2 Ω |
| Per-Phase Rotor Resistance, R _r | 3.547E-2 Ω |
| Per-Phase Stator Leakage Inductance, L _{is} | 3.763E-4 H |
| Per-Phase Rotor Leakage Inductance, L _{ir} | 3.763E-4 H |
| Per-Phase Magnetizing Inductance, L _m | 7.527E-3 H |
| Motor Inertia | 0.012 [kg·m²] |
| PWM Switching Frequency of the Inverter, fc | 10000 Hz |
| Total Switching Energy Loss per Amp of the IGBT-Diode Combination, EQD | 160 □J/A |
| Voltage at which EQD is specified, Vnom | 350 V |
| On State IGBT Resistance, rQ | 4.0E-3 □ |
| On State Diode Resistance, rD | 4.0E-3 □ |
| Forward Voltage Drop of the IGBT, VQ | 1 V |
| Forward Voltage Drop of the Diode, VD | 1 V |
| Type of PWM used [Sinusoidal(1) or Space Vector(0)] | 1 |
| Number of Samples to Save to the MATLAB Workspace, sample_N | 20000 |
| Length of Time Between Each Sample, sample_T | 0.1 |

References:

- [1] Ken Berringer, Jeff Marvin and Philippe Perruchoud, "Semiconductor Power Losses in AC Inverters," *Conference Record-IAS Annual Meeting* (IEEE Industry Applications Society), pp. 882-886, 1995.
- [2] Philippe J.P. Perruchoud and Peter J. Pinewski, "Power Losses for Space Vector Modulation Techniques," *IEEE Workshop on Power Electronics in Transportation*, pp. 167-173, Oct. 1996.

3.6 Table lookup steady-state generator (No electrical parameters)



| INPUT | OUTPUT |
|---------------------------|--------------------------|
| Desired AC Current (Amps) | Shaft Torque (N-m) |
| Shaft Speed (rpm) | DC Current (Amps) |
| DC Bus Voltage (V) | Actual AC Current (Amps) |

Purpose:

Parameters:

| llimw_mot llimw_gen llim_mot llim_gen | vector of shaft speed (rad/s) for lookup of limit current (motor mode) vector of shaft speed (rad/s) for lookup of limit current (motor mode) vector of limit currents in motor mode vector of limit currents in generator mode |
|--|--|
| mtrp1_Voc mtrp1_Vd mtrp1_Np mtrp1_n mtrp1_I mtrp1_J | line to line voltage (V) for machine at design speed but open circuit line to line voltage (V) for machine at design conditions number of poles shaft speed (rad/s) for machine at design conditions line to line current (A) for machine at design conditions motor inertia constant (kg*m^2) |
| mtrp1_eff mtrp1_conv_eff | motor efficiency (0-1) converter efficiency (0-1) |

Auxiliary Calculations:

$$Ke = Voc/\omega_d$$

 ω_d is design speed in rad/s

$$K_{t} = \frac{I * V_{d} * \sqrt{3}}{\omega_{d}} \eta_{m}$$

$$Ls = \sqrt{\frac{{V_d}^2 - {V_{oc}}^2}{(I^* \omega_d * Np/2)^2}}$$

genp1 module1 Mask

- (1) genp_simp
- (2) Simple Scaling PM Generator Definitions (Click on "Help" to list Inport and Outport parameters.)|Limit Current Lookup Vectors|Ke & Kt|[Motor Efficiency,Converter Efficiency]|[Npoles,Ls]|Inertia Constant (kg*m^2)
- (3) Ilimw_mot=@1(1,:);Ilimw_gen=@1(2,:);Ilim_mot=@1(3,:);Ilim_gen=@1(4,:); Ke=@2(1);Kt=@2(2);eff_motor=@3(1);c1=sqrt(3)/@3(2);c2=sqrt(3)*@3(2); npLs=@4(1)*@4(2)/2;J=@5;
- (4) Simple\nScaling\nPM Gen
- (5) Simple Scaling PM Generator Block Port Parameters\n\nInport 1: DC Bus Voltage (V).\nInport 2: Shaft Speed (RPM).\nInport 3: AC Current Command (A).\n\n Outport 1: DC Current (A).\nOutport 2: Vector of [Shaft Torque (N*m), Inertia Constant (kg*m^2)].

Modeling Equations

$$V_{ac} = K_e * \omega_d$$
 where η_m is the machine efficiency

$$T = I_{ac} * K_t * \eta_m \qquad \text{for motor mode (Iac > 0)}$$

$$I_{ac} * K_t / \eta_m \qquad \text{for generator mode (Iac < 0)}$$

$$I_{dc} = \frac{V_{ac} * I_{ac} * \sqrt{3}}{V_{dc}} \left(\frac{1}{\eta_c}\right) \qquad \text{for motor mode (Iac > 0)}$$

$$= \frac{V_{ac} * I_{ac} * \sqrt{3}}{V_{dc}} \eta_c \qquad \text{for generator mode (Iac < 0)}$$

and $\eta_{\rm c}\,$ is the converter efficiency

4.0 ENERGY STORAGE LIBRARY

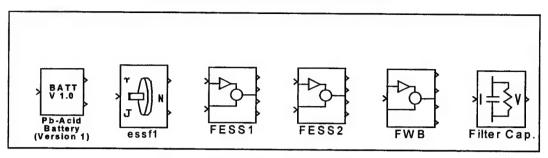
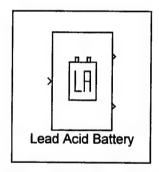


Figure 25. Battery Model Library

The energy-storage library contains modules that can be used to store or deliver energy to an HEV. The energy-storage device is typically located between a power management controller and the traction motor.

4.1 Lead Acid Battery



| INPUTS | OUTPUTS | |
|------------------------|---------------------|--|
| System Current Sum [A] | DC Bus Voltage [V] | |
| | State-Of-Charge [] | |

Constants as defined by the mask:

tot_num: Total Number of Series Cells in System []

Eoc: Open-Circuit Voltage of a Single Cell [V]

cell_r: Internal Resistance of a Cell $[\Omega]$ cell_K: Polarization Resistance of a Cell $[\Omega]$

term_Rb: Terminal Resistance of the Battery System $[\Omega]$ Ct: Terminal Capacitance of the Battery System [F]

C5: Discharge Capacity @ 5 hour rate and 30°C [A-hr]

chrg_eff: Charge Efficiency of the Battery []
dischrg_eff: Discharge Efficiency of the Battery []

amb_T: Ambient Temperature in °C (-20°C to 60°C)

init ECP: Initial Polarization Voltage [V]

init_SOC: Initial State-of-Charge of Battery System (0-1)

init_Q: Initial Energy within the Battery

Auxiliary Calculations: None

Mask:

- 1. Lead-Acid Battery ESS
- 2. Lead-Acid Battery-Series Cell Configuration [Num of Cells, Eoc(V) of cell]: |Cell Defns[r,Kpr (ohms)]: |Term Defns[Rb(ohms),Ct(F)]: |Chrg Defns[Cap(A-hrs)]: |[chg eff,dischg eff,temp(C)]: |[Init K V(V),Init SOC(0-1)]:
- 3. tot_num=@1(1,1); Eoc=@1(1,2); cell_r=@2(1,1); term_Rb=@3(1,1); cell_K=@2(1,2); Ct=@3(1,2); C5=@4(1,1); amb_T=@5(1,3); chrg_eff=@5(1,1); dischrg_eff=@5(1,2); init_ECP=@6(1,1); init_SOC=@6(1,2); init_Q=C5*3600*(1-@6(1,2));

Assumptions:

- The battery model is valid for the temperature range -20°C to 60°C.
- The internal resistance of the battery is considered constant throughout the battery operation. Typically, this varies with battery state of charge and temperature.
- When modeling a collection of batteries, each battery is assumed to have the same open circuit voltage and state of charge. In actuality, this is not true, since each battery can be at a different state of charge and therefore have a different open circuit voltage.
- Positive current entering the battery charges, negative current discharges
- The electrode polarization is not big.
- Electromotive potential E is the function of SOC and temperature.
- Polarization resistance depends on both the SOC and the direction of the current.
- Capacity is the function of temperature and current.
- Acid electrolyte mole concentration (if flooded battery) is 5M when the battery is fully charged.

The inputs and outputs of the lead-acid battery, energy-storage system are shown in Figure 26.

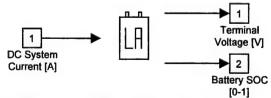


Figure 26. Inputs And Outputs Of Lead-Acid Battery Energy-Storage System

The mask contains default values for $300V - 25\ 12V$ cell, lead-acid battery system. These values are listed in Table 12. An example of the mask window for this module is displayed in Figure 27. The first input line asks for the number of cells within the energy storage system and the open circuit voltage of a single cell. The next input vector defines the internal cell resistance and the polarization resistance of a cell. The terminal resistance and capacitance of the energy-storage system are listed in next input vector. The total capacity of the energy-storage system is defined in the fourth vector. The fifth input vector contains the values for the ambient temperature of the system as well as the system's charge and discharge efficiencies. The initial state of the energy-storage system is defined by the initial polarization voltage and the initial state of charge.

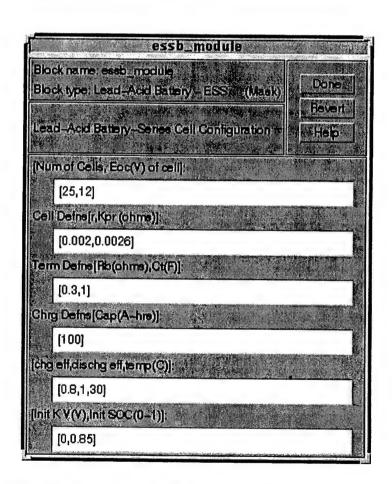
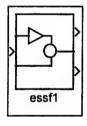


Figure 27. Window Displayed When Mask Is Activated For The Lead Acid
Battery – Energy Storage System

| Table 12. Default Values | | |
|---|------------|--|
| System Definitions | Values | |
| Total Number of Batteries | 25 cells | |
| Single Battery Open-Circuit Voltage | 12 V | |
| Internal Resistance(r) of a Battery | 2.0E-3 Ω | |
| Polarization Resistance(K) of a Battery | 2.6Ε-3 Ω | |
| Terminal Resistance(Rb) of the Battery Pack | 0.3 Ω | |
| Terminal Capacitance of the Battery Pack | 1.0 F | |
| Discharge Capacity @ 5 hour rate and 30°C for a Battery | 100 [A-hr] | |
| Charge Efficiency of the Battery System | 0.8 | |
| Discharge Efficiency of the Battery System | 1 | |
| Ambient Temperature in °C | 30°C | |
| Initial Polarization Voltage(η) | 0 | |
| Initial State-of-Charge of the Battery System(0-1) | 0.85 | |

4.2 Flywheel Battery



| INPUTS | OUTPUTS |
|-------------------|--------------------------------|
| Input Current (A) | DC Bus Voltage (V) |
| | Flywheel State of Charge (0-1) |

Purpose:

This block models a flywheel battery and an associated internal controller. The model incorporates a simple flywheel model with a steady-state PM motor/generator model and inverter/rectifier. The inputs and outputs are the same as the chemical battery making this device appear as a controllable DC voltage source. In order to make voltage an output, this model includes a capacitor and resistor in parallel across the terminal. The choice of capacitance to maintain stability in the bus voltage is dependent on the peak loads, and time step being used in the simulation. Note that this capacitance does not relate directly to a capacitor rating required on the bus. Though some form of capacitance will be required, its exact value will require a higher fidelity simulation running at much smaller time steps than

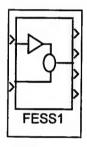
the 1/10 sec typically used for this model. The controller included in this model is a sample of a simple technique for maintaining a specified voltage on the bus. Other control methods may also be desired and may be implemented by the user by unmasking the block.

Parameters:

Auxiliary Calculations: None

Flywheel Battery Mask: no mask)

4.2.1 Flywheel Battery (Roller Bearings)



| INPUTS | OUTPUTS |
|---------------------|----------------------------|
| Voltage (V) | Output Current (A) |
| Current Command (A) | Speed (RPM) |
| | Discharge Efficiency (0-1) |
| | Charge Efficiency (0-1) |

Purpose:

There are two major components and one auxiliary component of this system:

- 1. Motor/Generator and Converter
- 2. Flywheel
- 3. Efficiency Calculation

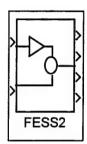
This subsystem uses a permanent magnet generator. The 'current command' is the current command provided to the generator controller. The 'output current' is the actual current output to the DC Bus. Inputs for the 'Flywheel Subsystem' are DC Voltage, generator torque, generator inertia, and bearing loads. The 'Flywheel Subsystem' has outputs of auxiliary current draw, stored mechanical power, and rotor speed.

Parameters:

Auxiliary Calculations: None

Flywheel Energy Storage Subsystem 1 Mask: (no mask)

4.2.2 Flywheel Battery (Magnetic Bearings)



| INPUTS | OUTPUTS |
|---------------------|----------------------------|
| Voltage (V) | Output Current (A) |
| Current Command (A) | Speed (RPM) |
| | Discharge Efficiency (0-1) |
| | Charge Efficiency (0-1) |

Purpose:

There are two major components and one auxiliary component of this system:

- 1. Motor/Generator and Converter
- 2. Flywheel
- 3. Efficiency Calculation

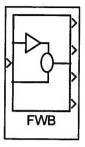
This subsystem uses a permanent magnet generator. The 'current command' is the current command provided to the generator controller. The 'output current' is the actual current output to the DC Bus. Inputs for the 'Flywheel Subsystem' are DC Voltage, generator torque, generator inertia, and bearing loads. The 'Flywheel Subsystem' has outputs of auxiliary current draw, stored mechanical power, and rotor speed.

Parameters:

Auxiliary Calculations: None

Flywheel Energy Storage Subsystem II Mask: (no mask)

4.2.3 Flywheel Battery (Simple Model)



| INPUTS | OUTPUTS |
|-------------------|----------------------------|
| Input Current (A) | Voltage (V) |
| | SOC (0-1) |
| | Discharge Efficiency (0-1) |
| | Charge Efficiency (0-1) |

Purpose:

This block models a flywheel battery with a simple feed-forward control and low gain feedback. The feed-forward signal exactly balances the input current. There is a low gain feedback to keep the bus voltage near its reference to adjust for losses.

Parameters:

Auxiliary Calculations: None

Flywheel Battery System Mask: (no mask)

4.3 Capacitor



| INPUTS | OUTPUTS |
|----------------|-----------------|
| Current [amps] | Voltage [volts] |

Constants:

cap_capacitance:

Capacitance [F]

cap resistance:

Self-discharge resistance $[\Omega]$

cap_initial_voltage:

Initial Charge Voltage [V]

Auxiliary Calculations: None

Mask:

(1) Capacitor Module

(2) Capacitor Module|Capacitance [F]|Self-Discharge Resistance [ohms]|Initial

Voltage [V]

(3) Capacitance=@1;Resistance=@2;Initial_Voltage=@3;

Assumptions:

For most capacitors the primary loss mechanism is the series resistance of the capacitor.

This has been ignored in this model to avoid algebraic loops which could arise. There are

other secondary effects such as hysteresis which could be modeled, but in general these

effects are neglected.

The following presents typical values of the constants used in the capacitor model

Constant

Value

cap_capacitance:

20E-3 [F]

cap resistance:

2E6 [Ω]

cap initial voltage:

230 [V]

5.0 VEHICLE LIBRARY

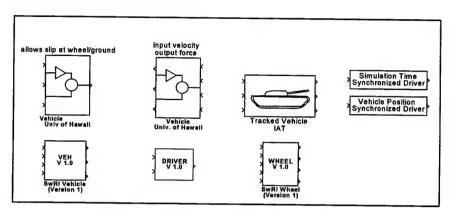
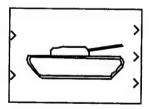


Figure 28. Vehicle Model Library

This library contains models of both tracked and wheeled vehicles. There are two versions for the wheeled vehicle and wheel modules. The first version contains a differentiator block, and the second version avoids this differentiator block through reformulation of the dynamic equations. Both versions have been tested to produce the same results, although version 2 executes faster than version 1.

5.1 Tracked Vehicle



| INPUTS | OUTPUTS |
|---|-----------------------------|
| Fuel Mass(kg) | Sprocket (Axle) Speed (rpm) |
| Vector of [Shaft Torque(N-m), Eff Motor + Coupling Inertia (kg*m^2) | Vehicle Position (m) |
| Terrain Gradient (rad) | Vehicle Velocity (rpm) |

Purpose:

The purpose of this block is to simulate the dynamics of a tracked vehicle by summing forces from various inputs, including aerodynamic drag, rolling resistance, and drag due to slope. This sum is divided by the inertia of the vehicle to determine its acceleration, which is then

integrated once for velocity and twice for position. Note that this model does not include active suspension loads.

Parameters:

| track_r | radius (m) of track drive sprocket |
|-----------|---|
| track_b | track damping constant (N/(rad/s)) for friction torque |
| track_J | effective inertia of track (in vehicle reference frame, Kg* m²) |
| veh_mass | Gross vehicle mass less fuel (kg) |
| veh_Cd | coefficient of aerodynamic drag of the vehicle |
| veh_A | Frontal area of vehicle (m^2) |
| veh_pos_i | Initial position of vehicle (m) |
| veh_spd_i | Initial velocity of vehicle (m/s) |
| veh_RR_m: | Rolling resistance of vehicle (velocity independent) [N/kg] |
| veh_RR_v: | Rolling resistance vs. velocity [N/(m/s)] |
| | |
| sample N | max number of samples |
| | • |
| sample_T | simulation time between samples |

Auxiliary Calculations: None

Vehicle Mask

- (1) Tracked-Vehicle Dynamics
- (2) Tracked Vehicle Dynamics Block Definitions\n(Click on "Help" to list Inport and Outport parameters.)|[Sprocket Radius (m), Damping Constant (N*s), Inertia (kg*m^2)]|Vehicle Mass (kg)|{RR_m (N/kg),RR_v (N*s/m),Cd,Affront]|[Initial Position (m),Initial Speed (m/s)]|[sample N,sample T]
- (3) r=@1(1);b=@1(2);J=@1(3);mass=@2;RR_m=@3(1);RR_v=@3(2);Cd=@3(3); A=@3(4);pos_i=@4(1);spd_i=@4(2);sample_N=@5(1);sample_T=@5(2);
- (4) Drawing Commands
- (5) Tracked-Vehicle Dynamics Block Port Parameters\n\nInport 1: Fuel Mass (kg).\nInport 2: Vector of [Shaft Torque (N*m), Effective Motor+Coupling Inertia (kg*m^2)].\nInport 3: Terrain Gradient (radians).\n\nOutport 1: Sprocket (Axle) Speed (RPM).\nOutport 2: Vehicle Position (m)\nOutport 3: Vehicle Velocity (m/s)

Model Equations:

This model is appropriate for modeling heavy vehicles and in particular, vehicles with tracks, where there is data on the static rolling resistance. It assumes that there are five forces acting on the vehicle:

The aerodynamic force:

 $Faero = Cd*Area*vel^2$

The static rolling resistance:

Frrm = Rm*vehicle mass

The dynamic rolling resistance:

Frrv = Rv*vel

The gravity force (dependent on grade in direction of travel):

Fgrad = vehicle mass * g * sin(grad)

The effective thrust force of the drive train: an input (see note below)

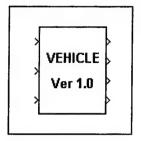
These forces are summed and divided by the effective mass of the vehicle to determine its acceleration. This acceleration can then be integrated to determine the velocity of the vehicle.

The effective mass of the vehicle is determined by the following equation, which accounts for fuel usage and rotational inertia of the drive train.

 $m_{effective} = m_{dry} + m_{fuel} + m_{effdrivetrain}$

Note that the effective thrust available from the drive train has had all velocity-dependent torques deducted in previous blocks, but has not had any deduction for inertial effects. These inertial effects are collected in this block and accounted for in meffdrivetrain.

5.2 Wheeled Vehicle (Version 1)



| Inputs | Outputs |
|-----------------------------|----------------------------|
| Vehicle Velocity [m/s] | Total Load on Vehicle [N] |
| Road Grade [radian] | Maximum Traction Force [N] |
| Fuel Mass [kg] | Total Vehicle Mass [kg] |
| Vehicle Acceleration [m/s²] | |

Constants:

veh_air_density: Density of the air that the vehicle is exposed to [kg/m³]

veh_aero_drag_coef: Drag coefficient of vehicle [] veh front area: Frontal area of vehicle [m²]

veh_normal_wind: Wind velocity normal to vehicle motion [m/s]

veh_parallel_wind: Head wind velocity [m/s]

veh_coef_yaw_sens: Coefficient of yaw sensitivity of the vehicle during motion []

veh_drag_coef: Aerodynamic drag coefficient []

veh_fs: Vehicle speed dependent rolling coefficient [] veh_f0: Vehicle speed independent rolling coefficient []

Timesteps_max: Maximum number of the array size

of variables saved to workspace during simulation

Auxiliary Calculations:

yout veh: An array consisting of two vectors: actual vehicle

velocity [km/hr] and distance traveled [km]

veh_RR_tract_loss:Rolling resistance energy loss during acceleration [kWh]veh_RR_regen_loss:Rolling resistance energy loss during deceleration [kWh]veh_aero_regen_loss:Aerodynamic resistance energy loss during acceleration

[kWh]

veh aero tract loss: Aerodynamic resistance energy loss during deceleration

[kwh]

veh_inertial_tract_energy: Total energy required to accelerate vehicle [kwh]

veh_inertial_regen_energy: Total recovery energy available during deceleration

[kwh]

Mask:

(1) Vehicle Module

(2) Vehicle Module (SwRI)|[Air Density [kg/m³], Vehicle Aero Drag Coeff []]|Vehicle frontal Area [m²]|[Normal Wind Speed [m/s], Parallel Wind Speed [m/s]]|[Speed

Effect Friction Coef [],road friction coefficient [],Vehicle coef of yaw sensitivity [] |Vehicle Mass [kg]|Maximum Time Steps []

veh_air_density=@1[1];veh_aero_drag_coef=@1[2];veh_front_area=@2; veh_normal_wind=@3[1];veh_parallel_wind=@3[2];veh_fs=@4[1];veh_f0=@4[2];veh_coef_yaw_sens=@4[3];veh_mass=@5;timesteps_max=@6;

Assumptions:

- The total load acting on the vehicle is the sum of all the driving resistance forces. These consist of the aerodynamic drag, tire rolling resistance, and road grade dependent loads. In the calculation of aerodynamic forces, the effect of head wind and normal wind components have been included. In the computation of the tractive resistance, the effect of the vehicle speed on the traction coefficient has been considered.
- The total vehicle mass includes the weight of the fuel, which decreases as the heat engine produces power.

The following presents typical values used for the constants in the vehicle model

| Constant | Value |
|---------------------|-----------------------|
| veh_air_density: | $1.23 [kg/m^3]$ |
| veh_aero_drag_coef: | 0.4[] |
| veh_front_area: | $3.0 [m^2]$ |
| veh_normal_wind: | $0.0 [\text{m/s}^2]$ |
| veh_parallel_wind: | $0.0 [\text{m/s}^2]$ |
| veh_coef_yaw_sens: | 0.002[] |
| veh_drag_coef: | 0.4 [] |
| veh_fs: | 0.005 [] |
| veh_f0: | 0.01 [] |
| Timesteps_max: | 10000[] |

5.3 Wheeled Vehicle (Version 2)



| INPUTS | OUTPUTS |
|--------------------------------|---------------------------|
| Driving force into vehicle [N] | Velocity of vehicle [m/s] |
| Mass of fuel consumed [kg] | |
| Brake fraction [] | |
| Wheel mass [kg] | |
| Road grade [rad] | |

Constants:

same as Wheeled Vehicle (Version 1) (see Section 5.2)

Auxiliary calculations:

veh1_accel_hist:

Vehicle acceleration history

veh1_speed_hist

Vehicle speed history

veh1_position_hist

Vehicle position history

Mask:

(1) Vehicle Module

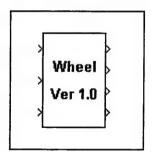
(2) Vehicle Module|Air Density (kg/m^3), Aero Drag Coeff ()|Vehicle Frontal Area (m^2)|Normal Wind Speed (m/s),Parallel Wind Speed (m/s)|Spd-dep Rolling Coef,V-indep Roll Coeff,Yaw Sens Coeff|Vehicle Chassis Mass (kg), Road/Tire Friction Coefficient []|Record Variable Quantity and Time (#,sec)

(3)veh_air_density=@1(1);veh_aero_drag_coef=@1(2);veh_front_area=@2;veh_normal_wind =@3(1);veh_parallel_wind=@3(2);veh_fs=@4(1);veh_f0=@4(2);veh_coef_yaw_sens=@4(3); veh_mass=@5(1);roadtire_frict_coef=@5(2);sample N=@6(1);sample T=@6(2);

Assumptions: Same as Wheeled Vehicle (Version 1) (see Section 5.2)

For typical values for the constants, please refer to Section 5.2.

5.4 Wheel (Version 1)



| Inputs | Outputs |
|--------------------------------|---------------------------|
| Driving force into vehicle [N] | Velocity of vehicle [m/s] |
| Mass of fuel consumed [kg] | |
| Brake fraction [] | |
| Wheel mass [kg] | |
| Road grade [rad] | |

Constants:

whl1 tr:

Wheel Tire Radius [m]

whl1 mass:

Wheel mass [kg]

motor N max:

Maximum motor speed [rpm]

timesteps max:

Maximum number of the array size

of variables saved to workspace during simulation

Auxiliary Calculations:

service brk energy:

Energy loss during application of the mechanical brake [kWh]

whl_tract_energy:

Energy delivered to the wheels during acceleration [kWh]

whl regen energy:

Energy recovered by the vehicle during deceleration of wheel

[kWh]

Mask:

(1) Wheel Module

(2) Wheel Module (SwRI)|Wheel Tire Radius [m]|Wheel Tire Mass [kg]|Max Motor Speed [rpm]|Max Timesteps []

(3) whl_tr=@1;whl_mass=@2;motor_N_max=@3;timesteps max=@4;

Assumptions:

The vehicle velocity and acceleration are based on the assumption that the entire mass of the vehicle is concentrated at the wheel center.

The following presents typical values used for the constants in the wheel model.

Constant

Value

whl1 tr:

0.3 [m]

whl1_mass:

25 [kg]

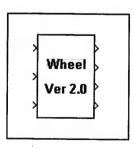
motor N max:

7000 [rpm]

timesteps max:

10000

5.5 Wheel (Version 2)



| INPUTS | OUTPUTS |
|-------------------------|-------------------------------------|
| Input Torque [Nm] | Driving Force [N] |
| Coupler Inertia [kg m²] | Rotational Speed of Wheel [rad/sec] |
| Vehicle Velocity [m/s] | Equivalent mass [kg] |

Constants:

whl1_tr:

Wheel Tire Radius [m]

whl1 mass:

Wheel mass [kg]

Auxiliary Calculations: None

Mask:

1. WHEEL MODULE

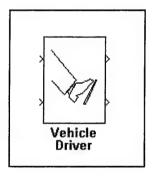
2. WHEEL MODULE (SwRI)\n\n T1,V,J1 (in) <=> F,N2,m (out)|Wheel System's Tire Radius [m]| Total Wheel Mass (Wheel,Tire, and Brake Sys) [kg]

3. wheel radius = @1; wheel mass = @2;

Assumptions:

The vehicle velocity and acceleration are based on the assumption that the entire mass of the vehicle is concentrated at the wheel center.

5.6 Driver



| INPUTS | OUTPUTS |
|---------------------|------------------------|
| Desired Speed [m/s] | Driver Power Demand [] |
| Actual Speed [m/s] | |

Constants:

dvr_proport_gain:Proportional gain of PID controller within driver model []dvr_integral_gain:Integral gain of PID controller within driver model []dvr_deriv_gain:Derivative gain of PID controller within driver model []

Auxiliary Calculations:

yout dvr: vector containing:

1. PID controller output (driver power demand) []

2. Desired speed [m/s]

3. Actual speed [m/s]

Mask: None

Assumptions:

The driver is modeled as a PID controller with fixed gains. The controller output is dependent on its gains and the error between the desired and actual vehicle speed.

The following shows typical values for the constants of the driver model.

Constants Value dvr_proport_gain: 0.2 [] dvr_integral_gain: 0.001 [] dvr_deriv_gain: 0 []

6.0 CONTROLLER LIBRARY

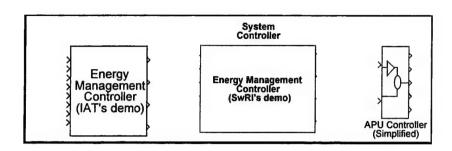
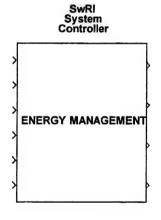


Figure 29. Controller Library

The controller library contains examples of energy-management controllers, which are dependent on the HEV application at hand. Therefore, these controllers are provided as examples of possible energy-management controllers, which the user can use as a basis to develop custom power management controllers. This library also includes controllers for the energy storage device and the APU.

6.1 Energy Management Controller (I)



| INPUTS | OUTPUTS |
|---------------------------------|----------------------------------|
| Generator Output Current [Amps] | Battery Current Command [Amps] |
| Drive Motor Current Draw [Amps] | Engine Throttle Command [0-1] |
| System Voltage [Volts] | Generator Current Command [Amps] |
| ESS Current Requirement [Amps] | Engine ON/OFF [1/0] |
| *ESS State of Charge [] | |
| Engine Speed [rpm] | |
| *ESS: Energy Storage System | |

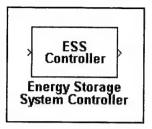
Constants: None

Auxiliary Calculations: None

Mask: None

Assumptions: Specific to application

6.1.1 Energy Storage System



| INPUTS | OUTPUTS |
|---|------------------------------|
| *ESS State of Charge | ON/OFF signal to **APU [1/0] |
| *ESS: Energy Storage System **APU: Alternate Power Unit | |

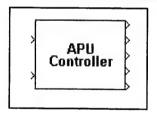
Constants: None

Auxiliary Calculations: None

Mask: None

Assumptions: Specific to application

6.1.2 APU Controller



| INPUTS | OUTPUTS |
|------------------------|----------------------------------|
| ESS State of Charge [] | Engine Throttle Command [0-1] |
| Engine Speed [rpm] | Generator Current Command [Amps] |
| | Engine ON/OFF [1/0] |

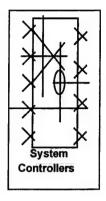
Constants: None

Auxiliary Calculations: None

Mask: None

Assumptions: Specific to application

6.2 System Controller



| INPUTS | OUTPUTS |
|--------------------------------|---------------------------|
| Generator Output Current (A) | Engine Throttle Command |
| Drive Motor Output Current (A) | Generator Current Command |
| System Voltage (V) | Battery Power Command |
| ESS Percent Power Command | Engine On/Off |
| Engine Speed (RPM) | |

Parameters:

Auxiliary Calculations: None

System Controllers Mask: None

7.0 COUPLING LIBRARY

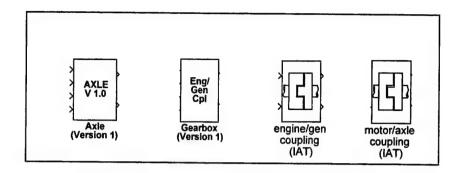


Figure 30. Coupling Model Library

The coupling library contains mechanical couplers representing shaft-to-shaft connections between blocks. These couplings allow for a gear ratio and an efficiency of power transfer. Couplers are typically located between the engine and the generator, as well as between the traction motor and the wheel.

7.1 Engine Generator Coupling



| INPUTS | OUTPUTS |
|--------------------------|-----------------------|
| Engine Torque [Nm] | Engine Speed [rpm] |
| Generator Torque [Nm] | Generator Speed [rpm] |
| Engine Inertia [kgm²] | |
| Generator Inertia [kgm²] | |

Constants:

cpl_speed_ratio:

Ratio of input shaft speed to output shaft speed of the coupler

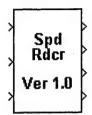
cpl efficiency:

Efficiency of coupler

Auxiliary Calculations: None

Mask: None

7.2 Motor Wheel Coupling (I)



| Inputs | Outputs |
|------------------------------------|-----------------------------------|
| Input Torque [Nm] | Output Torque [Nm] |
| Output Side Rotational Speed [rpm] | Input Side Rotational Speed [rpm] |
| Inertia of the driving component | Axle inertia at input [kg ·m²] |
| | Axle inertia at output [kg ·m²] |

Constants:

axl1 gear ratio:

Axle Gear Ratio (Output Gear Radius/Input Gear Radius) []

axl1 J1:

Axle Inertia at input [kg·m²]

axl1 J2:

Axle Inertia at output [kg·m²]

axl1_efficiency:

Axle Efficiency from input to output []

Auxiliary Calculations: None

Mask:

(1) Axle Module

(2) Axle Module (SwRI)|Axle Gear Ratio []|Axle Input Side Inertia $[kg \cdot m^2]$ |Axle Output Side Inertia $[kg \cdot m^2]$ |Axle Efficiency []

(3) axl_gear_ratio=@1;axl_J1=@2;axl_J2=@3;axl_efficiency=@4;

Assumptions:

- Internal efficiencies between the individual gears within the axle subsystem have not been considered. These are modeled by the variable axl_efficiency, which represents the overall inefficiency from the input to output shaft.
- The axle module dynamics (see Section 5.1, Technical Notes) is based on the analysis of two spur gears, one on the input side and the other on the output side. The dynamic model will need additional enhancements if more complex gear systems such as planetary gears are to be considered for the axle.
- Backlash effects within the gears have not been considered in the development of the axle model.

The following presents typical values used for the constants in the axle model

Constant

Value

axl1 gear ratio:

2[]

axl1_J1:

 $10 [kg \cdot m^2]$

axl1 J2:

 $10 [kg \cdot m^2]$

axl1_efficiency:

96.13 %

axl mass:

100 kg

7.3 Motor Wheel Coupling (II)



| INPUTS | OUTPUTS |
|---|-----------------------------------|
| Input Torque [Nm] | Output Torque [Nm] |
| Wheel Rotational Speed [rpm] | Input Side Rotational Speed [rpm] |
| Inertia of the driving component [kgm²] | Output Equivalent Inertia [kg·m²] |
| | Power Consumed [kg·m²] |

Constants:

axl1_gear_ratio:

Axle Gear Ratio (Output Gear Radius/Input Gear Radius) []

axl1 J1:

Axle Inertia at input [kg·m²]

axl1_J2:

Axle Inertia at output [kg·m²]

axl1_efficiency:

Axle Efficiency from input to output []

Auxiliary Calculations: None

Mask:

- (1) Axle Module
- (2) AXLE MODULE (SwRI)\n\nT1,N2,J1 <=> T2,N1,J2|Axle Gear Ratio []|Axle Efficiency []|Axle Input Gear Inertia [kg*m2]|Axle Output Gear Inertia [kg*m2]
- (3) gear_ratio = @1;efficiency = @2;ingear_inertia = @3;outgear_inertia = @4

Assumptions: See Section 7.2.

8.0 MISCELLANEOUS LIBRARY

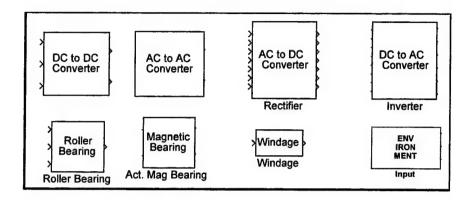


Figure 31. Miscellaneous Components Library

This library contains electrical couplings that convert electrical power between separate buses. These couplings include variations in voltage and account for power transfer inefficiencies. Other bearing models such as roller and magnetic bearings are also included in this library.

8.1 DC-DC Converter



| INPUTS | OUTPUTS |
|--------------------------------|-----------------------|
| High Voltage Power Command (W) | High Side Current (A) |
| High Voltage (V) | Low Side Current (A) |
| Low Voltage (V) | |

Purpose:

The DC-DC Converter block models a solid state converter that inverts, transforms, and rectifies electricity between two DC buses. This model is a simple power transformer with efficiency that accounts for the direction of power flow. The frequency of the inverted power is assumed to be high to reduce ripple effects on the DC bus with small capacitors. The power required to be moved from the high voltage bus to the low voltage bus is input as a function of time, and the model determines the associated DC currents on each bus. Note the

sign convention on the currents and power variables. The controller that supplies the power signal in watts must insure that the bus voltages are within desired ranges. Note that the currents are determined to conserve power, and may become large as voltages are decreased by this and other load paths.

Parameters:

dcdc1 eff

Efficiency of DC/DC Converter (0-1)

Auxiliary Calculations: None

DC-DC Mask

- (1) DC to DC Converter
- (2) DC to DC Converter Block Definitions\n(Click on "Help" to list Inport and Outport parameters.)|Efficiency (0-1)
- (3) eff=@1;
- (4) DC to DC\nConverter
- (5) DC to DC Converter Block Port Parameters\n\nInport 1: High Voltage Power Command (W).\nInport 2: High Voltage (V).\nInport 3: Low Voltage (V).\n\n Outport 1: High Side Current (A).\nOutport 2: Low Side Current (A).

Model Equations:

$$I_{hi} = P_{hi}/V_{hi}$$

 $I_{hi} = P_{hi}/V_{hi}$ $I_{hi} > 0$ is current into the converter

$$I_{lo} = I_{hi} * \eta$$

 $I_{lo} = I_{hi} * \eta \qquad \qquad \text{when } P > 0 \text{ (power flows from hi to lo voltage)} \\ I_{hi} * (1/\eta) \qquad \qquad \text{when } P < 0$

note that I_{lo}>0 represents current flow **out** of the converter

8.2 AC-AC Converter



| INPUTS | OUTPUTS |
|--------------------------------|---------------------------|
| High Voltage Power Command (W) | High Side Current (A_rms) |
| High Voltage (Vrms_II) | Low Side Current (A_rms) |
| Low Voltage (Vrms_II) | |

Purpose:

The AC-AC Converter block models a solid state or conventional iron transformer for changing the voltage between two AC buses. This model is a simple power transformer with efficiency, which accounts for the direction of power flow. It follows the same convention used in the DC-DC converter. The power required to be moved from the high voltage bus to the low voltage bus is input as a function of time, and the model determines the associated DC currents on each bus. Note the sign convention on the currents and power variables. The controller, which supplies the power signal in watts, must insure that the bus voltages are within desired ranges. Note that the currents are determined to conserve power and may become large as voltages are decreased by both this and other load paths. The power transferred through this model assumes that both buses are at a Power Factor of 1. Later modifications could allow for more detailed treatment of not PF=1 conditions.

Parameters:

aca eff

Efficiency of AC/AC Converter (0-1)

Auxiliary Calculations: None

AC-AC Mask

- (1) AC to AC Converter
- (2) AC to AC Converter Block Definitions\n(Click on "Help" to list Inport and Outport parameters.)|Efficiency (0-1)

- (3) eff=@1;
- (4) AC to AC\nConverter
- (5) AC to AC Converter Block Port Parameters\n\nInport 1: High Voltage Power Command (W)\nInport 2: High Voltage (Vrms_ll).\nInport 3: Low Voltage (Vrms_ll).\n\nOutport 1: High Side Current (A_rms).\nOutport 2: Low Side Current (A rms).

Model Equations:

$$I_{bi} = P_{bi}/(sqrt(3)*V_{bi})$$

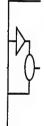
 $I_{hi} = P_{hi}/(sqrt(3)*V_{hi})$ $I_{hi} > 0$ is current **into** the converter

$$I_{lo} = I_{hi} * \eta$$

 $I_{lo} = I_{hi} * \eta \qquad \qquad \text{when } P > 0 \text{ (power flows from hi to lo voltage)} \\ I_{hi} * (1/\eta) \qquad \qquad \text{when } P < 0$

■ note that I_{lo}>0 represents current flow **out** of the converter

8.3 AC-DC converter



| INDUTO | |
|---|--|
| INPUTS | OUTPUTS |
| Input DC Bus Voltage [Volts] | Output DC Bus Voltage [Volts] |
| Magnetizing Per Unitized Current [] | Output Magnetizing Per Unitized Current [] |
| Per Unitized Stator Current along q axis [] | Output Per Unitized Stator Current along q axis [] |
| Per Unitized Stator Voltage along q axis [] | Output Per Unitized Stator Voltage along q axis [] |
| Per Unitized Stator Current along d axis [] | Output Per Unitized Stator Current along d axis [] |
| Per Unitized Stator Voltage along d axis [] | Output Per Unitized Stator Voltage along d axis [] |

Auxiliary Calculations: None

Mask: None

Assumptions:

- The buck rectifier type is valid for simulations that require positive DC rectifier command.
- Rectifier harmonic effects are not modeled.
- The rectifier is assumed to have a fixed, user-definable efficiency.

8.4 DC-AC Converter

SS Boot Ine



| INPUTS | OUTPUTS |
|--|---|
| Input Bus DC Voltage [Volts] | Output Per Unitized Stator Voltage in the q axis [] |
| Per Unitized Synchronous magnetic field speed [] | Output Per Unitized Stator Current in the q axis [] |
| Per Unitized Stator Voltage in the q axis [] | Output Per Unitized Stator Voltage in the d axis [] |
| Per Unitized Stator Current in the q axis [] | Output Per Unitized Stator Current in the d axis |
| Per Unitized Stator Voltage in the d axis [] | Output Per Unitized Rotor Current in the q axis [] |
| Per Unitized Stator Current in the d axis [] | Output Per Unitized Rotor Current in the d axis [] |
| Per Unitized rotor Current in the q axis [] | |
| Per Unitized rotor Current in the d axis [] | |

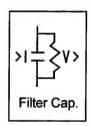
Auxiliary Calculations: None

Mask: None

Assumptions:

- The model is a fully controlled boost inverter.
- The model does not include inverter harmonic effects.

8.5 Capacitor



| INPUTS | OUTPUTS |
|-------------|-------------|
| Current (A) | Voltage (V) |

Purpose: To model a parallel capacitor and resistor.

Parameters:

CM_Cap

Capacitance (F)

CM_Res

Self-Discharge Resistance (Ohms)

 CM_V

Initial Voltage (V)

Auxiliary Calculations: None

Capacitor Module Mask

(1) Capacitor Module

(2) Capacitor Module Capacitance [F] Self-Discharge Resistance [Ohms] Initial Voltage [V]

(3) Capacitance=@1;Resistance=@2;Initial_Voltage=@3;

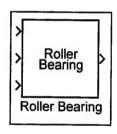
(4) Drawing Commands

(5) Input is Current in Amps\n Output is Voltage in Volts

Model Equations:

$$I - \frac{V}{R} = C \frac{dV}{dt}$$

8.6 Roller Bearing



| INPUTS | OUTPUTS |
|---------------------|--------------|
| Radial Force (N) | Torque (N-m) |
| Thrust Force (N) | |
| Bearing Speed (RPM) | |

Purpose:

To models a roller bearing. Drag torque is calculated based on thrust load, radial load, and viscous drag. An example follows showing extraction of parameters from typical manufacturer's data.

Parameters:

RB_rad Radial Load Coefficients [Tr (N-m), Fro (N), Er (Exponent)]
RB_thr Thrust Load Coefficients [Tt (N-m), Fto (N), Et (Exponent)]
RB_vis Viscous Drag Coefficients [Tv (N-m), No (RPM), Ev (Exponent)]

Auxiliary Calculations: None

Roller Bearing Mask

- (1) Roller Bearing
- (2) T = Tr*(Fr/Fro)^Er \n + Tt*(Ft/Fto)^Et\n + Tv*(N/No)^Ev|Radial Coefficients[Tr(N-m), Fro(Force), Er(Exponent)]|Thrust Coefficients[Tt(N-m), Fto(Force), Et(Exponent)]|Viscous Coefficients[Tv(N-m), No(RPM), Ev(Exponent)]
- (3) RE=@1(3);RK=@1(1)/@1(2)^RE;AE=@2(3);AK=@2(1)/@2(2)^AE; VE=@3(3);VK=@3(1)/@3(2)^VE;
- (4) Roller\nBearing
- (5) This bearing model calculates the drag due to normal ball bearings. Normally radial and thrust exponents (Er & Et) are near 1.5, viscous exponent (Ev) is usually 2/3. Model uses the absolute value of the input forces and speed for calculations.\n\nInput 1 is Radial Force (Fr)\nInput 2 is Thrust Force (Ft)\nInput 3 is Speed (N)\n\nOutput is Bearing Drag in N-m

Model Equations:

$$\tau = \tau_{l} \left(\frac{F_{r}}{F_{ro}} \right)^{E_{r}} + \tau_{l} \left(\frac{F_{l}}{F_{lo}} \right)^{E_{l}} + \tau_{v} \left(\frac{N}{N_{o}} \right)^{E_{v}}$$

Example of Extraction of Inputs from Manufacturers Data

| | Table 13. Typical Manufacturer's Data | | | | |
|--------------|---------------------------------------|--------------|---------------|-------------|-------------|
| Radial Force | Radial Torque | Thrust Force | Thrust Torque | Rotor Speed | Lube Torque |
| (lbs) | (N-m) | (lbs) | (N-m) | (RPM) | (N-m) |
| 40 | 0.0013 | | 0.0042 | 1000 | 0.0962 |
| 50 | 0.0018 | | 0.0058 | 2000 | 0.1528 |
| 70 | 0.0030 | | 0.0092 | 4000 | 0.2425 |
| 100 | 0.0051 | | 0.0153 | 6000 | 0.3178 |
| 130 | 0.0075 | | 0.0222 | 8000 | 0.3850 |
| 180 | 0.0121 | | 0.0352 | 12000 | 0.5045 |
| 240 | 0.0185 | | 0.0527 | 16000 | 0.6111 |
| 350 | 0.0326 | | 0.0895 | | |
| 450 | 0.0472 | | 0.1271 | | |
| 600 | 0.0729 | | 0.1897 | | |
| 820 | 0.1172 | | 0.2923 | | |
| 1100 | 0.1832 | | 0.4380 | | |

Choose Nominal Force of 100 lbs, Maximum of 1100 lbs and Speed=16000 RPM

$$F_{ro}=100 \text{ lbs}$$
 $T_{ro}=.0051 \text{ N-m}$

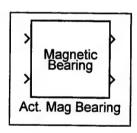
$$E_r = \frac{\ln(T_{\text{max}}/T_{ro})}{\ln(F_{\text{max}}/F_{ro})} = \frac{\ln(.1832/.0051)}{\ln(1100/100)} = 1.49$$

$$F_{to} = 100 \text{ lbs}$$
 $T_{to} = .0153 \text{ N-m}$

$$E_t = \frac{\ln(T_{\text{max}}/T_{to})}{\ln(F_{\text{max}}/F_{to})} = \frac{\ln(.438/.0153)}{\ln(1100/100)} = 1.40$$

$$E_{\nu} = \frac{\ln(T_1/T_{\nu})}{\ln(N_1/N_{\rho})} = \frac{\ln(.2425/.611)}{\ln(4/16)} = .667$$

8.7 Magnetic Bearing



| INPUTS | OUTPUTS |
|-------------|--------------------|
| Force (N) | Electric Power (W) |
| Speed (RPM) | Drag Torque (N-m) |

Purpose:

The magnetic bearing approximately models an active magnetic bearing. Bearings are assumed to have a defined relationship between air gap flux and force. This model linearly interpolates the electric losses and rotating losses for the given input force at the base speed. The rotating losses are assumed to be due to eddy current and hysteresis losses in the magnetic core of the rotor. The eddy current losses will be proportional to speed squared,

while the hysteresis losses will be proportional to the speed. This allows scaling for speed variations of these rotating torques to account for speed effects.

Parameters:

MB_F Vector of Input Forces (N)
MB_elc_loss Vector of Electric Losses (W)

MB_rot_loss Vector of Hysteresis Rotational Losses (W) at Base Speed MB_cur_rot_loss Vector of Eddy Current Rotational Losses (W) at Base Speed

MB spd Base Speed (RPM)

Auxiliary Calculations: None

Magnetic Bearing Mask

(1) Mag Bearing

- (2) Active Magnetic Bearing Model|Input Force|Electric Losses (W)|Hysteresis Rotational Losses (W) at Base Speed|Eddy Current Rotational Losses (W) at Base Speed|Base Speed (RPM)
- (3) Input=@1;Electric=@2;Hysteresis=@3/@5*30/pi;Eddy=@4/@5/@5*30/pi;
- (4) Magnetic\nBearing
- (5) All losses are calculated as curve fits as a function of input force. Electric power is assumed independent of speed. Hysteresis losses are assumed to increase linearly with speed. Eddy current losses are assumed to increase as the speed squared. Hysteresis and eddy current losses appear as mechanical drag torque.\n\nInput 1 is Force\nInput 2 is Speed in RPM\n\nOutput 1 is Electric Power Draw in Watts\nOutput 2 is Drag Torque in N-m

Model Equations:

$$E_F = Fit (F, P_{eddy}, F_{in})$$

$$\tau \omega = H_{F} \left(\frac{N}{N_{o}} \right) + E_{F} \left(\frac{N}{N_{o}} \right)^{2}$$

where

Pout is the required electrical power

 τ is the drag torque

F is the input force

N is the input rotational speed

Fin is the array specified in the mask under 'Input Force'

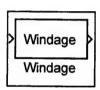
Pelect is the array specified in the mask under 'Electric Losses...'

Physt is the array specified in the mask under 'Hysteresis...'

Peddy is the array specified in the mask under 'Eddy Current...'

Fit(V,Y,X) is a linear interpolation of the 'Y' vs. 'X' data at x value 'V'

8.8 Windage



| INPUTS | OUTPUTS |
|-------------|-------------------|
| Speed (RPM) | Drag Torque (N-m) |

Purpose: To calculate windage as a function of speed for a constant vacuum pressure.

Parameters:

W_spd

Base Speed (RPM)

W drag spd

Drag at Base Speed (W)

W De

Speed Exponent for Drag Power

Auxiliary Calculations: None

Windage Mask:

- (1) Windage Module
- (2) Windage Equation\nP=Po(N/No)^De|Base Speed (RPM) [No]|Drag at Base Speed (W) [Po]|Speed Exponent for Drag Power [De]
- (3) Drag_Const=@2*30/pi/(@1^@3);Drag_Exp=@3-1;
- (4) Windage
- (5) Models rotor windage assuming a constant vacuum level. The exponent (De) will normally vary from De=2 at reasonable vacuum (<.001 torr) to De=3 at poor vacuum (>1 torr).\n\nInput is speed in RPM\nOutput is drag torque in N-m

Model Equations:

$$\tau \omega = P_o \left(\frac{N}{N_o}\right)^{De}$$

8.9 Driving Profile



| INPUTS | OUTPUTS |
|--------|----------------|
| | Driving cycle |
| | Road Gradient |
| | Head Wind data |

The driving profile model provides the environmental/operating inputs to the simulation. These are: driving cycle in which vehicle velocity is described as a function of time, road gradient, and head-wind information as a function of time.

Auxiliary Calculations: None

Mask: None

Assumptions: Application dependent

9.0 LIST OF ALL VARIABLES

| Table 14. Motor Wheel Coupling | | | |
|--------------------------------|------------------------------------|------------------|--------|
| Variable | Description | Units | Type |
| axl1_J1 | Inertia at input side of coupling | kgm ² | Scalar |
| axl1_J2 | Inertia at output side of coupling | kgm ² | Scalar |
| axl1_efficiency | Coupling efficiency | - | Scalar |
| axl1_gear_ratio | Coupling gear ratio | - | Scalar |
| axl1_mass | Mass of coupling | kg | Scalar |
| axl1_name | Name of coupling | - | Scalar |
| axl1_weight | Weight of coupling | N | Scalar |
| shft_log_name | Name of coupling shift logic | - | Scalar |

| Table 15. Constants | | | |
|---------------------|--|-------|--------|
| Variable | Description | Units | Туре |
| c_bar_Pa | Conversion factor from bar to Pascal | - | Scalar |
| c_ft_m | Conversion factor from ft to m | - | Scalar |
| c_hp_kW | Conversion factor from hp to kW | - | Scalar |
| c_in3_m3 | Conversion factor from in ³ to m ³ | - | Scalar |
| c_inHg_Pa | Conversion factor from in Hg to Pascal | - | Scalar |
| c_in_m | Conversion factor from in to m | - | Scalar |
| c_kPa_Pa | Conversion factor from kPa to Pa | - | Scalar |
| c_lb_kg | Conversion factor from lb-mass to kg | 1- | Scalar |
| c_lbf_N | Conversion factor from lb-force to N | T- | Scalar |
| c_lbft_Nm | Conversion factor from ft-lb to Nm | - | Scalar |
| c_lbft2_kgm2 | Conversion factor from lb-mass ft ² to kgm ² | - | Scalar |
| c_lbphphr_kgpkWhr | Conversion factor from lb per hp hr to kg per kWhr | - | Scalar |
| c_liter_m3 | Conversion factor from liter to m ³ | 1 | Scalar |
| c_psi_Pa | Conversion factor from psi to Pa | - | Scalar |
| c_rpm_radps | Conversion factor from rpm to rad per sec | - | Scalar |

| Table 16. Engine-Generator Coupling | | | |
|-------------------------------------|----------------|-------|--------|
| Variable | Description | Units | Type |
| cpl1_speed_ratio | Coupling ratio | - | Scalar |

| Variable | Description | Units | Type |
|------------|---|----------|--------------|
| cycle | Table of time (first column in sec) versus desired speed (second column in m/s) | | Vector (Nx2) |
| cycle_name | Name of driving cycle | — | Scalar |
| road_grade | Gradient of road | rad | Scalar |

| Table 18. Driver | | | |
|-------------------|--|-------|--------|
| Variable | Description | Units | Туре |
| dvr1_name | Name of driver | - | Scalar |
| dvr1_weight | Driver weight | N | Scalar |
| dvr_deriv_gain | Derivative gain of driver PID controller | - | Scalar |
| dvr_integral_gain | Integral gain of driver PID controller | - | Scalar |
| dvr_proport_gain | Proportional gain of driver PID controller | - | Scalar |

| Table 19. Spark Ignition Engine | | | |
|---------------------------------|--|----------------|--------------|
| Variable | Description | Units | Туре |
| eng1_cat_cnvtr_name | Engine catalic converter | - | scalar |
| eng1_cat_cnvtr_weight | Engine catalic converter weight | N | scalar |
| eng1_fuel_HV | Engine fuel heat value | J/kg | scalar |
| eng1_fuel_density | Engine fuel density | kg/l | scalar |
| eng1_fuel_weight | Engine fuel weight | N | scalar |
| eng1_name | Engine name | - | scalar |
| eng1_weight | Engine weight | N | scalar |
| eng_af_ratio_Pi | Vector of intake manifold pressure for air fuel ratio | Pa | vector (1x3) |
| eng_af_ratio_speed | Vector of engine speed for air fuel ratio | rad/sec | vector (1x2) |
| eng_af_ratio_table | Engine air fuel ratio table | - | Matrix (2x3) |
| eng_ambient_air_density | Engine ambient air density | kg/m³ | scalar |
| eng_ambient_pressure | Engine ambient pressure | Pa | scalar |
| eng_ambient_temperature | Engine ambient temperature | K | scalar |
| eng_catalyst_eff_CO | Catalyst conversion efficiency for carbon monoxide | - | scalar |
| eng_catalyst_eff_HC | Catalyst conversion efficiency for hydro carbons | - | scalar |
| eng_catalyst_eff_NO | Catalyst conversion efficiency for nitrogen oxides | - | scalar |
| eng_catalyst_eff_PM | Catalyst conversion efficiency for particulate matter | - | scalar |
| eng_compression_ratio | Engine compression ratio | - | scalar |
| eng_displacement | Engine displacement | m ³ | scalar |
| eng_emissions_CO_table | Table of engine emissions for carbon monoxide | kg/kg fuel | Matrix (5x5) |
| eng_emissions_HC_table | Table of engine emissions for hydro carbons | kg/kg fuel | Matrix (5x5) |
| eng_emissions_NOx_table | Table of engine emissions for nitrogen oxides | kg/kg fuel | Matrix (5x5) |
| eng_emissions_PM_table | Table of engine emissions for particulate matter | kg/kg fuel | Matrix (5x5) |
| eng_emissions_Pi | Vector of intake manifold pressure | Pa | Vector (1x5) |
| eng_emissions_speed | Vector of engine speed for different emissions | rad/sec | Vector (1x5) |
| eng_exh_pres_scaling | Scaling factor for matching exhaust pressure | | scalar |
| eng_exh_temp_Pi | Vector of intake manifold pressure for exhaust temperature | Pa | vector (1x2) |
| eng_exh_temp_af_coeff | Engine exhaust temperature to air | - | scalar |

| Table 19. Spark Ignition Engine | | | |
|---------------------------------|--|----------------|--------------|
| Variable | Description | Units | Туре |
| | fuel ratio coefficient | | |
| eng_exh_temp_speed | Vector of engine speed for exhaust | rad/sec | vector (1x2) |
| | temperature | | 10000 (1702) |
| eng_exh_temp_table | Exhaust temperature table | K | Matrix (2x2) |
| eng_fmep_factor_0 | Correlation factor 0 for friction mean | - | scalar |
| | effective pressure | | 332 |
| eng_fmep_factor_1 | Correlation factor 1 for friction mean | - | scalar |
| | effective pressure | | |
| eng_fmep_factor_2 | Correlation factor 2 for friction mean | - | scalar |
| | effective pressure | | |
| eng_fuel_evaporation_time_co | Time constant for fuel evaporation in | sec | scalar |
| nstant | intake manifold wall | | |
| eng_gas_const_air | Specific gas constant for air | J/kg/K | scalar |
| eng_gas_const_exhaust | Specific gas constant for exhaust | J/kg/K | scalar |
| | gases | | |
| eng_inertia | Engine rotary inertia | kgm² | scalar |
| eng_liquid_fuel_fraction | Fraction of fuel that stays in liquid | - | scalar |
| | form | | |
| eng_manifold_volume | Engine intake manifold volume | m ³ | scalar |
| eng_max_air_flow | Engine max air flow | kg/s | scalar |
| eng_mol_wt_air | Molecular weight of air through | kg/kmol | scalar |
| | throttle | " | |
| eng_mol_wt_exhaust | Molecular weight of exhaust gases | kg/kmol | scalar |
| eng_muffler_pressure_factor | Engine muffler pressure correlation | - | scalar |
| | factor | | |
| eng_nominal_isfc | Engine nominal indicated specific | kg/J | scalar |
| | fuel consumption | | |
| eng_off_torque_fact | Factor for torque when engine is off | Nm/rad/ | scalar |
| | | s | |
| eng_rated_air_mass_flow | Rated air mass flow for engine | kg/s | scalar |
| eng_rated_air_vol_flow | Rated air volume flow for engine | m³/s | scalar |
| eng_rated_bmep | Rated Brake Mean Effective | Pa | scalar |
| | Pressure | | |
| eng_rated_exhaust_density | Rated exhaust air density | kg/m³ | scalar |
| eng_rated_exhaust_pressure | Rated exhaust gas pressure | | scalar |
| eng_rated_exhaust_temperatu | Rated exhaust gas temperature | | scalar |
| re | | | |
| eng_rated_intake_vacuum | Intake manifold vacuum at rated | Pa | scalar |
| | conditions | | |
| eng_rated_power | Rated engine power | Watts | scalar |
| eng_rated_pres_ratio_infl | Pressure ratio influence factor (in | - | scalar |
| | flow equation) at rated conditions | | |
| ong roted cross | [fraction] | | |
| eng_rated_speed | Maximum engine speed | rad/s | scalar |
| eng_rated_torque | Rated engine torque | | scalar |
| eng_rated_vol_eff | Rated engine volumetric efficiency | - | scalar |
| eng_speed_density_weight | Fractional weight for speed density | - | scalar |
| | air flow compared to mass flow | | |
| eng_std_air_density | sensor [fraction] | 1(3 | |
| ong_otd_dii_deliaity | Density of standard air | kg/m³ | scalar |

| Table 19. Spark Ignition Engine | | | | |
|---------------------------------|--|----------|--------------|--|
| Variable | Description | Units | Туре | |
| eng_std_pres | Standard pressure | Pa | scalar | |
| eng_std_temp | Standard temperature | K | scalar | |
| eng_stoich_af_ratio | Correlation factor for effect of air fuel ratio on exhaust temperature | - | scalar | |
| eng_throttle_bypass_ratio | Ratio of bypass flow area around throttle to total throttle area | - | | |
| eng_universal_gas_const | Universal gas constant | J/kmol/K | scalar | |
| eng_vol_eff_Pi | Table of intake manifold pressure vs. vol efficiency | Pa | Vector (1x2) | |
| eng_vol_eff_speed | Table of engine speed for vol efficiency | rad/s | Vector (1x6) | |
| eng_vol_eff_table | Table of engine volumetric efficiencies | - | Matrix (6x2) | |

| Table 20. Lead Acid Battery | | | |
|-----------------------------|---|-------|--------|
| Variable | Description | Units | Type |
| essb1_name | Battery name | - | scalar |
| essb1_weight | Battery weight | N | scalar |
| essb_C | Internal capacitance of a cell | F | scalar |
| essb_C5 | Discharge capacity @ 5 hour rate at 30 Celsius for a cell | A-hr | scalar |
| essb_CT | Terminal capacitance | F | scalar |
| essb_E | Open circuit voltage of a cell | V | scalar |
| essb_l5 | Discharge current @ 5 hour rate for a cell | Α | scalar |
| essb_K | Polarization resistance of a cell | Ω | scalar |
| essb_Q0 | Initial charge in battery cell | A-hr | scalar |
| essb_Rb | Terminal resistance for the battery | Ω | scalar |
| essb_chrg_eff | Battery charge efficiency | - | scalar |
| essb_dischrg_eff | Battery discharge efficiency | - | scalar |
| essb_init_ECP | Battery initial polarization voltage | V | scalar |
| essb_init_SOC | Battery initial state of charge | 1- | scalar |
| essb_r | Internal resistance of a cell | Ω | scalar |
| essb_tot_num | Total number of batteries | - | scalar |

| Table 21. Permanent Magnet Generator | | | |
|--------------------------------------|---|-------|--------|
| Variable | Description | Units | Type |
| genp1_ctrl_dgain | Derivative gain of PID controller for generator | - | scalar |
| genp1_ctrl_igain | Integral gain of PID controller for generator | - | scalar |
| genp1_ctrl_pgain | Proportional gain of PID controller for generator | - | scalar |
| genp1_ctrlr_name | Generator controller name | - | scalar |
| genp1_ctrlr_weight | Generator controller weight | N | scalar |
| genp1_name | Generator name | - | scalar |
| genp1_weight | Generator weight | N | scalar |

| Table 22. AC Induction Motor | | | | |
|------------------------------|------------------------------|-------|--------|--|
| Variable | Description | Units | Туре | |
| moti1_ctrlr_name | Motor controller name | - | scalar | |
| motl1_ctrlr_weight | Motor controller weight | N | scalar | |
| motl1_name | Motor name | - | scalar | |
| motl1_weight | Motor weight | N | scalar | |
| motor_N_max | Maximum rated speed of motor | rpm | scalar | |

| Table 23. Simulation Constants | | | |
|--------------------------------|--|-------|--------|
| Variable | Description | Units | Type |
| sample_N | Number of samples to save to workspace | - | scalar |
| sample_T | Time step length between saved samples | - | scalar |

| Table 24. Vehicles | | | | |
|---------------------------|---|-------------------|--------|--|
| Variable | Description | Units | Type | |
| veh1_aero_drag_coef | Aerodynamic drag coefficient | - | scalar | |
| veh1_air_density | Air density | kg/m ³ | scalar | |
| veh1_chassis_weight | Chassis Weight | N | scalar | |
| veh1_coef_yaw_sens | Coefficient of sensitivity to yaw | - | scalar | |
| veh1_f0 | Vehicle speed independent rolling coefficient | - | scalar | |
| veh1_front_area | Frontal area of vehicle | m ² | scalar | |
| veh1_fs | Vehicle speed dependent rolling coefficient | - | scalar | |
| veh1_mass | Vehicle mass | kg | scalar | |
| veh1_name | Vehicle name | - | scalar | |
| veh1_normal_wind | Wind velocity normal to vehicle motion | m/s | scalar | |
| veh1_parallel_wind | Head wind velocity | m/s | scalar | |
| veh1_passengers_weight | Passenger weight | N | scalar | |
| veh1_roadtire_frict_coeff | Road tire coefficient of friction | - | scalar | |

| Table 25. Miscellaneous | | | | |
|-------------------------|----------------------|-------|--------|--|
| Variable | Description | Units | Type | |
| weight_total | Total vehicle weight | N | scalar | |

| Table 26. Wheel | | | |
|-----------------|--------------|-------|--------|
| Variable | Description | Units | Туре |
| whi1_mass | Wheel mass | kg | scalar |
| whl1_radius | Wheel radius | m | scalar |
| whl1_tr | Wheel radius | m | scalar |

N: Length of the time (sim_time) vector

HYBRID ELECTRIC VEHICLE SIMULINK TOOLBOX

(Commercial Vehicle Version)

Technical Notes

Version 1.1

1.0 INTRODUCTION

These technical notes provide the equations used within the individual modules of the DARPA Hybrid Electric Vehicle (HEV) simulation toolbox, hereinafter referred to as PATHS (Performance Assessment Toolbox for Hybrid Systems). These technical notes accompany the User's Guide for the HEV simulation toolbox. Use of PATHS is restricted to government-funded projects, following explicit permission by DARPA/SwRI only. All inquiries to obtain permission to use PATHS must be directed to Dr. A. Nedungadi at Southwest Research Institute (210-522-3965).

PATHS is developed under the MATLAB/SIMULINK[©] environment, and is provided to users in source code form. An experienced MATLAB/SIMULINK[©] user can easily trace the inputs to the outputs and determine the transfer function between these two. The following notes provide the user with the basic principles of physics that have been employed to model the individual modules of PATHS. Modules that use table lookup methods are not described in this document, since these are not based on principles of physics. Cursory equations describing the internal operation within certain modules are provided in the User's Guide. In this case, the user is referred to the User's Guide for information on the underlying technical equations. All equations of controller modules of the controllers library (refer to User's Guide) have been omitted since these are based on classical PID control laws. As a result, this document contains technical equations for the following modules, which is a subset of the entire PATHS software (please refer to the User's Guide for a complete listing of all modules of PATHS):

ELECTRIC MACHINE LIBRARY

| Ш | AC induction steady state motor |
|---|---|
| | Permanent magnet steady state generator |
| | AC Induction dynamic motor |
| | Permanent magnet dynamic generator |

| ENERGY STORAGE LIBRARY |
|--|
| Lead acid battery |
| flywheel battery |
| Capacitor |
| |
| VEHICLE LIBRARY |
| Wheeled vehicle (version 1 and 2) |
| Wheel (version 1 and 2) |
| |
| COUPLINGS LIBRARY |
| Gear box |
| Engine-generator coupling |
| ☐ Motor-wheel coupling (version 1 and 2) |
| |
| MISCELLANEOUS LIBRARY |
| Roller bearing |
| Magnetic bearing |
| ☐ Windage model |

2.0 ELECTRIC MACHINE LIBRARY

2.1 Steady State AC Induction Motor

Figure 32 shows the inputs and outputs of the steady-state induction motor model - motI1_module. Figure 33 depicts the per-phase equivalent circuit model of the induction machine and defines the motor parameters. Figure 34 shows the induction motor model after the transformation to the synchronous d-q reference frame. The electrical terminal voltages and currents are calculated directly from this equivalent circuit and the mechanical equations using the command values of torque and speed. The synchronous reference frame electrical and mechanical equations used in the simulation are,

$$\begin{aligned} v_{qs}^e &= R_s i_{qs}^e + \omega \lambda_{ds}^e \\ v_{ds}^e &= R_s i_{ds}^e - \omega \lambda_{qs}^e \\ 0 &= R_r i_{qr}^e + (\omega - \omega_r) \lambda_{dr}^e \\ 0 &= R_r i_{dr}^e - (\omega - \omega_r) \lambda_{qr}^e \\ \lambda_{qs}^e &= (L_m + L_{ls}) i_{qs}^e + L_m i_{qr}^e \\ \lambda_{ds}^e &= (L_m + L_{lr}) i_{ds}^e + L_m i_{dr}^e \\ \lambda_{qr}^e &= (L_m + L_{lr}) i_{qr}^e + L_m i_{qs}^e \\ \lambda_{dr}^e &= (L_m + L_{lr}) i_{dr}^e + L_m i_{ds}^e \end{aligned}$$

where the e superscript denotes the synchronous reference frame.

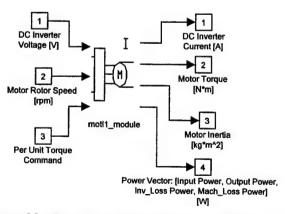


Figure 32. Inputs and Outputs of motI1_module

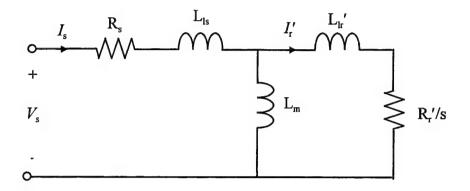


Figure 33. Induction Machine Per Phase Equivalent Circuit

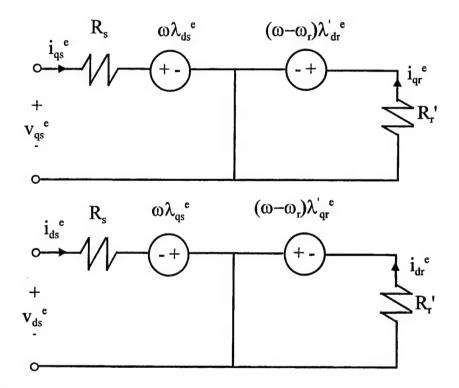


Figure 34. Steady-state dq equivalent circuit of an induction motor

The motor is controlled using conventional rotor flux field orientation (i.e., "brushless de" control) such that in the synchronous reference frame, $\lambda_{qr}^{\ \ e} = 0$.

2.2 Steady State Permanent Magnet Generator

Figure 35 shows the inputs and outputs of the steady-state generator model - genp1_module. Figure 36 depicts the steady-state synchronous d-q reference frame model used in the simulation. The electrical terminal voltage is calculated directly from this equivalent circuit using the command values of current and speed. The electrical and mechanical equations used in the simulation, and given by the equivalent circuit, are,

$$\begin{split} i_{qs}^{e} &= i_{qm}^{e} + \frac{1}{R_{m}} (\omega_{r} L_{ds} i_{dm}^{e} - \omega_{r} L_{md} I_{df}) \\ i_{ds}^{e} &= i_{dm}^{e} - \frac{\omega_{r} L_{qs} i_{qm}^{e}}{R_{m}} \\ v_{qs}^{e} &= -R_{s} i_{qs}^{e} + \omega_{r} L_{md} I_{df} - \omega_{r} L_{ds} i_{dm}^{e} \\ v_{ds}^{e} &= -R_{s} i_{ds}^{e} + \omega_{r} L_{qs} i_{qm}^{e} \\ \tau &= L_{md} I_{df} i_{qm}^{e} \end{split}$$

where the superscript e denotes the synchronous reference frame, and I_{df} is the fictitious current, which corresponds to the strength of the permanent magnet. This current is internally calculated from the no load speed and voltage. The iron loss resistor, R_m , is calculated from the rated core losses value provided by the user.

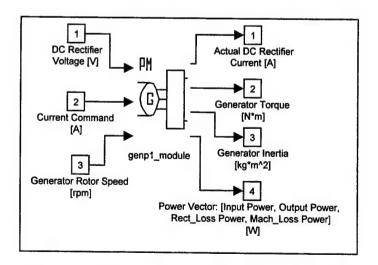


Figure 35. Inputs and Outputs of genp1_module

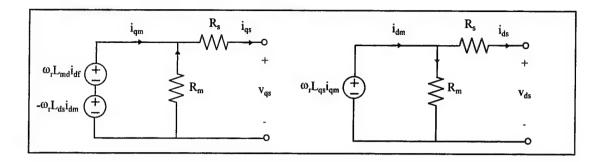


Figure 36. Steady-State dq-Equivalent Circuits

The generator is controlled using conventional synchronous reference frame field orientation (i.e., "brushless dc" control) such that $i_{dm} = 0$.

2.3 AC Induction Dynamic Motor

Figure 37 below shows the inputs and outputs for the induction motor/boost inverter system. The standard steady-state induction machine, per-phase equivalent circuit is shown in the previous section. Please refer to this section for information about what each resistance or inductance referenced in the mask relates to electrically.

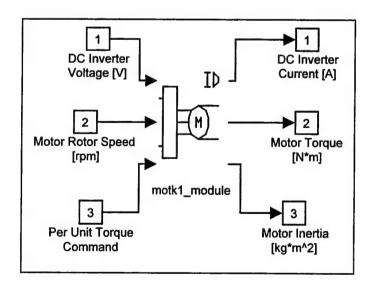


Figure 37. Inputs and Outputs of motk1_module

Figure 38 depicts the synchronous reference frame d-q dynamic model of the induction machine and defines the motor parameters. The electrical terminal voltages and currents are calculated directly from this equivalent circuit and the mechanical equations using the command values of torque and speed. The synchronous reference frame electrical and mechanical equations used in the simulation are,

$$v_{qs}^{e} = R_{s}i_{qs}^{e} + \omega \lambda_{ds}^{e} + \stackrel{\checkmark}{\lambda_{qs}^{e}}$$

$$v_{ds}^{e} = R_{s}i_{ds}^{e} - \omega \lambda_{qs}^{e} + \stackrel{\checkmark}{\lambda_{ds}^{e}}$$

$$0 = R_{r}i_{qr}^{e} + (\omega - \omega_{r})\lambda_{dr}^{e} + \stackrel{\checkmark}{\lambda_{qr}^{e}}$$

$$0 = R_{r}i_{dr}^{e} - (\omega - \omega_{r})\lambda_{qr}^{e} + \stackrel{\checkmark}{\lambda_{dr}^{e}}$$

$$\lambda_{qs}^{e} = (L_{m} + L_{ls})i_{qs}^{e} + L_{m}i_{qr}^{e}$$

$$\lambda_{ds}^{e} = (L_{m} + L_{ls})i_{ds}^{e} + L_{m}i_{dr}^{e}$$

$$\lambda_{qr}^{e} = (L_{m} + L_{lr})i_{qr}^{e} + L_{m}i_{qs}^{e}$$

$$\lambda_{dr}^{e} = (L_{m} + L_{lr})i_{dr}^{e} + L_{m}i_{qs}^{e}$$

$$\tau = L_{m}(i_{qs}^{e}i_{dr}^{e} - i_{ds}^{e}i_{qr}^{e})$$

where the e superscript in the equations denotes the synchronous reference frame.

The motor is controlled using conventional rotor flux field orientation (i.e., "brushless dc" control) such that in the synchronous reference frame, $\lambda_{qr}^{\ e} = 0$. The stator currents, $i_{qs}^{\ e}$ and $i_{ds}^{\ e}$, are controlled in the synchronous reference frame through a standard PI current regulator. The PI gains are user-definable.

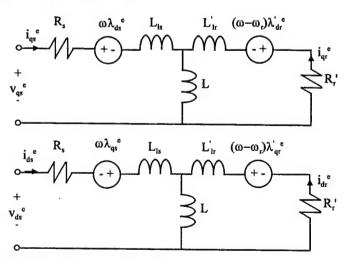


Figure 38. Dynamic dq equivalent circuit of an induction motor

2.4 Permanent Magnet Dynamic

Figure 39 shows the inputs and outputs of the dynamic generator model - genq1_module. Figure 40 depicts the dynamic synchronous d-q reference frame model used in the simulation. The electrical terminal voltage is calculated directly from this equivalent circuit using the command values of current and speed. The electrical and mechanical equations used in the simulation, and given by the equivalent circuit, are,

$$\begin{split} i_{qs}^{e} &= i_{qm}^{e} + \frac{1}{R_{m}} \left(\omega_{r} L_{ds} i_{dm}^{e} - \omega_{r} L_{md} I_{df} + L_{qs} i_{qm}^{\acute{Y}} \right) \\ i_{ds}^{e} &= i_{dm}^{e} - \frac{1}{R_{m}} \left(\omega_{r} L_{qs} i_{qm}^{e} - L_{ds} i_{dm}^{\acute{Y}} \right) \\ v_{qs}^{e} &= -R_{s} i_{qs}^{e} + \omega_{r} L_{md} I_{df} - \omega_{r} L_{ds} i_{dm}^{e} - L_{qs} i_{qm}^{\acute{Y}} \\ v_{ds}^{e} &= -R_{s} i_{ds}^{e} + \omega_{r} L_{qs} i_{qm}^{e} - L_{ds} i_{dm}^{\acute{Y}} \\ \tau &= L_{md} I_{df} i_{qm}^{e} \end{split}$$

where the superscript e denotes the synchronous reference frame, and I_{df} is the fictitious current, which corresponds to the strength of the permanent magnet. This current is internally calculated from the no load speed and voltage. The iron loss resistor, R_m , is calculated from the rated core losses value provided by the user.

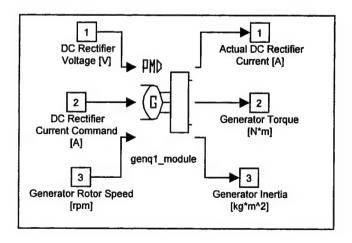


Figure 39. Inputs and Outputs of genq1_module

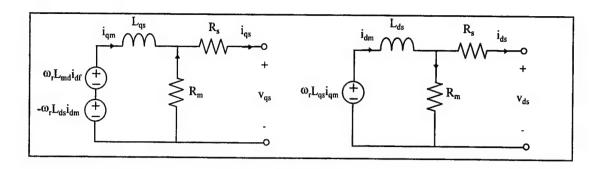


Figure 40. Dynamic Generator dq-Equivalent Circuits

The generator is controlled using conventional synchronous reference frame field orientation (i.e., "brushless dc" control) such that $i_{dm}=0$. The q-axis current, i_{qm} , is controlled in the synchronous reference frame through a standard PI current regulator. The PI gains are user-definable.

3.0 ENERGY STORAGE LIBRARY

3.1 Lead Acid Battery

Figure 41 shows the circuit diagram used to develop the dynamic model of the lead-acid battery. A single battery cell is described by the following parameters:

 $r_i[\Omega]$: Internal resistance of cell i

E_i [V]: Open circuit voltage of cell i

c_i[F]: Capacitance of cell i

 $K_i[\Omega]$: Polarization Resistance of cell i

SOC_i: State of charge of cell I

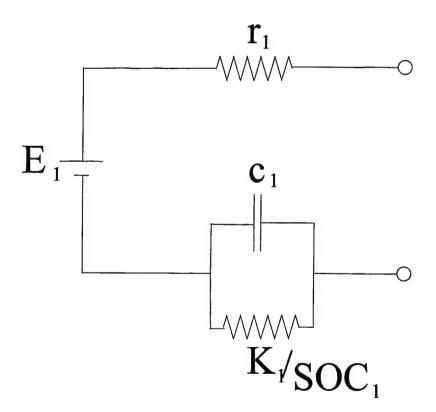


Figure 41. Circuit Diagram for a Single Cell of a Lead Acid

In a battery with multiple cells, the circuit will consist of N single cells in series with a terminal resistance R_T [Ω] and capacitance C_T [F]. Figure 42 shows 2 single cells in series, a terminal resistance R_T [Ω] and capacitance C_T [F]. Positive current I is shown by the direction of the arrow in Figure 41. Referring to Figure 41, and assuming that $c_1 = c_2$, $E_1 = E_2 = E$, $K_1 = K_2$, Kirchoff's voltage law can be formulated as follows:

$$N(Vc) + N(E) + N(I_r r) + I_r R_T = V_T$$
 [1]

where:

Vc: The voltage across the capacitor c_1 [V]

N: The number of cells in the battery []

I_r: The portion of the current I that flows into the internal resistance r [A]

V_T: The terminal voltage [V]

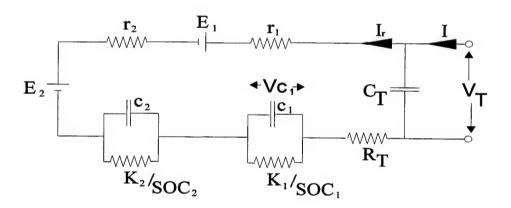


Figure 42. Circuit Diagram for a Lead Acid Battery with Two Cells

The above lead acid battery model has two states: Vc and V_T . Therefore, this is a second order battery model. Assuming, $SOC_1 = SOC_2 = SOC$, the above equation can be combined with Kirchoff's current law to determine these two states as follows:

$$I = C_{T} \frac{dVT}{dt} + I_{r}$$
 [2]

$$Ir = c \frac{dVc}{dt} + \frac{Vc}{K/SOC}$$
 [3]

Solving for Ir in equation (11) and substituting it in equations (12) and (13) yield the following for the two states V_T

$$\frac{dVT}{dt} = \left[I - \frac{(V_T - N(E) - N(Vc))}{N(r) + R_T}\right] \left(\frac{1}{C_T}\right)$$
 [4]

$$\frac{dVc}{dt} = \left\{ \left[\frac{(V_T - N(E) - N(Vc))}{N(r) + R_T} \right] - \frac{Vc}{K_{SOC}} \right\} \frac{1}{c}$$
 [5]

Assuming positive current (charging) is in the direction shown in Figure 41, the state of charge SOC of the battery can be calculated as a function of the battery capacity. The battery capacity can be expressed as a function of temperature and discharge current Id as follows:

$$C(I,T) = C_5 \left(\frac{Id}{I_5}\right)^{-0.325} \left[1 + 0.008(T - 30)\right]$$
 [6]

where:

C₅: Internal battery capacity [A-h]

 I_5 : Discharge current at 5 hour rate for the battery

Id: Discharge current

T: Temperature at which the battery operates [Deg C]

During the discharge, (Id < 0), the SOC can be calculated as follows:

$$\frac{dSOC}{dt} = \frac{100}{C(Id, T)} Id \left(\frac{1}{\eta_d}\right)$$
 [7]

where:

 η_d : Discharge efficiency []

During charge (Ic > 0), the SOC can be calculated as follows:

$$\frac{\text{dSOC}}{\text{dt}} = \frac{(100 - \text{SOC})\eta_c \text{Ic}}{Q}$$
 [8]

where:

η_c: Charge efficiency []

Ic: Charge current [A]

Q: Total Quantity missing in the battery over the entire operating time t

Q is calculated as follows:

$$Q = \left| \int_{0}^{t} I \, dt \right|$$
 [9]

3.2 Flywheel Battery

There are numerous possible flywheel energy storage system configurations. One of these configurations is shown in Figure 43.

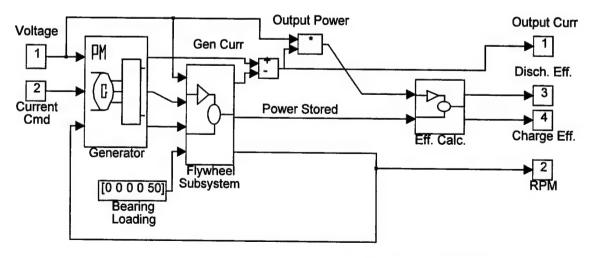


Figure 43. Flywheel Energy Storage System Configuration

Units

Voltage:

Volts

speed:

RPM

current:

Amps

Notes

inputs:

2(voltage, current command)

states:

1+(speed and generator states)

outputs:

4(output current, speed, discharge & charge eff)

direct feedthrough:

There are two major components and one auxiliary component of this system:

1. Motor/Generator and Converter

2. Flywheel

3. Efficiency Calculation

This subsystem uses a permanent magnet generator. The 'Current Command' is the current command provided to the generator controller. The 'Output Current' is the actual current output to the DC Bus. Inputs for the 'Flywheel Subsystem' are the DC voltage, generator torque, generator inertia and bearing loads. The 'Flywheel Subsystem' has outputs of auxiliary current draw, stored mechanical power, and rotor speed.

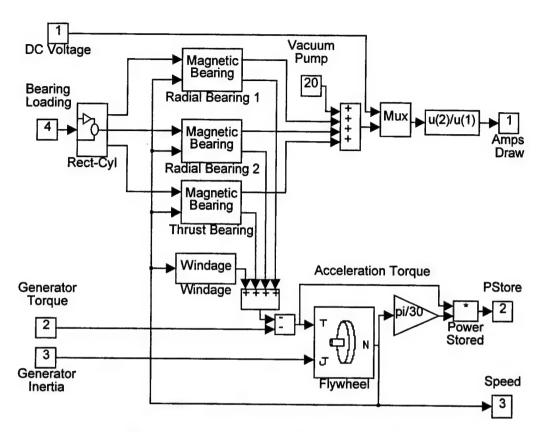


Figure 44. Flywheel Subsystem with Magnetic Bearings

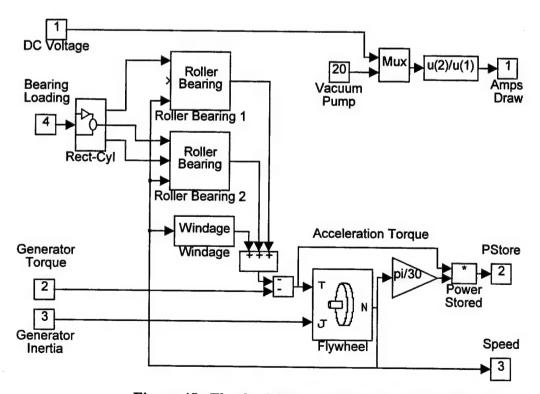


Figure 45. Flywheel Subsystem with Roller Bearings

The vacuum system is assumed to have a constant electrical power draw specified by the user. The inputs to the bearings are the forces on the bearings. These forces will be highly dependent on the mounting, with particular attention to whether gimbal mounting removes gyroscopic effects. The torque, which must be reacted by the bearings as radial forces to overcome gyroscopic effects, follows the following form:

 $\tau = J\omega_{rotor}\dot{\theta}$

where

t: reaction torque to rotate the flywheel (N-m)

J: moment of inertia of the rotor (Kg-m)

w_{rotor}: rotor speed (rad/sec)

 $\dot{\theta}$: rate of change of rotor position (rad/sec)

Because of the fairly high rotor speeds, a fairly low rate of change of rotor angle can generate a large gyroscopic torque. If a small bearing span is used this could generate large bearing forces. The equations to translate vehicle accelerations from the six degrees of freedom (X, Y, Z, yaw, pitch and roll) into bearing forces will be mounting dependent and is left to the system integrator.

3.2.1 Efficiency Calculation for Flywheel Energy Storage System

Inputs for the efficiency calculation subsystem 'Eff. Calc.' are the power going into stored energy and the power going into electrical energy. The efficiency calculation subsystem uses the following equations.

$$\begin{split} E_{out,discharge} &= \int_{P_{elect>0}} P_{elect} & E_{out,charge} &= \int_{P_{mech>0}} P_{mech} \\ E_{in,discharge} &= \int_{P_{elect>0}} P_{loss} + E_{out,discharge} & E_{in,charge} &= \int_{P_{elect<0}} P_{loss} + E_{out,charge} \end{split}$$

$$\eta_{discharge} = \frac{E_{out, discharge}}{E_{in, discharge}} \qquad \qquad \eta_{charge} = \frac{E_{out, charge}}{E_{in, charge}}$$

There is a case where electrical power flows into the flywheel energy storage system but stored energy also decreases. With the above equations, these losses are included in the efficiency calculation by counting them as charging losses.

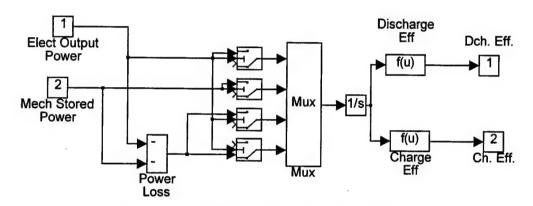


Figure 46. Flywheel Energy Storage Efficiency Calculation

3.2.2 Flywheel Battery System

A flywheel battery system can be defined as a flywheel energy storage system with an associated filter capacitor and controller to regulate a DC bus voltage. The relationship between the DC voltage and input current could be similar to a lead-acid battery, but a control scheme that maintains a fairly constant voltage can be used. A flywheel battery system with a simple feed-forward control and low gain feedback is shown. The feed-forward signal exactly balances the input current. There is a low gain feedback to keep the bus voltage near it's reference (300 volts in this case) to adjust for losses.

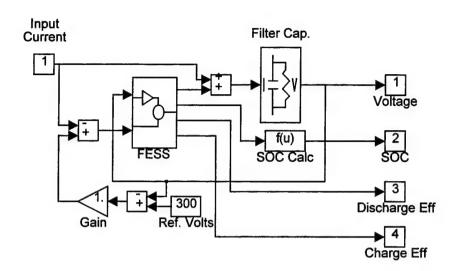


Figure 47. Simple Flywheel Battery System

3.3 Capacitor

Mathematical Model

$$I - \frac{V}{R} = C \frac{dV}{dt}$$

Units

current: Amps

voltage: Volts

resistance: Ohms

capacitance: Farads

Notes

inputs: 1 (current)

states: 1 (Voltage)

outputs: 1 (Voltage)

direct feedthrough: no

4.0 VEHICLE LIBRARY

4.1 Wheeled Vehicle (Version 1)

This wheeled vehicle model calculates all the load forces acting on the vehicle. The total load force is as follows:

$$F_{Load} = F_{aero} + F_{roll} + F_{grade}$$

where:

F_{load} [N]: Total resistance force acting on the vehicle

F_{aero} [N]: Aerodynamic load on vehicle

 F_{roll} [N]: Rolling resistance from the tires on the vehicle

F_{grade} [N]: Resistance as a result of the slope of the road (road grade force)

The aerodynamic drag force F_{aero} is expressed as a function of the vehicle frontal area (A), aerodynamic drag coefficient (C_d), the air density (r), the coefficient of yaw sensitivity (a), the normal (V_n) and parallel (V_p) wind velocity component, and the vehicle velocity (V) as follows:

$$F_{aero} = 0.5 \rho C_d A (V - V_p)^2 (1 + \alpha \tan^{-1} (\frac{V_n}{(V - V_p)}))$$

where:

F_{aero} [N]: Aerodynamic drag force

ρ [kg/m³]: Air density

Cd []: Aerodynamic drag coefficient

A [m²]: Vehicle frontal area

V [m/s]: Vehicle velocity

V_n [m/s]: Normal wind velocity component

Vp [m/s]: Parallel wind velocity component

 $\alpha[]$: Coefficient of yaw sensitivity

The rolling resistance force is expressed as follows:

$$F_{\text{roll}} = \mu \text{ Weight } \cos(\tau)$$

 $\mu = f_0 + 3.24 f_s \left(\frac{V}{100} \right)^{2.5}$ (2)

where:

V [mph]: V

Vehicle speed

m[]:

Coefficient of friction

Weight [N]:

Total vehicle weight

 $f_0[]$:

Coefficient of rolling resistance []

f_s[]:

Speed dependent coefficient of friction

The road grade force is expressed as follows:

$$F_{grade} = Weight sin(\alpha)$$
 2

where:

Weight [N]:

Total vehicle weight

 α [rad]:

Road gradient

4.2 Wheeled Vehicle (Version 2)

In this model, the vehicle is modeled as a single mass, whose acceleration is computed using Newton's second law of motion:

$$m_{eq}\ddot{x} = F_{driving} - F_{load}$$

where:

m_{eq} [kg]:

Equivalent mass of vehicle

x [rad/sec2]: Vehicle acceleration

F_{driving} [N]: Total driving force on vehicle

F_{load} [N]: Total resistance load on vehicle

The mass of vehicle takes fuel consumed mass (as fuel is consumed, total fuel mass decreases) into consideration. The vehicle acceleration is integrated once to determine vehicle speed, and again to determine vehicle position. The computation of F_{load} is the same as described in the wheeled vehicle version (1), with the exception of including Fbrake, which is provided by the driver model. Therefore, Fload is computed as follows:

$$F_{Load} = F_{aero} + F_{roll} + F_{grade} + F_{brake}$$

4.3 Wheel Model (Version 1)

Figure 48 shows the physical model of the vehicle and the driven wheel, along with all forces acting on the vehicle. The following is an explanation of all forces acting on the vehicle:

F_{load} [N]: Sum of all load forces opposing the motion of the vehicle. This

force comprises the Aero dynamic load and the gradient load.

 $F_f[N]$: The friction force acting on the surface of the tires as a result of the

friction coefficient between the tires and the road.

m [Kg]: The total mass of the vehicle (including the wheel mass)

x [m]: The linear displacement of the vehicle

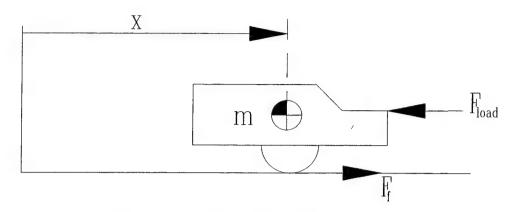


Figure 48. Physical Model of the Vehicle and Wheel

For the system shown in Figure 48, Newton's law can be formulated as follows:

$$m\ddot{x} = F_f - F_{load} (1)$$

Figure 49 shows the physical model of the wheel. The following is an explanation of the forces and moments acting on the wheel:

 T_d [Nm]: The driving torque on the wheel delivered from the axle

 $F_f[N]$: The friction force acting on the surface of the tires as a result of the

friction between the tires and the road.

 $J_W \, [kg \; m^2] \colon \quad \ \ \, \text{The mass moment of inertia of the wheel}$

q [rad]: The rotation in radians of the wheel

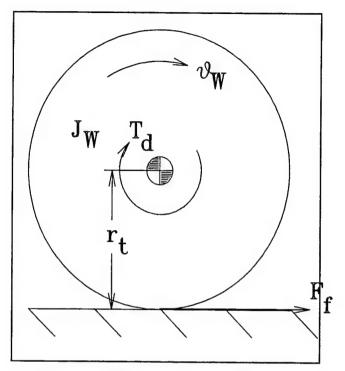


Figure 49. Physical Model Of The Wheel

Assuming a constant tire radius, Newton's law can be formulated for the wheel as follows:

$$J_w\ddot{\theta} = T_d - F_f r_t (2)$$

From Equation (1), F_f can be expressed as follows:

$$F_f = m\ddot{x} + F_{load} (3)$$

Combining equations (2) and (3), it follows:

$$\begin{split} J_W\ddot{\theta} &= T_d \text{-} m\ddot{x}_{T_t} \text{-} F_{load} \ r_t \\ \ddot{x} &= r_t \ddot{\theta} \\ J_W\ddot{\theta} &= T_d \text{-} m_T_t^2 \ddot{\theta} \text{-} F_{load} \ r_t \ (4) \\ (J_W + m_T^2) \ddot{\theta} &= T_d \text{-} F_{load} \ r_t \\ \ddot{\theta} &= \frac{T_d \text{-} F_{load} \ r_t}{J_W + m_T^2} \end{split}$$

4.4 Wheel Model (Version 2)

This wheel model converts the vehicle velocity into the rotational speed of the wheel, which is equal to the rotational speed of the output shaft of the axle. The axle or coupler connects the electric motor to the wheel.

$$\omega_{\text{wheel}} = V / r_{\text{wheel}}$$

where:

 ω_{wheel} [rad/sec]:Rotational speed of the wheel

r_{wheel} [m]:

Wheel radius

V [m/s]:

Vehicle linear velocity

The driving torque acting on the wheel is converted to driving force as follows:

$$F_{driving} = \frac{T_{axle_out}}{r_{wheel}}$$

where:

F_{driving} [N]:

Total driving force acting on vehicle

 $T_{\text{axle_out}}\left[Nm\right]\!\!:$

Total output torque delivered from axle

 r_{wheel} [m]:

Wheel radius

If the entire mass of the vehicle is regarded as concentrated at the wheel mass center, then the total inertia of the wheel can be computed as follows:

$$m_{eq} * r_{wheel}^2 = (1/2 * mwheel * rwheel}^2 + Jaxle_out$$

where:

meq [Kg]:

Equivalent vehicle mass

rwheel[m]:

Wheel radius

Jaxle outpt [kgm²]:

Output Inertia of axle

5.0 COUPLINGS LIBRARY

5.1 Motor Wheel Coupling (Version 1)

Figure 50 shows the physical model of the motor wheel coupling as well as the free body diagram for each gear. The following is an explanation of all forces and moments shown in Figure 50:

T₁ [Nm]: Torque at the input side of the coupler model

T₂ [Nm]: Torque at the output side of the coupler model

F [N]: The contact force between gear 1 and gear 2

q₁ [rad]: The rotation of the shaft at the input side of the coupler model

 q_2 [rad]: The rotation of the shaft at the output side of the coupler model

J₁ [kgm²]: Inertia at the input side of the coupler model

J₂ [kgm²]: Inertia at the output side of the coupler model

r₁ [m]: Radius of input gear of the coupler model

 r_2 [m]: Radius of output gear of the coupler model

G []: Gear ratio of the coupler

η[]: Coupler efficiency

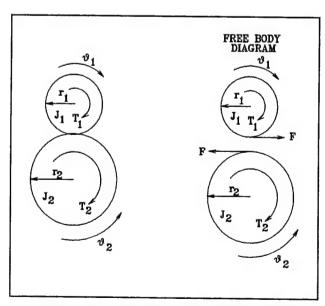


Figure 50. The Coupler Physical Model

Newton's law can be formulated for both gears as follows:

$$\ddot{\theta}_{1} = \frac{T_{1} - Fr_{1}}{J_{1}}$$

$$\ddot{\theta}_{2} = \frac{Fr_{2} - T_{2}}{J_{2}}$$

$$\frac{\ddot{\theta}_{1}}{\ddot{\theta}_{2}} = \frac{\dot{\theta}_{1}}{\dot{\theta}_{2}} = \frac{r_{2}}{r_{1}} = G$$

$$\therefore F = \frac{(J_{2}\ddot{\theta}_{2} + T_{2})}{r_{2}} ; \quad \ddot{\theta}_{1} = \ddot{\theta}_{2}G$$

From equation (1), the coupler model can be formulated as follows (traction):

$$\ddot{\theta}_2 G J_1 - T_1 = -\frac{1}{G} (J_2 \ddot{\theta}_2 + T_2)$$

$$T_2 = [T_1 - (G J_1 + (\frac{1}{G}) J_2 \ddot{\theta}_2)] G \eta$$

The output torque T2 of the coupler in regen mode is then:

$$T_2 = [T_1 - (GJ_1 + (\frac{1}{G})J_2\ddot{\theta}_2]G(\frac{1}{\eta})$$

5.2 Motor Wheel Coupling (Version 2)

This model computes the total inertia as seen by the wheel as follows:

$$(J_{in} + J_{ingear})G^2 + J_{outgear} = J_{wheel}$$

where:

 J_{in} [kgm²]: Inertia of the rotor of the motor

J_{ingear} [kgm²]: Inertia of the input side of the gear coupler between the motor and wheel

G[]: Gear ratio of coupler

 J_{outgear} [kgm²]: Inertia of the output side of the gear coupler between the motor and wheel

J_{wheel} [kgm²]: Total inertia that the wheel has to accelerate

The gear ratio is defined as follows:

$$G = \frac{N_{in}}{N_{out}}$$

where:

 $N_{in}[rpm]$:

Rotational speed at the input side of the coupler

N_{out}[rpm]:

Rotational speed at the output side of the coupler

The torque output of the coupler is computed as follows (traction mode):

$$T_{out} = T_{in}G\eta$$

The torque output of the coupler is computed as follows (regen mode):

$$T_{\text{out}} = T_{\text{in}}G(\frac{1}{\eta})$$

where:

Tout [Nm]:

Torque to drive wheel

Tin [Nm]:

Torque inputted into coupler from motor

G[]:

Gear ratio

η[]:

Coupler efficiency

6.0 MISCELLANEOUS LIBRARY

The equations used in this library are briefly discussed in the User's manual. Therefore, the reader is referred to the User's Manual for the equations describing the models of the miscellaneous library.

HYBRID ELECTRIC VEHICLE SIMULINK TOOLBOX

(Commercial Vehicle Version)

PATHS Validation
Draft Copy

Version 1.1

EXECUTIVE SUMMARY

The following report summarizes the efforts to validate PATHS, a modeling and simulation software for electric and hybrid vehicles. Due to time and budget constraints, it was impossible to validate all the components of the PATHS software. Therefore, only key components of PATHS were validated. The APU, AC induction motor, lead acid and driver-axle-wheel-vehicle combined models were validated. These are the components that are principally used to model a commercial hybrid vehicle.

Validation was performed by first developing a computer model of a 22-foot series hybrid shuttle bus, followed by comparing its output to data collected from the same bus on a dynamometer. Section 1 describes the series hybrid bus and the driving profiles used during validation.

Section 1.1 describes the results of the APU model validation. Fuel consumption and CO (Carbon Monoxide) and NOx (Nitrogen Oxide) emissions were measured and compared with model predictions. Model and measured data agreed with each other to within less than 5%, while considerably larger deviations up to 100% were observed between measured and model predicted CO and NOx emissions. This can be largely attributed to insufficient emissions data obtained from the manufacturer.

Section 1.2 describes the validation of the AC induction motor model. The consumed motor current in motor mode and regenerated current in generator mode were compared with data collected from the motors of the bus. The model predicts transient and steady-state operations of the motor within 10%, except for measured motor current spikes in current draw and regeneration.

Section 1.3 describes the validation of the lead acid battery model. Battery state of charge and voltage predicted by the model were compared with measured data from the hybrid bus. The model predicted battery state of charge compared within 5% to the measured data of the same. Larger deviations were observed with the comparison of the model predicted and measured battery voltage.

Section 1.4 describes the validation of the combined driver-axle-wheel-vehicle model.

Finally, Section 2.0 describes the hybrid bus model of the 22-foot series hybrid shuttle bus that was used to validate PATHS.

Section 3.0 provides concluding comments on this validation report.

1.0 INTRODUCTION

This document comprises the validation and testing of the main components of PATHS. The reader is referred to the User's Guide and Technical Notes for a more detailed description of PATHS. The validation includes the following main models of PATHS. These are the models that are used at a minimum to model a general series hybrid vehicle.

- APU model from the engine library
- AC induction motor model (including inverter) from the electric machine library
- Lead acid battery model from the energy storage library
- Driver-axle-wheel-vehicle combined model

The data for the validation of the above components was obtained from a 22-foot series hybrid shuttle bus developed by the Electricore consortium. This bus has a 35-kW, CNG-fueled Auxiliary Power Unit (APU) with two battery packs, each containing 26 lead-acid batteries. The vehicle is propelled by two 70-kW (peak), AC-induction wheel motors, one on each side of the rear wheels. A fixed ratio speed reducer of 20:1 is integrated into the motor before the output to the wheels.

The hybrid bus was placed on a heavy-duty chassis dynamometer at Southwest Research Institute (SwRI) and operated on two driving cycles: the CBD and EPA schedule D driving cycles. Figure 51 shows the CBD driving profile, and Figure 52 illustrates the EPA schedule D driving profile.

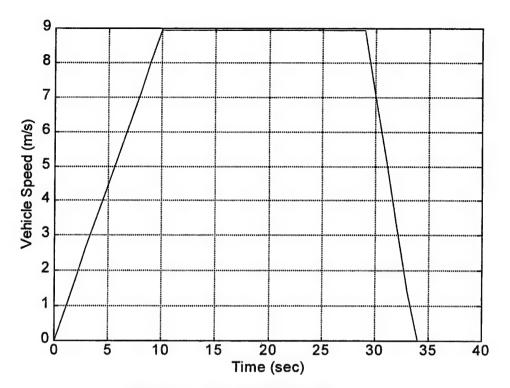


Figure 51. CBD Driving Profile

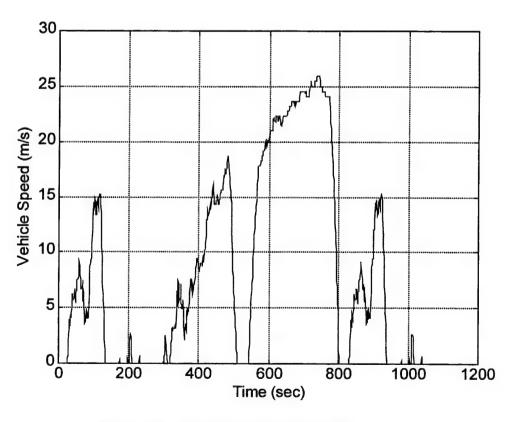


Figure 52. Schedule D Driving Profile

Data was collected over six consecutive EPA schedule D and ten CBD-14 driving cycles respectively. A CBD-14 driving profile consists of 14 consecutive CBD segments (see Figure 50 for one CBD driving segment). For each of the aforementioned driving cycles, the following data was collected on a second-by-second basis:

- Bus voltage (volts)
- Vehicle speed (miles per hour)
- APU engine speed (rpm)
- Accelerator pedal position (0-1)
- Brake pedal position (0-1)
- Current into and out of left motor inverter (DC amps)
- Current into and out of right motor inverter (DC Amps)
- Current into and out of left battery pack (DC Amps)
- Current into and out of right battery pack (DC Amps)
- Generator current (DC Amps)
- Battery pack state of charge (%)

The following sections describe the validation results of the main components of PATHS.

1.1 APU Model Validation

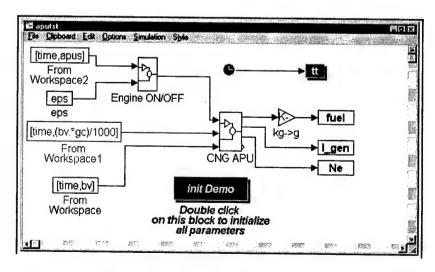


Figure 53. APU Model Validation

The APU model shown in Figure 53 is of the table look-up type and models a 35 kW CNG engine, coupled to a permanent magnet generator. Table 27 describes the inputs and outputs of the APU model.

| Table 27. APU MODEL | |
|-----------------------------|-----------------------------|
| INPUTS | OUTPUTS |
| Engine on/off state | Mass of fuel consumed (kg) |
| Desired electric power (kW) | Generator current (DC Amps) |
| Battery voltage (volts) | Engine speed (rpm) |
| | APU inertia (kgm²) |

The APU model was tested by providing collected test data on bus voltage and generator current (the electric power is equal to the product of the bus voltage and generator current) as inputs to the model and comparing the model outputs of fuel consumed and engine speed with measured data of the same. Figure 54 shows a comparison of fuel consumed as predicted by the APU model and measured fuel consumption data. Figure 55a and 55b illustrate a comparison of the APU emissions (HC and Nox) predicted by the model and the collected data.

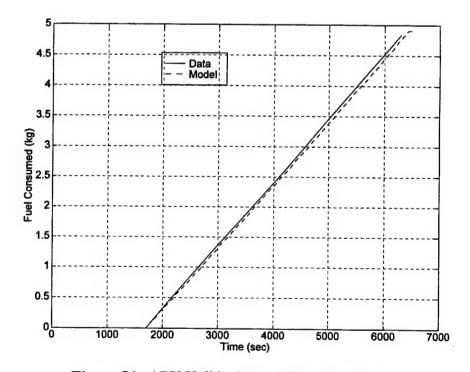


Figure 54. APU Validation – 6 EPA Schedule D

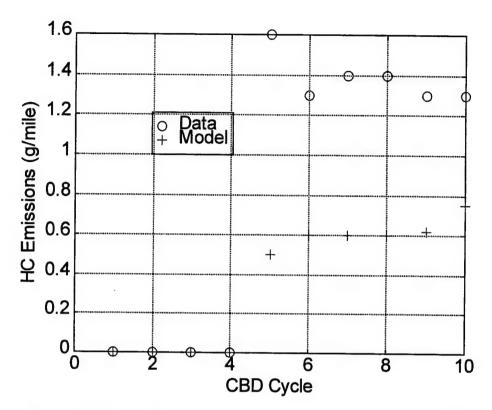


Figure 55a. APU Model Validation -10 CBD Driving Cycles (HC Emissions)

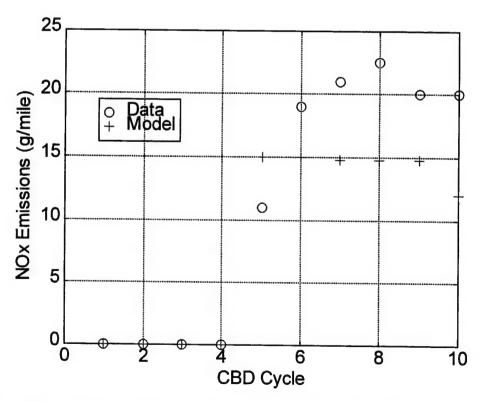


Figure 55b. APU Model Validation -10 CBD Driving Cycles (NOx Emissions)

1.2 AC Induction Motor Model

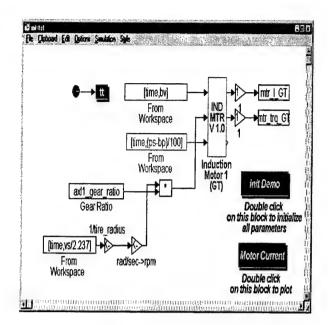


Figure 56. AC Induction Motor

The AC induction motor model must have several parameters defined prior to integration into a hybrid vehicle simulation model. The essential motor model parameters are described in Table 28.

| Table 28. AC INDUCTION MOTOR MODEL PARAMETERS | |
|---|--|
| P (hp): | Rated power of motor |
| V (volts) | Rated operating voltage |
| f (Hz) | Rated operating frequency |
| n(rpm) | Rated speed |
| CL(hp) | Core losses at rated voltage and speed |
| SLL(hp) | Stray load losses at rated voltage and speed |
| Rs(Ω) | Per phase stator resistance |
| Rr(Ω) | Per phase rotor resistance |
| Lls(H) | Per phase stator leakage inductance |
| Lir(H) | Per phase rotor leakage resistance |
| Lm(H) | Per phase magnetizing inductance |
| η (-) | Inverter efficiency |
| I(kgm²) | motor inertia |
| sample_N | Number of samples saved to workspace |
| sample_T | Time between each saved sample |

The above parameters must be matched for an individual motor by means of the full-throttle torque speed curve of the motor. The full throttle and part throttle torque speed curves for the 70 kW AC induction motor are illustrated in Figure 57. An iterative procedure was used to match the motor parameters to produce the torque speed characteristics shown in Figure 57. Figure 58 shows the motor model predicted torque speed characteristics superimposed on that of Figure 57. The final motor parameters that were used to simulate the hybrid bus are defined in the model mask, illustrated in Figure 58.

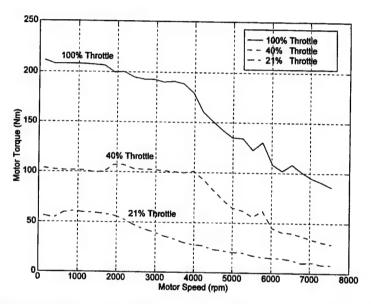


Figure 57. System Voltage = 312V - Measured Motor Data

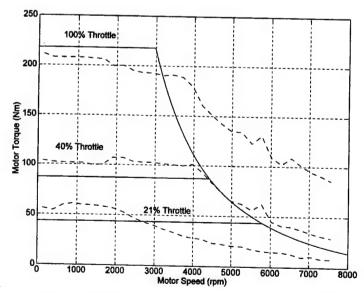


Figure 58. System Voltage = 312 V - Measured Motor Data vs. Model

| Block name: moti1_module Block type: SS Induction Motor Sys () | OK |
|--|----------------|
| SS Induction Motor/Inverter System | Cancel Help |
| Rated [P(hp),V(V),f(Hz)]: | |
| [114,312,135] | |
| Rated [n(rpm),CL(hp),SLL(hp)]: | |
| [4000,10,10] | |
| [Rs,Rr in ohms, Lls,Llr,Lm in H]: | |
| [0.01983,0.01235,42.5E-6,42.5E-6,2.5E-3] | |
| Inverter Efficiency: | |
| 0.98 | |
| Machine Inertia(kg*m*m): | |
| 0.02821 | |
| [sample_N,sample_T]: | |
| [20000,0.1] | |

Figure 59. SS Induction Motor Sys (Mask)

| Table 29. AC INDUCTION MOTOR MODEL | |
|------------------------------------|-------------------------|
| INPUTS | OUTPUTS |
| Bus voltage (V) | Motor current (DC Amps) |
| Motor speed (rpm) | Motor torque (Nm) |
| Torque command (0-1) | Motor inertia (kgm²) |

The motor model was validated by providing collected test data on bus voltage, torque command from driver accelerator and brake pedal, and vehicle speed as inputs to the model and comparing the model outputs of current and torque with measured data of the same. Figure 60 shows a comparison of the model predicted current and measured data for the first 500 seconds of the EPA schedule D driving profile. Figure 61 shows the same comparison for the last 500 seconds of the same driving profile.

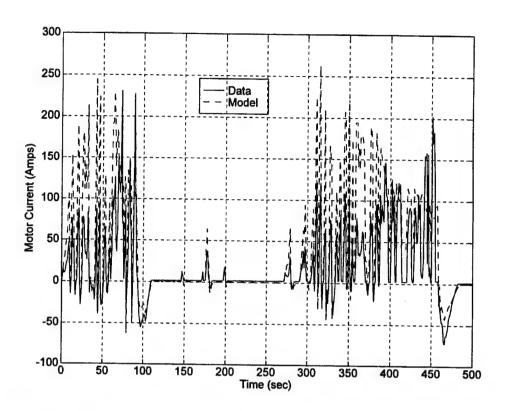


Figure 60. Motor Model Validation - 1 EPA Schedule D (first 500 seconds)

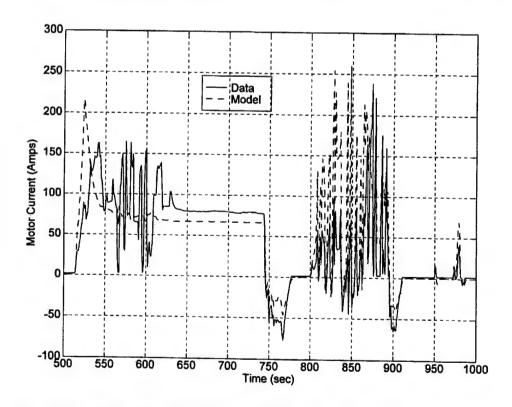


Figure 61. Motor Model Validation - EPA Schedule D (last 500 seconds)

1.3 Lead Acid Battery Model

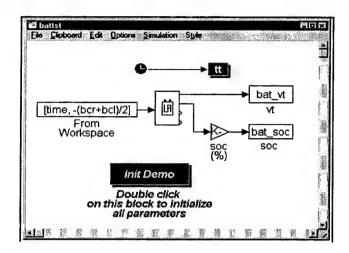


Figure 62. Lead Acid Battery Model

The lead acid battery model parameters are presented in Table 30.

| Table 30. LEAD ACID BATTERY MODEL PARAMETERS | |
|---|---------|
| Number of batteries | (-) |
| Open circuit voltage of a battery | (volts) |
| Internal resistance of the battery | (Ω) |
| Polarization resistance of the battery (Ω) | (Ω) |
| Battery capacitance | (F) |
| Terminal battery resistance | (Ω) |
| Terminal battery capacitance | (Ω) |
| Discharge capacity at a 5 hour rate and 30° Celsius | (A-hr) |
| Discharge current at a 5 hour rate and 30° Celsius | (A) |
| Charge efficiency | (0-1) |
| Discharge efficiency | (0-1) |
| Operating temperature | (° C) |
| Initial polarization voltage | (V) |
| Initial state of charge | (0-100) |

The hybrid bus is equipped with two battery packs, each containing 26 batteries. The above parameters needed for the model were obtained from the battery manufacturer and are entered into the model mask, illustrated in Figure 63. Note the mask represents a battery pack containing 26 batteries.

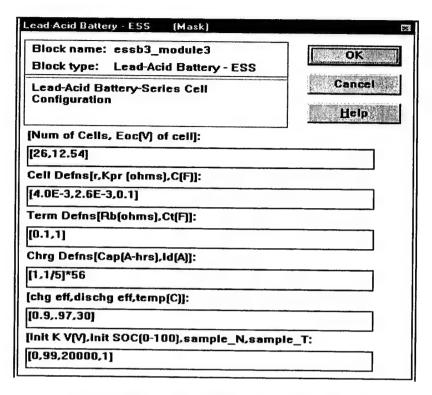


Figure 63. <u>Lead-Acid Battery – ESS (Mask)</u>

The input and outputs of the battery model are described in Table 31.

| Table 31. BATTERY MODEL | |
|------------------------------------|-------------------------|
| Inputs | Outputs |
| Charge/discharge current (DC Amps) | Battery voltage (volts) |
| | State of charge (0-1) |

The battery model was validated by supplying to the battery model input the measured charge/discharge current and comparing the model predicted battery pack state of charge and voltage with measured data. Figure 64 shows a comparison of the battery state of charge as predicted by the model and measured on the bus. Figure 65 shows a comparison of the battery voltage as predicted by the model and measured on the bus using the EPA Schedule D test.

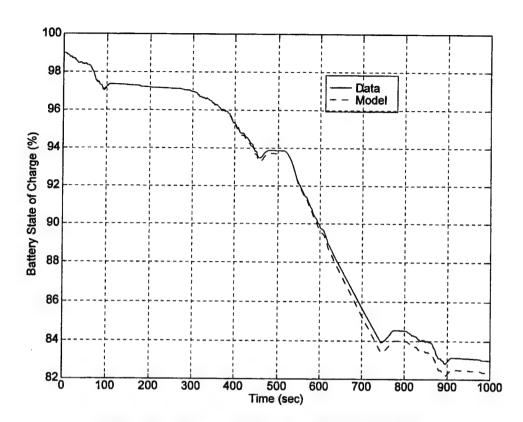


Figure 64. Battery Validation- EPA Schedule D

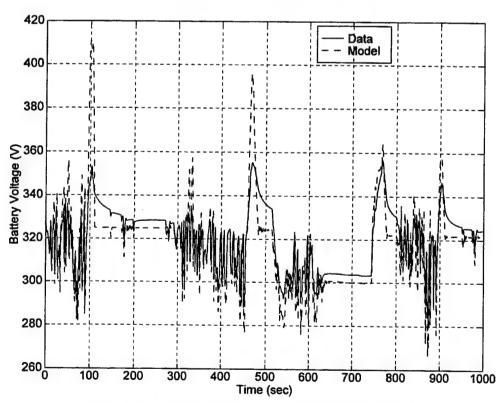


Figure 65. Battery Validation – EPA Schedule D

1.4 Driver-Axle-Wheel-Vehicle Combined Model

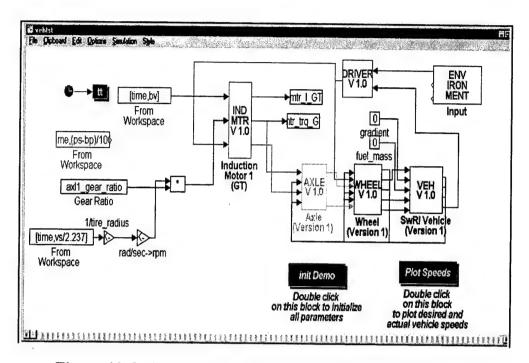


Figure 66. Driver-Axle-Wheel-Vehicle Combined Model

This combined model consists of four component models. The nature of the available test data required us to combine these four components into a single model for testing and validation purposes. The Tables 32-35 summarize the inputs and outputs of each of the component models.

| Table 32. DRIVER MODEL | |
|-----------------------------|--------------------|
| INPUTS | OUTPUTS |
| Desired vehicle speed (m/s) | Power demand (0-1) |
| Actual vehicle speed (m/s) | |

| Table 33. AXLE MODEL | |
|--------------------------|----------------------------------|
| INPUTS | OUTPUTS |
| Input torque (Nm) | Output torque (Nm) |
| Output shaft speed (rpm) | Input shaft speed (rpm) |
| Input inertia (kgm²) | Equivalent output inertia (kgm²) |

| Table 34. WHEEL MODEL | |
|-------------------------------------|--------------------------------|
| INPUTS | OUTPUTS |
| Maximum traction force (N) | Rotational wheel speed (rpm) |
| Power demand from driver (0-1) | Vehicle speed (m/s) |
| Torque at input (Nm) | Vehicle acceleration (m/s²) |
| Total resistive load (N) | Wheel moment of inertia (kgm²) |
| Total vehicle mass (kg) | Service brake force (N) |
| Equivalent inertia (kgm²) from axle | |

| Table 35. VEHICLE MODEL | |
|-----------------------------|----------------------------|
| INPUTS | OUTPUTS |
| Vehicle speed (m/s) | Total load on vehicle (N) |
| Gradient (radians) | Maximum traction force (N) |
| Fuel mass consumed (kg) | Vehicle speed (m/s) |
| Vehicle acceleration (m/s²) | Total vehicle mass (kg) |
| Service brake force (N) | |

Figure 67 shows a comparison of the pedal and brake positions between the measured data and that predicted by the driver model, while following the EPA - schedule D driving profile.

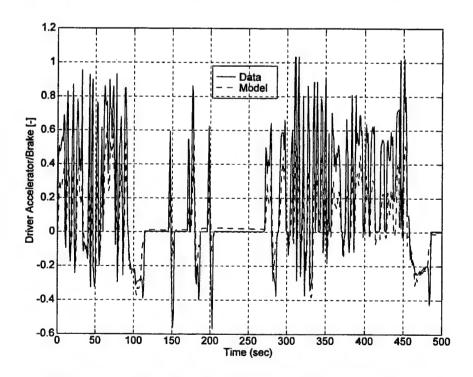


Figure 67. <u>Driver Model Validation – EPA Schedule D</u>

2.0 Hybrid Bus Model

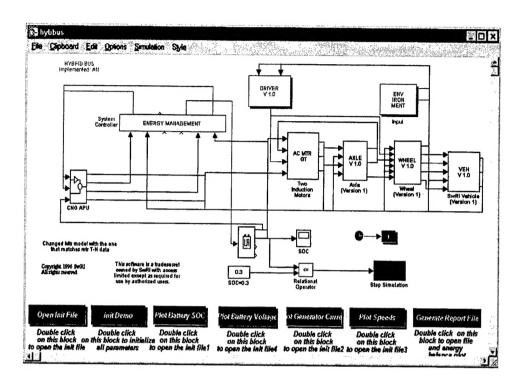


Figure 68. Hybrid Bus Model

The subcomponents described in Sections 1.1 to 1.4 were combined to model a 22-foot series hybrid shuttle bus developed by the Electricore consortium. As described in Section 1, this bus is equipped with two 70-kW wheel, AC-induction motors, a 35-kW CNG-fueled APU, and two battery packs, each containing 26 lead-acid batteries. The weight of the hybrid bus is approximately 14,600 pounds (empty weight plus an estimated 10 passengers). The inertia weight for the chassis dynamometer was computed from this estimate of the bus weight. Based on the frontal area and drag coefficient, the road load was estimated at 52 hp at a speed of 50 mph. The rolling resistance was computed to be 17 hp and the aerodynamic losses were computed as 35 hp. The power management controller turned the APU on when the battery state of charge fell below 75%, and turned the APU off when the battery state of charge increased above 85%. The electrical power requested from the APU was a function of state of charge, that is user modifiable. Figure 69 shows the model of the hybrid bus using the components described in Sections 1.1 to 1.4.

Figure 69 shows a comparison of the battery state of charge, while the hybrid bus was operated over 6 EPA-Schedule D driving profiles. Figure 70 shows the relative error of the model predicted battery voltage with respect to the measured data during operation over 6 EPA-Schedule D driving profiles. Figure 71 compares the vehicle speed predicted by the model with data measured on the dynamometer test stand.

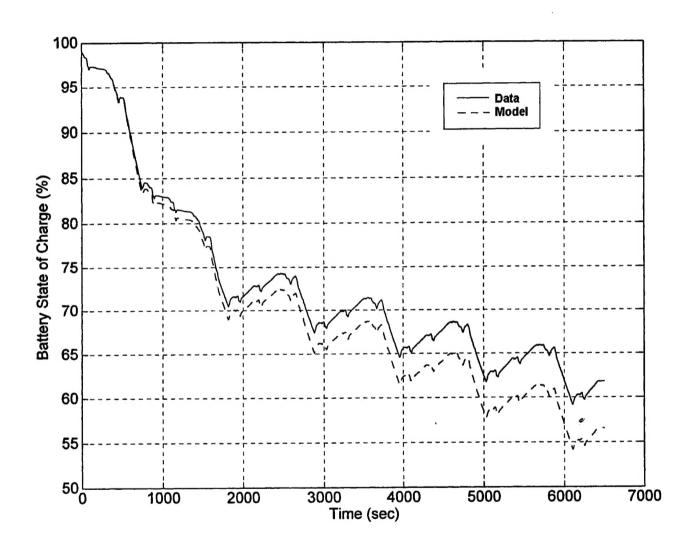


Figure 69. Hybrid Bus Model Validation - EPA Schedule D

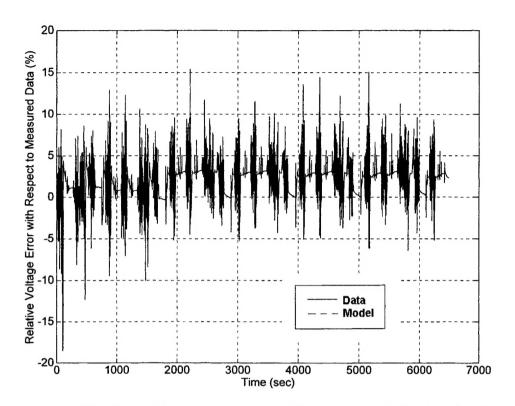


Figure 70. Hybrid Bus Model Validation - EPA Schedule D (Battery Voltage)

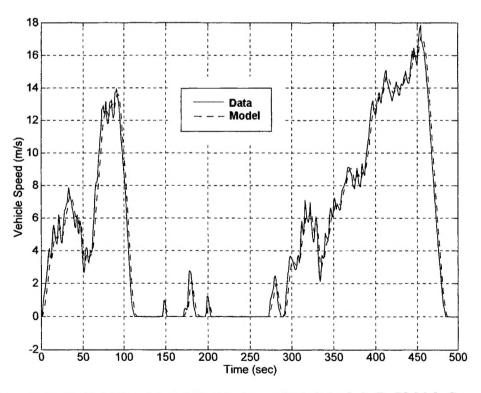


Figure 71. Hybrid Bus Model Validation - EPA Schedule D (Vehicle Speed)

3.0 CONCLUSIONS

This document describes the first attempt to validate PATHS. The validation exercise was limited to key components from the many libraries of PATHS. The validation was performed by comparing the model predictions with data collected from a hybrid bus operating on EPA and CBD driving profiles. The models that were validated appear to agree with the test data reasonably well. The results that are described in this report lend significant credibility in applying PATHS to designing and building hybrid vehicles.

It is apparent that some models compare very well with measured data, while others do not. For example, the APU model was able to predict fuel consumption to within 1% of the measured data, while predictions of the HC emissions were off by almost a 100%. Although the predicted battery state of charge compared quite well to the measured data (within less than 5%), the predicted battery voltage was sometimes much larger than what was measured. However, it was remarkable to observe the trends were duplicated throughout the driving profile.

Ideally, changes to the model would have to be made after performing the described validation exercise in order to refine and develop a better model. There were no funds remaining for this task, but we hope that funding will be available for this important task in the future.

The validation results have provided the much-needed confidence to use PATHS in designing and developing a hybrid or pure electric vehicle. We hope that it will find more widespread usage throughout the electric/hybrid vehicle industry and become an accepted design tool.